Integrated-Optic Electrorefraction Modulators

by

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Abstract

The large electroabsorption (EA) and electrorefraction (ER) effects that can be achieved in coupled quantum well (CQW) structures give these structures great potential for use in intensity, phase, and polarization modulators for future optical links. This thesis focuses on designing structures that will result in state-of-the-art performance of CQW-based modulators.

In this thesis, a design for a push-pull polarization-modulation scheme is presented, and it requires placing multiple repetitions of two different CQW structures in the optical waveguide of the proposed polarization modulator. The main function of one of the two structures is to provide a large increase of the refractive index for the TM polarization, without a proportionate increase of the refractive index for the TE polarization. It is shown that this effect can be achieved by anticrossing light holes. The main function of the other structure is to provide a large decrease of the refractive index for the TE polarization, without a proportionate decrease of the refractive index for the TM polarization. It is shown that, although this effect can be efficiently achieved by anticrossing heavy holes, the CQW structures that achieve this effect by anticrossing electrons are less sensitive to the layer thickness and compositional variations that may be expected during the growth process. The large EA and ER effects in CQW structures are typically seriously compromised by the layer variations, and, it is shown in this thesis that decreasing the confinement of the anticrossing wave functions can decrease the sensitivities of the CQW structures to these variations. In addition, the very small confinement of light holes in the InGaAlAs-based material systems together with the small sensitivity of the light-hole band edge to the compositional variations, make the anticrossing of the light holes the most robust-to-growth and, therefore, the most promising mode of operation for CQW-based ER intensity, phase, and polarization modulators.

The absorption spectra of the novel CQW structures designed in this thesis are obtained using the variational method for solving the 1S exciton equation in the effective-mass, envelope-function approximation, and the electric-field-induced refractive index changes are obtained using the Kramers–Krönig relations.
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List of Abbreviations

ACQW  Asymmetric Coupled Quantum Well
AWG  Arrayed Waveguide Grating
CATV  Cable Television
CQW  Coupled Quantum Well
DFB  Distributed Feedback
DGD  Differential Group Delay
EA  Electroabsorption
EDFA  Eearbium-Doped Fiber Amplifier
ER  Electrorefraction
HWHM  Half-Width-at-Half-Maximum
ITU  International Telecommunication Union
LAN  Local-Area Network
MQW  Multiple Quantum Well
NRZ  Non-Return-to-Zero
OOK  On-Off Keying
PCS  Personal Communications Services
QCSE  Quantum-Confined Stark Effect
QWPC  Quantum Well Polarization Conversion
RF  Radio Frequency
RZ  Return-to-Zero
RZ-DPSK  Return-to-Zero Differential-Phase-Shift-Keyed
SCM  Sub-Carriers Multiplexing
SNR  Signal-to-Noise Ratio
SQW  Square Quantum Well
TE  Transverse-Electric
TDM  Time-Division Multiplexing
TM  Transverse-Magnetic
VCSEL  Vertical-Cavity Surface-Emitting
WDM  Wavelength-Division Multiplexing
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Co-Authorship Statement

The work presented in this thesis was a collaboration between me and my supervisor, in which I took the leading role.
Chapter 1
Introduction

High-speed optical fiber communication networks play a vital role in the ongoing information revolution. Consequently, there is a huge demand for improving performance of the optical networks and their components, such as: semiconductor lasers, photodetectors, and electro-optic modulators. The research objective of this thesis is to make a contribution to the area of optical communications by pursuing the development of InGaAlAs-based electro-optic modulators using coupled quantum well (CQW) structures [1]–[3]. Electro-optic modulators based on CQW structures have the potential to become a leading technology for efficient high-speed conversion of electrical into optical signals, not only in optical communications but also in signal processing and instrumentation. This is mainly because CQW structures provide very large electroabsorption effect (electric-field-induced change of optical absorption) and electrorefraction effect (electric-field-induced change of refractive index) and should enable modulators based on them to have shorter lengths and lower drive voltages than
modulators based on square quantum wells or on the linear electro-optic effect. Both the short lengths and the low drive voltages possible with CQW modulators will be essential requirements for next-generation high-speed optical networks, which will, in turn, require electro-optic modulators having bandwidths of 100 GHz and above. [4]

In this thesis, a design for the first push-pull polarization modulator that is based on any type of quantum well structure is presented [1]. The effect is achieved by placing multiple repetitions of two types of CQW structure in the optical waveguide of the modulator. Upon the application of an electric field normal to the planes of the quantum wells, one of the structures mainly provides a positive change of the refractive index for the TM polarization, while the other structure mainly provides a similar negative change of the refractive index for the TE polarization. As a result, an input polarization state containing equal powers in both the TE and TM fundamental modes of the waveguide can be switched between orthogonal states. Polarization modulation has been traditionally associated with linear electro-optic modulators, and it has been used in an increasing number of modulation schemes, which have provided considerable improvements to the systems using them [5]. The CQW polarization modulator design presented in this thesis will enable these modulation schemes to be applied in next-generation high-speed optical networks as well.
Although they provide large electroabsorption and electrorefraction effects, CQW structures are quite sensitive to the layer thickness and compositional variations that are likely to occur in their quantum well layers during growth processes [2], [3]. The layer variations severely affect the properties of CQW structures, reducing the magnitude of the electroabsorption and electrorefraction effects that can be achieved. This thesis also presents a method that can be used to decrease the sensitivities of CQW structures to layer variations and, thus, significantly improve the magnitude of the electroabsorption and electrorefraction effects achievable with these structures. The method is mainly based on decreasing confinement of the electronic states in the CQW structures to their quantum well layers [3], and it can be used to improve not only the performance of the polarization modulator, but also the performance of electroabsorption and electrorefraction modulators in general. The large improvement achievable is expected to make a considerable impact on the state-of-the-art of electro-optic modulators.

The discussion of CQW modulators begins in Section 1.5 of this Introduction, Chapter 1, and continues throughout Chapters 2–6, which contain manuscripts that have been published, have been submitted for publication, or will be submitted for publication in journals. The last chapter of this thesis, Chapter 7, presents a discussions that relates Chapters 2–6 to each other, and to the field of optical fiber communications in general, and it also gives recommendations for future work on CQW modulators. The remainder of the Introduction starts with a discussion of analog and digital optical links (Section
1.1 Optical Fiber Communications

Today's global need for greater telecommunication network capacities seems insatiable. In the 1970s, the transmission loss of optical fibers was reduced to only ~0.5 dB/km within a 12 THz spectral region near 1310 nm and to only ~0.2 dB/km within a 15 THz spectral region near 1550 nm [6]. It was clear that data transmission capacities of optical
fibers would eventually overshadow those achievable with the copper wire [7]. Subsequently, a global research effort was initiated in order to develop optical transmitters and receivers operating around both 1310 nm and 1550 nm. Although the spectral region around 1550 nm has smaller optical loss than that around 1310 nm, and is dominant in long-haul communications, the region near 1310 nm has also been widely used in fiber-optic communications as the group-velocity dispersion is zero, i.e., the dispersion changes sign, close to 1310 nm. Besides optical loss, group-velocity dispersion in fibers is one of the most important properties limiting the performance of a communication system [8]. It is also worth mentioning that the first-generation fiber-optic systems operated in the region near 800 nm using multimode fiber. The relatively large loss in this region (~2.5 dB/km) and the intermodal dispersion [8] limited digital systems to bit rates of only ~45 Mbps and repeater spacing of only ~10 km [7]. Due to its cost-effectiveness and maturity, this short-wavelength technology has reemerged recently in short-haul applications, such as in local-area networks (LANs) [9].

1.1.1 Digital Communications

The majority of fiber-optic systems are digital and operate in the spectral range around 1550 nm. In these systems, data are typically encoded in binary representation. Among the various characteristics of lightwaves that can be modulated, e.g., intensity, phase, frequency, and polarization, intensity modulation has been most commonly used mainly
because of the simplicity of the envelope photodetection [10]. Therefore, as will be explained in more detail below, optical transmitters are realized either by direct modulation or by external modulation of the intensity of light coming out of a semiconductor laser. In direct-modulation transmitters, the current of a semiconductor laser is directly modulated by the binary electrical data stream, which switches the intensity of the laser's output from the "on" state (maximum light intensity at the output) to the "off" state (almost no light at the output), and vice versa [11], see Fig. 1.1(a). In external-modulation transmitters, the intensity of light from a semiconductor laser is switched on and off by an external optical modulator, which has its electrical port driven by the digital data stream [10], see Fig. 1.1(b). The on-off modulation in digital optical systems is also referred to as on-off keying (OOK).

Figure 1.1: Schematics of an optical transmitter for digital communications: (a) directly-modulated semiconductor laser and (b) externally-modulated semiconductor laser.

In order to maximize the transmission capacity of a digital fiber-optic network, many different data streams at lower bit rates are commonly multiplexed to achieve higher bit rates in a single optical channel operating at a single wavelength. Typically, the
interleaving is done electronically, and is referred to as time-division multiplexing (TDM). The highest transmission rate in commercially available TDM systems is around 10 Gbps for each channel [12]. Many researchers are working on the next generation of TDM systems that will operate at 40 Gbps data rates. Traditionally, when planning future networks, service providers expect a fourfold increase in a network capacity at about 2.5 times the cost of the network equipment [13]. In combination with the TDM, commercial digital fiber-optic networks employ wavelength-division multiplexing (WDM), increasing the transmission capacities to about 1 Tbps [12]. In WDM links, many 10 Gbps (or lower bit rate) channels, each at a different carrier wavelength ($\lambda$), are multiplexed onto the same single-mode fiber using, for example, an arrayed waveguide grating (AWG) [14], as shown in Fig. 1.2. The channels form an infinite frequency grid centered at 193.1 THz, and are typically separated by 50 or 100 GHz, as regulated by the International Telecommunication Union (ITU) [12]. As also shown in Fig. 1.2, the multiplexed light is amplified by a cascade of erbium-doped fiber amplifiers (EDFAs), with about 100 km spacing between them [7], before entering the AWG demultiplexer at the other side of the link. Due to their ability to simultaneously amplify, in the optical domain, many WDM channels in the low-loss 1550 nm spectral region, EDFAs play a very important role in fiber-optic communications [15]. The gains of EDFAs cover the whole C-band (1530 nm–1565 nm) and a large part of the L-band (1565 nm–1625 nm), i.e., the spectrum between 1565 nm and 1610 nm. For amplification of wavelengths shorter than these, including those around 1310 nm, Raman amplifiers are commonly
used [14] (Raman amplifiers are also used to complement EDFAs in ultra-long-haul systems). As shown in Fig. 1.2, at the end of a WDM link, which can be several thousand kilometers long [7], each channel is demultiplexed and passed to a separate receiver, which is a fast photodetector, for a simple envelope demodulation [14].

![Figure 1.2: Schematics of a wavelength-division-multiplexed digital fiber-optic link.](image)

**1.1.2 Analog Communications**

Although the vast majority of fiber-optic links are digital, there are an increasing number of applications for analog fiber-optic links. They are used for faithful transmission of RF signals over distances that are typically not as long as the distances covered by most digital links but are still too long for the use of coaxial cables. For example, the standard 3/8" coaxial cable exhibits a transmission loss of over 50 dB/km at the frequency of 1 GHz [16]. The fact that analog links mainly span relatively short distances makes the zero-dispersion 1310 nm spectral region very popular for these applications because the relatively high loss in the spectral region is not a limiting factor for short distances [11].
Similar to digital links, in analog links, transmitters are based on direct or external intensity modulation of semiconductor lasers, and the receivers are simply high-speed photodetectors. However, in analog links, the light intensity of the carrier is not switched on-off, but, rather, small-signal modulation is used in order to faithfully transmit the RF signal over the link. Small-signal modulation in analog links is more bandwidth-efficient than the OOK in digital links, and it also circumvents the costly analog-to-digital and digital-to-analog data conversion.

Some of the applications of analog links include the up-link (down-link) for cellular/PCS antenna remoting (here, PCS stands for Personal Communications Services), and transmit (receive) function in radar systems. Also, one of the first, and perhaps most commercial, applications of analog links was the distribution of cable television (CATV) signals [17]. Depending on the application, analog links can use only a single optical carrier, or they can employ wavelength-division multiplexing, similar to the digital links [18]. Also, similar to the TDM used in digital links for combining multiple signals into a single channel at a certain wavelength, sub-carrier multiplexing (SCM) is used in CATV systems to electronically combine multiple low-bandwidth signals onto the same carrier wavelength, as shown in Fig. 1.3 [19]. In an SCM link, N different signals (S₁ to Sₙ), each having a different RF carrier frequency (f₁ to fₙ), are added into a larger bandwidth signal that modulates a semiconductor laser. At the other end of the fiber, the optical
signal enters the high-speed photodetector (PD), where it is converted back into an electrical signal. At the end of the link, N band pass filters (BPF1 to BPFN) are used to separate the N input signals. Also, it is usual that some of the signals in an SCM link are digital.

Figure 1.3: Schematics of a sub-carrier-multiplexed analog fiber-optic link.

1.2 Optical Transmitters

As mentioned above, optical transmitters used in both digital and analog fiber-optic links are based on either direct or external modulation of the light coming out of a semiconductor laser. The performance requirements for these transmitters depend on the application and whether the optical link in question is digital or analog. An overview of the performance requirements for optical transmitters, with an emphasis on external
modulators, is given in [10]; the most important of these requirements are summarized below.

One of the basic requirements for optical transmitters used in most digital links is, again, operation near 1550 nm. In addition, the transmitters are required to operate at high data rates, \( i.e., \) have wide modulation bandwidths. In modern WDM links, data transmission capacities could be further increased by designing the links to have even larger numbers of low bit rate channels. However, such designs are difficult to implement because the optical multiplexing and demultiplexing circuits become very complex for large channel counts. Therefore, wide-modulation-bandwidth transmitters are very important for future high-capacity digital networks. An optical transmitter for digital links is also required to have large signal-to-noise ratio (SNR) and large extinction ratio. For example, an OOK transmitter should introduce as little noise into the system as possible. The device should leak as little light as possible when in its “off” state, and it should put out as much power as possible when in its “on” state. Also, as electronic drives that output more than 3.5 V become very expensive for data rates of 40 Gbps and higher, optical transmitters for the next-generation digital networks must have very low drive voltages. Finally, the last requirement for optical transmitters used in digital links, that will be mentioned here, is low chirp. Both directly modulated lasers and external intensity modulators introduce a certain amount of undesirable phase modulation in addition to the intensity modulation of the lightwave carrier. This effect results in an optical frequency (wavelength) chirp. In
optical waveguides that have nonzero group velocity dispersion, such as the common single-mode fibers used in the low loss 1550 nm spectral region, chirped optical pulses suffer excessive broadening and reduction of their peak powers. This effect limits the bitrate-distance product (BL) in 1550 nm digital links, making them dispersion-limited, rather than loss-limited systems. One way of quantifying chirp in external modulators is using Henry’s alpha parameter ($\alpha_H$) [10], which is defined as the ratio between the change of the real part of the refractive index ($\delta n$) and the imaginary part of the refractive index ($\delta k$) in the optical waveguide of the modulator. An equivalent to $\alpha_H$ in directly modulated lasers is the “linewidth enhancement factor” and is defined in the same way. It can also be shown that

$$\alpha_H = \frac{\delta n}{\delta k} = -2I(t)\frac{\partial \phi(t)}{\partial I(t)}\frac{\partial I(t)}{\partial t},$$

(1.1)

where $\phi(t)$ and $I(t)$ are time-dependent phase and intensity of light exiting the external modulator.

In analog links, low frequency chirp is not such an important requirement for optical transmitters, as analog links are typically shorter than digital links and many of them operate near 1310 nm, where common single-mode fiber has zero group velocity dispersion. Also, small-signal modulation, which is characteristic of analog links, typically introduces less frequency chirp than OOK in digital links. Similar to digital links, many analog links require very fast transmitters that introduce little noise into the
system, and output as much power as possible. Similar to digital transmitters, analog transmitters are required to achieve large changes in the intensity of light upon only small changes in the drive voltage, which is directly related to the so-called small-signal modulation efficiency. Perhaps the greatest difference between analog and digital transmitters is that the response of analog transmitters should be as linear as possible because in analog links data signals are supposed to be transmitted over the fiber link in a faithful manner without significant nonlinear distortions. There are several methods that can be used to compensate, to a certain degree, for nonlinear transmitter response, both in the electrical domain (e.g., using pre-distortion circuitry) and in the optical domain (e.g., cascading two external modulators in a way that their nonlinear responses cancel each other) [17]. Nonetheless, for these schemes to be effective, the transfer function of the transmitter should be as linear as possible. Finally, it is very important for analog transmitters, as well as the digital transmitters, to be affordable, to be insensitive to changes in temperature, and to have long lifetimes.

Having summarized the basic requirements for digital and analog transmitters, a performance comparison between the directly modulated transmitters and externally modulated transmitters will now be presented. The simplest and most economical way to implement an optical transmitter is to directly modulate the current of a semiconductor laser and, thus, modulate the intensity of its output light. Directly modulated lasers have small footprints and low power consumption. However, they have quite limited
frequency responses. The resonance frequencies of distributed feedback (DFB) lasers or vertical-cavity surface-emitting lasers (VCSELs) are typically lower than about 30 GHz [20]. As the modulation frequency is increased toward the resonance frequency, noise and non-linear distortions rapidly increase. In addition, directly modulated lasers generate significantly more chirp than most external modulators do. Although the performance of directly modulated lasers is being continuously improved using innovative methods, such as injection-locking [20], it is a widely accepted opinion that externally modulated lasers will continue to dominate in high-frequency (>20 GHz) links [10]. Furthermore, external modulators are essential for some modulation schemes, such as return-to-zero (RZ) modulation [14]. Unlike non-return-to-zero modulation (NRZ), where optical pulses completely fill the bit interval, in RZ modulation, optical pulses are much narrower than the bit interval. The NRZ modulation scheme was implied in Fig. 1.1. The RZ modulation scheme is illustrated in Fig. 1.4 below. Here, a pulse generator outputs a train of optical pulses that are significantly narrower than the bit interval, which is determined by the NRZ data stream driving the optical modulator. The optical modulator gates the pulses corresponding to “bit 0,” outputting RZ optical data stream. Using a mode-locked laser as a pulse generator is not cost effective, and the pulses are typically generated by another external modulator that modulates the output of a DFB laser [14]. The major disadvantage of RZ modulation is that it requires modulators that have higher bandwidths than those used for NRZ modulation. Nonetheless, RZ modulation offers important
benefits, such as clock transitions for the receiver even when the data contains a long string of 1s [21].

![Diagram of optical pulse train and modulation scheme](image)

**Figure 1.4:** Return-to-zero optical modulation scheme.

As will be explained in more detail in the following discussion on external modulators, unlike directly modulated lasers, some external modulators are capable of modulating the polarization of light. Polarization-modulation schemes have provided great improvements to both the analog and digital links that use them.

1.3 Overview of External Modulators

In this section, an overview of most common external modulation technologies is presented. First, attention is paid to the technologies that use the linear electro-optic effect in crystals and do not need any quantum wells for optical modulation. Subsequently, the main limitations of these technologies are discussed, giving a
motivation for modulators based on quantum well structures, particularly those based on coupled quantum well structures, as they are the main focus of this thesis.

1.3.1 Linear Electro-Optic Effect in Semiconductors

In GaAs and other crystals having the zincblende structure (e.g., InP), the change in the refractive index of the bulk crystal upon the application of the electric field ($F$) (after relatively simple tensor mathematics) can be shown to be one of the following three cases depending on the field direction [22]:

Case I: electric field applied in [001] direction

$$ n[001] = n_0 $$
$$ n[1\bar{1}0] = n_0 + \Delta n $$
$$ n[110] = n_0 - \Delta n $$

Case II: electric field applied in [110] direction

$$ n[1\bar{1}0] = n_0 $$
$$ n[\bar{1}10] = n_0 + \Delta n $$
$$ n[11\sqrt{2}] = n_0 - \Delta n $$

Case III: electric field applied in [111] direction

$$ n[1\bar{1}0] = n_0 + \frac{\Delta n}{\sqrt{3}} $$
$$ n[1\bar{1}2] = n_0 + \frac{\Delta n}{\sqrt{3}} $$
$$ n[111] = n_0 - \frac{2\Delta n}{\sqrt{3}} $$
In all of three cases, \( n_0 \) stands for the refractive index of the unperturbed, isotropic crystal, and

\[
\Delta n = \frac{n_0^3}{2} r_{41} F ,
\]

(1.5)

where \( r_{41} \) (negative constant) is the electro-optic coefficient of the crystal. However, because [111]-cut substrates and electric fields in [111] direction are not very common, the first two cases (Case I and Case II) are typically used for electro-optic modulators, resulting in three different modulation schemes: polarization modulation, intensity modulation (using, for example, Mach–Zehnder interferometer), and mode conversion.

### 1.3.2 Semiconductor Polarization Modulators

A GaAs polarization modulator is shown in Fig. 1.5(a). Several micrometers of an Al\(_{x}\)Ga\(_{1-x}\)As epitaxial layer are first grown on top of (001) GaAs. Typically, in order to provide the vertical confinement of light, during the growth of the Al\(_{x}\)Ga\(_{1-x}\)As epitaxial layer, the Al mole fraction, \( x \), is decreased in the region where the waveguide core is intended to be because the refractive index of the core needs to be higher than that of the cladding, and the refractive index of Al\(_{x}\)Ga\(_{1-x}\)As increases as \( x \) is decreased. When the top cladding layer is grown, \( x \) is increased to the same value it was for the bottom cladding layer. In order to provide the horizontal confinement of light, the AlGaAs is then etched to obtain a narrow, about 3 \( \mu \)m wide, optical single-mode ridge waveguide.
parallel to the [110] direction. Once the optical waveguide has been fabricated, electrodes, which are about 1 \( \mu \)m thick and 100 \( \mu \)m wide, are formed, and the sample is cleaved along (110) plane in order to get smooth input and output facets of the waveguide. As it is only the vertical component of the applied electrical field that is utilized for the polarization modulation scheme, one of the electrodes is evaporated directly above the optical waveguide in order to maximize the field “seen” by the light traveling through the waveguide. It is also a common practice to deposit about 0.2 \( \mu \)m of an optical buffer layer on the substrate before the electrodes are formed. This decreases the optical loss in the waveguide due to the free electrons in the metal.
For these particular crystal and field orientations, the refractive index change will be as shown in the Case I: Refractive index in the vertical direction (refractive index "seen" by the transverse-magnetic (TM) polarized light, i.e., the fundamental TM optical mode of the waveguide) will not change upon an application of the electric field, and the refractive index in the horizontal direction (refractive index "seen" by the transverse-electric (TE) polarized light, i.e., the fundamental TE optical mode) will change by a small amount. The change of the refractive index along the direction of the waveguide, [110] direction, is unimportant because there is no appreciable longitudinal component of the optical field. Consequently, if the incident light is polarized at 45° with respect to [001] direction, which can be achieved by passing unpolarized light through a polarizer rotated at the same 45° with respect to [001] direction [see Fig. 1.5(a)], or by aligning highly polarized laser light with the 45° direction, the light couples equal amounts of power into the TE and TM modes, which "see" two different effective refractive indices ($n_{\text{eff}}^{TE}$ and $n_{\text{eff}}^{TM}$, respectively). This is illustrated in Fig. 1.5(b). Here, it is important to note that a plane wave polarized, for example, in the [001] direction and propagating in bulk semiconductor crystal would "see" only the refractive index of the bulk crystal, i.e., $n_0$. This is different from waveguide modes, such as the TM-polarized fundamental mode propagating in an optical waveguide, which will "see" an average refractive index that depends on the waveguide material and geometry as well as surrounding materials, i.e., the effective refractive index for the fundamental TM mode($n_{\text{eff}}^{TM}$).
As the TE and TM modes “see” different effective refractive indices, they will undergo different phase shifts after propagating the length of the waveguide \((L)\), as given in the following two equations:

\[
\phi_{TM} = \frac{\omega}{c} \cdot n_{TM}^\text{eff} \cdot L \tag{1.6}
\]

\[
\phi_{TE}(F) = \frac{\omega}{c} \cdot n_{TE}^\text{eff}(F) \cdot L, \tag{1.7}
\]

where

\[
n_{TE}^\text{eff}(F) = n_{TE}^\text{eff}(F = 0) + \Delta n_{TE}^\text{eff} \tag{1.8}
\]

and

\[
\Delta n_{TE}^\text{eff}(F) = \frac{(n_{TE}^\text{eff}(F = 0))^3}{2} \cdot r_{41} \cdot F. \tag{1.9}
\]

Also, here, \(\omega\) is the frequency, and \(c\) is the speed of the light. The magnitude of \(r_{41}\) (1.4 \(\times 10^{-12}\) m/V for wavelength near 1550 nm) is very nearly the same for GaAs and AlGaAs of the waveguide. The phase shift of the TM mode is just a passive phase shift, and it is not affected at all by the presence of the electrical field. The TE mode, however, in addition to the passive phase shift, experiences a phase shift proportional to the electric field. The phase difference between the two components at the output of the waveguide is often called “phase retardation.” It can be easily shown that for a phase retardation of 180°, the polarization modulator can switch polarization of light between two orthogonal states using simple phase modulation of the fundamental TE mode [23].
If the waveguide was designed in such a way that \( n_{\text{eff}}^{\text{TE}}(F = 0) \) and \( n_{\text{eff}}^{\text{TM}} \) had the same magnitudes, and if no voltage (electric field) was applied, the TE and TM modes would undergo the same passive phase shifts. There would be no phase difference between them at the output of the device, where they would combine to form light polarized at the same angle as the incident light. If a polarizer is placed at the output of the device (such polarizer is often called the analyzer) and rotated 90° relative to the polarization of the incident light, as shown in Fig. 1.5(a), no light will go through the analyzer. However, if enough voltage is applied \( (V_\pi) \), the phase difference between the two modes at the output of the waveguide will be 180°, and this means that the polarization of the incoming light is rotated by 90°, so that all of the light will pass through the analyzer. Therefore, simply by adding the analyzer to a polarization modulator, the device can be used to convert polarization modulation into intensity modulation. The transfer function of the intensity modulator is described by the following expression [23]

\[
\frac{I_{\text{out}}}{I_{\text{in}}} = \sin^2 \left( \frac{\pi V}{2 V_\pi} \right),
\]

where \( I_{\text{in}} \) and \( I_{\text{out}} \) are intensity of light at the input and the output of the waveguide, respectively, \( V \) is the applied voltage, and \( V_\pi \) (half-wave voltage) is the voltage needed to induce 180° of phase retardation between the two modes. The transfer function, which has the same functional form for all intensity modulators based on linear electro-optic effect, is also plotted in Fig. 1.6. If \( n_{\text{eff}}^{\text{TE}}(F = 0) \) is not matched to \( n_{\text{eff}}^{\text{TM}} \), the transfer
function would have an extra phase term in the argument of the sinusoidal, which will move the function left or right on the horizontal axis.

![Graph of intensity modulator transfer function](image)

Figure 1.6: Intensity modulator transfer function.

If used as an intensity modulator for digital applications, this device would switch intensity of light from "off" state \( (V = 0) \) to "on" state \( (V = V_n) \). The transfer function given in Eq. (1.10) does not include the waveguide loss for the two modes. If the waveguide loss was included in Eq. (1.10), which is straightforward to do following the approach given in [23], it would be obvious that the waveguide loss is detrimental to the maximum optical power available from the device, and that differential loss between the two modes is detrimental to the extinction ratio of the device, which is defined as

\[
Extinction Ratio = 10 \log_{10} \left( \frac{I_{out}}{I_{in}} \right). \quad (1.11)
\]

Also, due to the fact that the effective refractive index changes for the two modes are not of the same magnitude and opposite sign, there will be a net phase change during the
operation of the device, and it will suffer from large frequency chirp. This is one of the main reasons why the polarization modulator is not widely used in digital communications.

If used in analog intensity-modulation applications, the device would be biased at $V = V_n / 2$, where the transfer function is most linear, and only small-signal modulation would be applied. Applications of polarization modulation, rather than intensity modulation, will be discussed below following the summary of the other most common polarization and intensity modulators.

### 1.3.3 Semiconductor Mach–Zehnder Modulators

A GaAs Mach–Zehnder intensity modulator is shown in Fig. 1.7. In this case, the incident TE light is split between two different waveguides, which in turn merge into a single output waveguide. The electrodes are designed and positioned in such a way that light traveling in one waveguide "sees" a vertical electric field pointing up, and the light in the other waveguide "sees" the vertical electric field pointing down. The orientation of the crystal is the same as for the polarization converter, so that the refractive index change is that of the Case I.
In the Mach–Zehnder case, however, only TE light is launched into the device, and only the refractive index change in the horizontal direction matters. The refractive index changes in the two waveguides will have the same magnitude but opposite sign because of the opposite polarity of the field applied to each of the branches. If no field is applied to the device, the incident TE light splits into two equal-power components that undergo the same (only passive) phase shifts and add up in phase as the two branches merge into the single output waveguide. This is the “on” state of the modulator. When an electric field is applied to the device, the phase shift in one branch will be -90° and in the other +90°, so that the total phase retardation will be 180°. The two components of light will add up destructively upon merging into the single output waveguide, and the analyzer is
not needed. This is the “off” state of the modulator. This type of a Mach–Zehnder intensity modulator is called a “push-pull” Mach–Zehnder modulator [10], and its transfer function has the same sinusoidal form as shown in Fig. 1.6.

In theory, push-pull Mach–Zehnder modulators introduce no net phase change and do not suffer from the problem of chirp. In practice, it is impossible to fabricate the two branches of the modulator to have the same geometry and provide exactly the same magnitude of the refractive index change, which is required for “zero-chirp” operation. The problem of the two arms not being perfectly symmetric can be solved by driving the push-pull device differentially, *i.e.*, applying different voltages to the two electrodes of the device, which allows for the chirp to be fine-tuned to the desired value. However, if chirp is not an issue at all for a particular application, voltage can be applied to only one arm of the modulator and the intensity modulation would still be possible. When the two arms of the push-pull Mach–Zehnder modulator are not perfectly balanced, they will also have different waveguide losses and optical mode shapes, preventing the light signals from the two branches to cancel completely in the “off” state. Similarly, the splitting ratio of the input Y-splitter is never ideally 50:50. The imbalance between the two arms is the limiting factor for the extinction ratio in push-pull Mach–Zehnder modulators [10].
1.3.4 Semiconductor Mode-Conversion Modulators

An illustration of a mode converter is shown in Fig. 1.8 (a). As can be seen from the figure, the electric field is applied in the horizontal, [110], direction, and the refractive indices in [11\sqrt{2}] and [11\sqrt{2}] directions (oriented ±45° with respect to the horizontal) will change by the same amount, although with opposite signs, corresponding to the Case II [see Fig. 1.8.(b)]. Horizontally polarized incident light (TE mode) can be thought of as being effectively split into the two equal-power "hybrid modes" components polarized along these two directions, as shown is Fig. 1.8(b). If no voltage is applied to the

![Figure 1.8: Semiconductor mode-conversion modulator: (a) device schematics and (b) refractive index change directions (Case II).](image-url)
electrodes, and if the effective refractive indices are the same for TE and TM modes, these two components will add up in phase at the output and combine into the TE mode again. If, however, enough voltage is applied to the electrodes ($V_\pi$), one of the vectors will undergo -90° phase shift and the other one will undergo +90° phase shift. The two components of light will then recombine at the output to form a TM mode. By definition, optical waveguide modes are states of light that do not change, unless somehow perturbed, as they propagate down a longitudinally invariant waveguide. The ability of the device to transfer power from one fundamental mode of the waveguide into another (TE into TM, or vice versa) is the reason the device is called a mode converter, not simply a polarization converter.

It is important to emphasize that complete mode conversion, which means that all power from one mode is transferred into the other, is possible only if the unperturbed (no external field condition) effective refractive indices of the TE and the TM mode are the same. This condition is also called the zero modal birefringence condition. In order to fully understand this, one can use the coupled-mode theory, rather than the simplistic explanation given above [24]. The effective refractive indices are inherently similar in III–V semiconductor optical waveguides. However, in order to achieve the low modal birefringence required for mode conversion, the geometry of the optical waveguide needs to be carefully designed. [4].
Similar to the polarization modulator, the 90° polarization rotation in a mode converter can be turned into intensity modulation simply by adding a cross-polarized analyzer. Its transfer function can be represented by Eq. (1.10) and illustrated by Fig. 1.6. Following the same logic as in the two previous modulation schemes, it is obvious that this is a push-pull device capable of zero-chirp operation. In comparison with the polarization modulator, the mode converter is twice as efficient because the material refractive index changes for two axes, not just one. Also, if the two modes experience different amounts of loss in the waveguide, the extinction ratio could be severely affected. Fortunately, the problem could be easily solved by rotating the input polarizer in order to put more power into the mode that suffers greater loss, matching the powers of the two modes at the output. In Mach–Zehnder modulators, the differential optical loss due to the imbalance of the two arms cannot be compensated so easily after the device has been fabricated.

1.3.5 Lithium Niobate Modulators

Modulators based on the linear electro-optic effect in Lithium Niobate (LiNbO₃) represent the most mature external optical modulator technology used in optical telecommunications. In them, optical waveguides are most often fabricated by diffusing titanium (Ti) into the crystal [10]. After the optical waveguide has been fabricated, its facets are polished, not simply cleaved as in III–V semiconductor modulators. Also, a thin optical buffer layer is often deposited on top of the waveguide (particularly for z-cut
modulators introduced below) to decrease the optical loss due to the metallic electrodes.

Unlike the isotropic III–V semiconductors, LiNbO$_3$ is an anisotropic, uniaxial crystal. Its material refractive index in one direction is different from those in the other two directions. This special direction is called the extraordinary optical axis, and the refractive index corresponding to it is called the extraordinary refractive index ($n_e$). The other two axes are called the ordinary axes, and the refractive indices are called the ordinary refractive indices ($n_o$). When the crystal is used for its electro-optic effect, its extraordinary axis is called z-axis, and the other two axes are called x-axis and y-axis.

Unlike, for example, the III–V semiconductor GaAs crystal that has only one nonzero electro-optic coefficient ($r_{41} = -1.4 \times 10^{-12}$ m/V), LiNbO$_3$ has 4 different nonzero electro-optic coefficients: $r_{33} = 30.8 \times 10^{-12}$, $r_{13} = 8.6 \times 10^{-12}$, $r_{22} = 3.4 \times 10^{-12}$, and $r_{51} = 28.0 \times 10^{-12}$ m/V [10]. The electro-optic effect in LiNbO$_3$ is typically used in three different modulation schemes, as shown in Fig. 1.9.

Upon the application of an electric field in the z direction ($F_z$), z-cut and y-propagating (waveguide is parallel to the y-axis) LiNbO$_3$ crystals will “see” the refractive index in the x direction change from $n_o$ (~2.29) to

$$n_x' = n_o - \frac{n_o^3}{2} r_{13} F_z,$$

(1.12)

and the refractive index in the z direction change from $n_e$ (~2.2) to
as shown in Fig. 1.9(a). Because, \( r_{33} \gg r_{13} \), the phase of the vertical, TM, polarization is much more efficiently modulated than the phase of the horizontal, TE, polarization. This type of refractive index change provides for an efficient TM-polarization phase/frequency modulator, TM-polarization Mach–Zehnder modulator, as well as a polarization converter, because the differential phase change for the TE and TM modes is quite large. The fact that the largest electro-optic coefficient for LiNbO\(_3\), \( r_{33} \), is more than twenty times larger than \( r_{41} \) for GaAs is somewhat deceiving, as it may seem that the refractive index change achievable in LiNbO\(_3\) is more than twenty times larger than the one achievable in GaAs. However, the refractive index change in LiNbO\(_3\) is only 3–4 times larger because it also strongly depends on the material refractive index itself, and the
isotropic material refractive index for GaAs (∼3.4) is considerably larger than either the ordinary or extraordinary index of LiNbO₃.

Fig. 1.9(b) illustrates x-cut, y-propagating LiNbO₃. The refractive indices in the transverse x and z directions change in the same way as for z-cut, y-propagating LiNbO₃, except that here the z-axis and $F_z$ are in the horizontal direction, so that x-cut, y-propagating LiNbO₃ is most appropriately used for TE-polarization phase/frequency/intensity modulation, or again, in polarization modulators.

Although in z-cut, y-propagating LiNbO₃ and x-cut, y-propagating LiNbO₃ efficient polarization modulation is possible, the polarization modulation is not push-pull. In addition, unlike the isotropic III–V semiconductors, y-propagating LiNbO₃ has large material birefringence ($n_o >> n_e$), which, in turn, results in large modal birefringence that cannot be simply overcome with any particular waveguide design. Consequently y-propagating LiNbO₃ polarization modulators suffer from large (10–15 ps) differential group delay (DGD) between the two modes, which is significantly larger than the DGD for GaAs mode converters (<0.5 fs). Such large DGD precludes y-propagating LiNbO₃ polarization modulators from being used in very important polarization-modulation applications [25].
Fig. 1.9(c) shows another typical LiNbO$_3$ modulation scheme. Here, LiNbO$_3$ is x-cut and z-propagating, and the electric field ($F_y$) is applied in the horizontal, y-direction.

Consequently, the field-dependent refractive index in the x-direction,

$$n_x = n_o + \frac{n_o^3}{2} r_{22} F_y,$$

and the field-dependent refractive index in the y-direction,

$$n_y = n_o - \frac{n_o^3}{2} r_{22} F_y,$$

experience same-magnitude, opposite-sign changes from the unperturbed ordinary refractive index. The push-pull, low-modal-birefringence polarization modulation is ideal for certain long-haul applications [25], [26]. Unfortunately, $r_{22}$ is quite a bit smaller than $r_{33}$, and the drive voltages in z-propagating LiNbO$_3$ modulators are larger than those in y-propagating LiNbO$_3$ modulators.

### 1.3.6 Polymer Modulators

Electro-optic polymers are an immature modulator technology [10], [27]. The polymers are synthetic organic materials obtained by embedding active electro-optic polymers, i.e., nonlinear optical chromophores, into a matrix of a standard polymer host, such as PMMA. It is very easy to form multilayer polymer stacks using spin-coating, which makes polymers very easy to integrate with various optoelectronic circuits. Unlike
metallic electrodes on semiconductor epitaxial layers, metallic electrodes can be easily sandwiched between polymer layers. In order to obtain a macroscopic electro-optic effect from the microscopic electro-optic effect that is characteristic of chromophore molecules, the molecules need to be aligned. This is achieved by heating (in the range between 100 and 200 °C) and cooling the polymer in a strong electric field (100–200 V/µm). This process is called polling. The electrodes used to apply the polling field are often removed and replaced by more appropriate, typically faster, microwave electrodes.

After polling, the isotropic electro-optic polymer becomes uniaxial. Its extraordinary axis is aligned with the direction of the field, and its ordinary axis is normal to the direction of the applied field. The extraordinary material refractive index is \( n_e = n + 2\Delta \), and the ordinary material refractive index is \( n_o = n - \Delta \), where \( n \approx 1.6 \) and \( \Delta \approx 0.1 \). If the z axis is aligned with the extraordinary axis, and only electric field in z direction is applied, the refractive index change for electro-optic polymers will be similar to the one for z-cut, y-propagating LiNbO₃, as shown in Fig. 1.9(a), and Eqs. (1.12) and (1.13). \( r_{33} \) is about three times larger than \( r_{13} \), and it could be increased if a greater polling field is applied. Unfortunately, the greater the polling field, the greater the material loss and birefringence. \( r_{33} \) can vary from several pm/V to ~100 pm/V. In electro-optic polymers, due to the low refractive index, \( r_{33} \) needs to be ~80 pm/V in order for the refractive index change of the polymer to be similar to that of LiNbO₃ for the same electric-field change.
Fig. 1.10 illustrates a push-pull Mach–Zehnder polymer modulator. During the polling process, the electric field is applied in opposite directions in two neighboring regions containing the electro-optic polymer, providing for the push-pull effect. The two regions form the cores of the optical waveguides in the two branches of a Mach–Zehnder modulator. The opposite alignment of the molecules (white arrows) with respect to the applied electric field (black arrows) is indicated in the figure. The waveguide cores in the horizontal direction are defined by decreasing the refractive index of the surrounding material (cladding) using either dry etching or photobleaching techniques [10]. Light confinement in the vertical direction is achieved by spin-coating materials with lower refractive indices than that of the core, above and below the waveguide.

1.3.7 Comparison of Linear Electro-Optic Modulators

The preceding sections presented only the basics of some of the best known linear electro-optic modulation technologies. Here, a more detailed performance comparison of
the technologies is given. One of the most important performance requirements for optical modulators is wide electro-optic bandwidth. For example, future WDM links will require optical modulators to operate at data rates of 40 Gbps and higher. The optical modulators that will be used in future WDM links will, therefore, need to have electro-optic bandwidths greater than 30 GHz, depending on the spectral efficiency of the digital signal (ratio of the bit rate to the bandwidth), which depends on the modulation and coding schemes used in the links [21]. In addition, high-frequency operation must be achieved without sacrificing modulator performance, e.g., the RF drive voltage should be less than 3.5 V [10].

Most high-frequency modulators, particularly those intended for operation at 40 Gbps and higher data rates, employ some type of traveling-wave electrodes, rather than lumped electrodes [28]. A lump electrode structure is basically a capacitor, such as shown in Fig. 1.8, connected in parallel with an impedance-matching resistor (typically, a 50 Ω resistor for broadband matching is used). In lumped electrode structures, the electrode length is short compared to the RF wavelength. The bandwidth of a lumped electrode structure is determined by the RC time constant, and the electro-optic bandwidth of the modulator is the smaller of the inverse of the RC time constant or the inverse of the time the light takes to propagate along the length of the capacitor, between its plates. The former is usually more limiting. In order to increase the electro-optic effect and lower the drive voltage, it is desirable to make the electrodes as long as possible, increasing the interaction between
the light and the modulating electric field. However, the capacitance increases with the electrode length, decreasing the bandwidth. As the linear electro-optic effect requires the electrodes of electro-optic modulators to be several centimeters long, traveling-wave electrodes need to be used. Even the short electroabsorption modulators (\( L < 1 \text{ mm} \)), which will be described in more detail in the following section, have shown better performance using traveling-wave electrodes [29].

In traveling-wave electro-optic modulators, the modulating signal is applied to one end of the electrodes, and the other end of the electrodes is terminated with a resistive load. The impedance of both the electrode and the load are matched to the impedance of the source, which is typically 50 \( \Omega \), so the electrode can be considered to be an extension of the transmission line and its bandwidth is not limited by the electrode charging time. Here, the basic idea is that the modulating electric field launched at one end of the electrodes propagates down the traveling-wave electrode at the same speed as the light, which is launched in the same direction in the optical waveguide. If the two speeds are not matched, the light-electric-field interaction will not integrate effectively as the two waves propagate. In semiconductor modulators, the electrical signal travels faster than the optical signal and is relatively easily slowed down by capacitive loading, as illustrated in Fig. 1.11 [4], [30], [31].
The electro-optic 3 dB bandwidth due to the velocity mismatch between the modulating signal and the optical mode is inversely proportional to the electrode length \( L \), as shown in the following equation

\[
    f_{3\,dB} = \frac{\frac{c}{L \left| n_{\text{elec}}^{\text{eff}} - n_{\text{opt}}^{\text{eff}} \right|}}.
\]

(1.16)

where \( n_{\text{elec}}^{\text{eff}} \) and \( n_{\text{opt}}^{\text{eff}} \) are the effective refractive index of the electrode structures and the effective refractive index of the optical mode, respectively, and \( c \) is the speed of light [4]. In LiNbO\(_3\) modulators, unlike in III–V semiconductor modulators, the material refractive index for electromagnetic waves is significantly larger for the microwave/millimeterwave frequencies than it is for optical frequencies. Therefore, the velocity of the electrical signal in the traveling-wave electrode needs to be increased considerably for fine velocity matching, which is challenging to do without increasing the drive voltage [27].
The electro-optic bandwidth of modulators is also limited by the electrode microwave loss, which is usually more dominant than the velocity mismatch effect for very high frequencies. The electro-optic 3dB bandwidth due to electrode loss is inversely proportional to the square of the length of the electrodes, as shown below

$$f_{3db} = \frac{2.54}{(\alpha_0 L)^2},$$

(1.17)

where $\alpha_0$ is a constant dependent on the dimensions and the resistivity of the electrodes, and $L$ is, as before, the length of the electrode [4].

In addition, a very important design constraint for high-performance electro-optic modulators is impedance matching. If the impedance of an electrode is not closely matched to the impedance of the source and/or the termination, the modulator will suffer from large frequency-dependent reflection loss and resonance issues.

The large electro-optic effect in LiNbO$_3$ modulators (again, the effect is 3–4 times larger than that in GaAs) does not necessarily provide for a device that is strikingly shorter and, thus, faster than other electro-optic modulators, because of constraints such as impedance matching, velocity matching, and low drive voltages, as mentioned above. To the contrary, LiNbO$_3$ Mach–Zehnder modulators typically have the largest footprints of all the available modulator technologies, which is perceived as one of their major
disadvantages [10]. Although a LiNbO$_3$ Mach-Zehnder modulator with bandwidth greater than 75 GHz, having 2 cm long electrode, has been demonstrated, the drive voltage for the device was large ($V_n = 5.1$ V) [32]. The length of the electrode had to be extended to 3 cm and its bandwidth consequently lowered to 30 GHz, in order for the modulator, with otherwise the same design, to have a drive voltage of only 3.5 V. Besides their large footprint, bias instability in LiNbO$_3$ Mach-Zehnder modulators is also perceived as one of their major disadvantages. A sudden change of the bias voltage can trigger a slow bias drift with a time constant of several hours to several days. The bias drift is due to slowly moving charge that is either trapped in LiNbO$_3$ and SiO$_2$ buffer layers, or is trapped at their surfaces and interfaces. The charge can be process related or it can be generated during the operation of the device by thermal or optical excitation. To minimize the drift problem, LiNbO$_3$ surfaces should be treated, and, also, the conductivities of the layers should be matched [10]. Nevertheless, due to large investments in LiNbO$_3$, it is still considered the benchmark technology for the linear electro-optic modulators [10]. LiNbO$_3$ optical waveguides exhibit low loss (~0.2 dB/cm), they can handle the largest optical powers (10s to 100s of mW), and they can be designed for very efficient coupling with the standard single-mode fibers (5 dB fiber-to-fiber insertion loss) [27].

In contrast with LiNbO$_3$ modulators, polymer modulators are a very immature technology, which is not yet very popular in the marketplace [10]. The technology has a
major advantage of being inexpensive and easy to integrate with various devices. The small refractive indices of polymers (~1.6) make them well matched to optical fibers (refractive index of silica is ~1.46). Also, the small refractive index and its small change from optical frequencies to microwave frequencies, provides for easy fabrication of 50 Ω traveling-wave electrodes, and excellent microwave-lightwave velocity match. Polymer Mach–Zehnder modulators with bandwidths of over 40 GHz, and drive voltages of about 10 V, have been reported [27]. The optical loss in polymer waveguides is typically ~3 dB/cm and the total, fiber-to-fiber loss is about 10–12 dB. The intense research in the field is continuously improving the properties of electro-optic polymers. One of the major challenges that the technology has to overcome is the instability of the electro-optic chromophores. If the optical power is large enough (~10 mW), the chromophores become excited and misaligned, diminishing the macroscopic electro-optic effect. For example, a 30 % decrease in the electro-optic efficiency has been estimated after a 10⁴ h operation for a device with a 10 μm² optical waveguide cross-sectional area and 10 mW of light power at 1320 nm [27]. The misalignment of the chromophores can also be induced by high-electric-field or thermal excitation. Further improvements to the stability of electro-optic polymers and to room-temperature deposition techniques may make electro-optic polymer modulators into a very desirable technology.

GaAs Mach–Zehnder electro-optic modulators have benefited immensely from the growth and fabrication processes that have been developed for telecommunication lasers
and photodetectors. Being a GaAs technology, they can, potentially, be monolithically integrated with lasers, photodetectors, and other GaAs-based devices. Many devices can be obtained from a 6" GaAs wafer, and their waveguide facets are easily cleaved (LiNbO₃ waveguides must be polished). Their typical chip length of ~3 cm is smaller than that of LiNbO₃ Mach–Zehnder devices, which is ~5 cm [10]. They can also handle large optical powers and their optical waveguide loss is ~1dB/cm, and the total, fiber-to-fiber loss is about 10–15 dB [27]. The GaAs dielectric properties provide for good microwave electrodes, and 40 Gbps devices with drive voltages of about 5 V are commercially available [10].

GaAs polarization converters also benefit from a mature GaAs growth and fabrication process, inheriting many properties that are similar to those of GaAs Mach–Zehnder modulators. Versawave Technology Inc. (formerly JGKB Photonics Inc.) has been a leader in developing ultrahigh-speed mode-conversion modulators [33]. Although still a young technology, Versawave’s mode converters exhibit remarkable properties when packaged as intensity polarization modulators as well as polarization modulators. Versawave’s mode converter, being a push-pull device, inherently has low chirp (±0.1) when packaged as an intensity modulator [34]. It also has the benefit that the chirp can be adjusted simply by rotating the input polarizer and/or the analyzer. Its package size (2–2.5 inches long) is the shortest of all the available linear electro-optic modulators [33]. Compared to GaAs Mach–Zehnder modulators, the mode converter is single-optical-
waveguide device and does not suffer from additional optical losses due to the Y-
splitters. Fiber-to-fiber optical loss is less than 7 dB. Having a bandwidth of ~33 GHz
and drive voltage of 3.5–4 V, the device has a great potential for future 40 Gbps optical
networks [33], [34].

When packaged as a polarization modulator, a mode converter has very similar properties
to the intensity modulator [35]. Due to its low birefringence, it has very low differential
 group delay (10s of 10^{-15}s), which is much smaller than that for y-propagating LiNbO_3
polarization modulators [25], as mentioned in the section on LiNbO_3 modulators. Ever
since it was introduced, Versawave’s polarization modulator has attracted considerable
attention for being a fast device, with many desirable properties, which enable an ever-
increasing number of polarization-modulation applications to be used at ultrahigh speeds
[5]. As explained in [5], Versawave’s polarization modulator was recently used at Bell
Laboratories for a 10^{-2} reduction (i.e., 100 times improvement) in uncorrected bit error
rate of a WDM transmission using in a novel polarization-alternating scheme. Here, the
polarization modulator was used to switch the polarization of alternating pulses in a
return-to-zero differential-phase-shift-keyed (RZ-DPSK) data stream in order to reduce
nonlinear degradation in a communication system, providing for a record-breaking reach.
The same modulator was also used in an experiment at the Naval Research Laboratory,
where, in an analog optical link, polarization modulation provided a 35 dB improvement
in inter-channel crosstalk compared to amplitude modulation. Also, it has been shown
that high speed polarization modulators can be used for scrambling the polarization of a forward pumped Raman amplifier in order to reduce the effect of the pump's polarization dependent gain on the data.

In conclusion, the outstanding performance of the Versawave’s mode converter as an intensity modulator, as well as a polarization modulator, that can be used in an ever-increasing number of applications is very inspiring. If a similar but shorter device could be made, it would enable these important modulation schemes to be used in still faster, future optical networks. For it to be significantly shorter, the device must be based on an effect that is significantly greater than the linear electro-optic effect used in the devices mentioned above. Various quantum well structures have been studied over the years in order to realize large electrorefraction as well as electroabsorption effects in semiconductors, both of which are essential for future electro-optic modulators and related electro-optic devices.

The main focus of the thesis is improving the-state-of-the-art in polarization and intensity modulators. In the thesis, coupled quantum well structures, rather than the more common square quantum well structures, are recognized as the most promising technology to achieve this goal in the foreseeable future. The rest of the Introduction chapter presents insights into the optical processes in square and coupled quantum well structures and their application to electro-optic modulators.
1.4 Multiple Quantum Well Modulators

Multiple quantum well (MQW) modulators are based on an array of identical, uncoupled square quantum wells (SQWs). Typically, 10–20 repetitions of a SQW are placed in the optical waveguide of an MQW modulator in order to enhance the interaction with the optical mode [36], [37]. However, as the SQWs are uncoupled, it is sufficient to focus on the optical processes for only one SQW in order to understand the basic operation of the MQW modulator. Fig. 1.12 illustrates a short-period MQW structure, with only two quantum wells, that has In$_{0.53}$Ga$_{0.47}$As wells and In$_{0.52}$Al$_{0.48}$As barriers. In the left-hand side quantum well, the lowest energy electron wave function ($\Psi_{E1}$) and the second lowest energy electron wave function ($\Psi_{E2}$) are shown in the conduction band and have “L” (for left-hand side) superscripts. Also, the two lowest energy heavy-hole wave functions ($\Psi_{HH1}$ and $\Psi_{HH2}$) and the two lowest energy light-hole wave functions ($\Psi_{LH1}$ and $\Psi_{LH2}$) are shown in the valence band and have the “L” superscripts. The corresponding wave functions in the right-hand side well have “R” superscripts.

The wave functions in Fig. 1.12 are obtained separately for each well, without a possibility of coupling with the corresponding wave functions in the other well, i.e., assuming that the two wells are infinitely spaced. When the SQWs are brought together, as long as they remain sufficiently far apart, the coupling between the wave functions, i.e., their overlap integrals, will remain small. The overlap integral for two 1-dimensional
The quantum wells are In$_{0.53}$Ga$_{0.47}$As, and the barriers are In$_{0.52}$Al$_{0.48}$As.

wave functions $f_A(z)$ and $f_B(z)$ is defined as

$$I_{AB} = \int_{-\infty}^{\infty} f_A(z)f_B(z)dz.$$ (1.18)

As SQWs are brought together, the high energy wave functions start to couple before the low energy wave functions do. It is clearly shown in Fig. 1.12 that $\Psi_{LH2}^L$ and $\Psi_{LH2}^R$ exhibit the deepest penetrations into the middle barrier and, thus, will have the
highest degree of coupling. Consequently, the energies and distributions of the two wave functions will change. However, it is often necessary to keep the barriers as thin as possible in order to increase the number of SQWs in the optical waveguide and increase their interaction with the optical mode. Fortunately, as explained below, it is the lowest energy wave functions (Ψ_{E1}, Ψ_{HH1}, and Ψ_{LH1}), which are more strongly confined to the quantum well layers than the respective second lowest energy wave functions (Ψ_{E2}, Ψ_{HH2}, and Ψ_{LH2}), that dominate the optical processes in MQW modulators, and the barriers are typically as thin as 50 to 100 Å. The characteristic thicknesses for the quantum wells are also typically smaller than 100 Å, depending on the specific application and the MQW modulator design. Also, the choice of material for the quantum wells depends on the specific application and intended wavelength of operation.

1.4.1 Electroabsorption in SQWs

Optical absorption in semiconductor structures of various dimensions (e.g., 1D, 2D, or 3D) strongly depends on the density of states in these structures. This is also true for quantum well structures, which have dimensionality between 2D and 3D [38]. In order for light to excite an electron from a valence-band state into a conduction band state, and become absorbed in the process, it needs to have the energy equal to the energy difference between these two states, assuming that the final state is not already occupied. The energy of light (E) is inversely proportional to its wavelength in vacuum (λ₀), i.e.,
\[ E = h \times c/\lambda_0, \] where \( h \) is Planck's constant and \( c \) is speed of light in vacuum. The two electron states need to be at the same point in space, \( i.e. \), they need to have a significant spatial overlap, and, because light adds negligible momentum to the system, they must have the same value for the wave vector \( k \). Such electron transitions are called direct interband transitions. In addition, the ability of light to induce the direct interband transition between these two states depends on its polarization and on the symmetry of the unit cells corresponding to the states [39], which is referred to as the "polarization selection rule."

Fig. 1.13 illustrates how the lowest energy electron wave function \( (\Psi_{E_1}) \) and either of the lowest energy hole wave functions \( (\Psi_{HH1} \text{ or } \Psi_{LH1}) \) in a SQW react to an electric field applied in the direction normal to the plane of the quantum well [40]. In order to achieve the electroabsorption and the electrorefraction effects that are used in optical modulators, the electric field must be applied in the direction normal to the planes of the quantum well structures regardless whether they are uncoupled SQWs, coupled quantum wells, or some other type of quantum well structure. The effective mass of the heavy holes is much larger than the effective mass of the light holes, and, consequently, the heavy-hole wave functions and the light-hole wave functions have different energies in a quantum well, they experience different degrees of confinement by a quantum well, and they exhibit different degrees of sensitivity to an applied electric field. However, the nature of their
response to an electric field is the same, and the hole wave function in Fig. 1.13 can be used to represent either $\Psi_{HHI}$ or $\Psi_{LHI}$.

![Figure 1.13: Effect of the electric field (E) on the lowest energy electron wave function, $\Psi_{EI}$, and on either of the lowest energy hole wave functions, $\Psi_{LHI}$ or $\Psi_{HHI}$: (a) zero-electric-field case, (b) nonzero-electric-field case [40]. © 1988 IEEE](image)

As shown in Fig. 1.13, upon the application of an electric field, the electron and the hole wave functions will be pulled to opposite sides of the quantum well, where they "see" the lowest potential energies. Their movement to the opposite sides of the quantum well is not surprising considering that electrons and holes have charges of opposite signs. The field, therefore, reduces the overlap integral [Eq. (1.18)] between these two states. In general, when no electric field is applied to a symmetric quantum well, such as those in Figs. 1.12 and 1.13(a), only those electron and hole wave functions corresponding to
states that have the same quantum number will have appreciable overlaps ($\Psi_{e1}$ and $\Psi_{hh1}$, $\Psi_{e1}$ and $\Psi_{lh1}$, $\Psi_{e2}$ and $\Psi_{hh2}$, $\Psi_{e2}$ and $\Psi_{lh2}$, $\Psi_{e3}$ and $\Psi_{hh3}$, $\Psi_{e3}$ and $\Psi_{lh3}$, etc.) [41]. Light-induced transitions between these states are called "allowed" transitions. As the electric field is increased, the nominally "allowed" transitions become less possible and the nominally "forbidden" transitions ($\Psi_{e1}$ and $\Psi_{hh2}$, $\Psi_{e1}$ and $\Psi_{lh2}$, etc.) start to dominate. Such behaviour can be easily proved mathematically, using simple geometrical arguments and the orthogonality of wave functions [41].

Fig. 1.13 illustrates another important effect that the electric field has on these states. As shown in the figure, the electric field reduces the energy separation ($E_a$) between these two states. Conversely, the field increases the corresponding wavelength separation between these two states, and this phenomenon is, therefore, commonly called "red shifting."

Similar to [10], Fig. 1.14 shows a rough sketch of zero-electric-field optical absorption in SQWs corresponding to electron-light-hole transitions. In the literature, optical absorption is represented by the absorption coefficient $\alpha$ (1/cm), which determines the fraction of photons absorbed over a given distance [39]. As mentioned above, the optical absorption is directly related to the density of states. The two steps in Fig. 1.14 are related to the joint density of states [38] for electrons and light holes, assuming that there is no coulombic interaction between them, and assuming that the SQW confines only the two
Figure 1.14: Schematic representation of SQW optical absorption for electron-light-hole transitions.

The lower step starts at the wavelength corresponding to the energy separation between $\Psi_{E1}$ and $\Psi_{LH1}$, and its height is proportional to the overlap integral for these two wave functions. Similarly, the second step starts at the wavelength corresponding to the energy separation between $\Psi_{E2}$ and $\Psi_{LH2}$, and, also, its height is proportional to the overlap integral for these two wave functions. As explained above, when an electric field is applied to the SQW, the edges of these steps will shift on the horizontal axis and their heights will start diminishing, while the heights of the nominally “forbidden” transitions will start appearing.

In order to fully describe optical absorption in SQWs and explain the origin of the two vertical lines in Fig 1.14, the electron and the light-hole states cannot be treated as independent, and the coulombic attraction between them must be included. As light excites an electron from a state in the valence band into an available state in the
conduction band, an oppositely charged light-hole (or heavy hole) is created in the valence band. The coulombic attraction forces the electron to spend more time in the vicinity of the light hole, and the two-particle system resembles that of the hydrogen atom. The more time the electron spends in the vicinity of the light hole, the greater the probability of finding the electron and hole in the same unit cell and, thus, the greater the strength of the optical absorption [38]. This two-particle system is called an exciton.

The vertical line sitting at a higher wavelength corresponds to the lowest energy state of the exciton associated with the $\Psi_{E1-LH1}$ transition (E1-LH1 exciton), while the other line corresponds to the lowest energy state of the exciton associated with the $\Psi_{E2-LH2}$ transition (E2-LH2 exciton). These states are similar to the lowest energy, radially symmetric 1S states of the 2-dimensional hydrogen atom. In this thesis, for the purpose of modeling electroabsorption and electrorefraction, the relative motion of an electron around a hole in the plane of the quantum well will be restricted to radially symmetric 1S orbitals [42]. The energy separation of the 2D 1S exciton state from the edge of the corresponding free-particle density of states step is called the exciton binding energy ($E_B$) [42]. In the literature, $E_B$ is given as a negative energy measured relative to the free-particle density of states step, i.e., the energy separation between the electron and hole states when the coulombic coupling is ignored. This is analogous to the 2D hydrogen atom, where the energies of the bound states are negative and those of the unbound states are positive (the same is true for the 3D hydrogen atom). Also, similar to the 2D
hydrogen atom, there are an infinite number of bound exciton states, where the energy separation between the states becomes progressively smaller for high-energy states. However, these states make smaller contributions to the electroabsorption and electrorefraction effects and are commonly neglected in the numerical modeling of these effects [38], [42], again, as is done in this thesis. It is also worth mentioning that the coulombic force enhances the free-particle density of states in the vicinity of the step edge, increasing the absorption coefficient for the corresponding energies. This is also analogous to the unbound positive-energy hydrogen atom states. Therefore, in the following discussions, these states will be referred to as exciton continuum states.

It has already been mentioned above that the electric field pulls electrons and holes in opposite directions and decreases the absorption due to the continuum. This is also true for the excitonic absorption. As an electric field applied in the direction normal to the quantum well separates an electron and a hole in the same direction, the separation between the two particles also increases in the two directions parallel to the plane of the quantum well. The in-plane increase of the exciton occurs because it is energetically favorable for the two-particle system to be nearly spherical. Stretching an exciton into a "pancake" would imply mixing in some highly non-spherical orbitals that have high energies. Conversely, squeezing the exciton by narrowing the quantum well, for example, makes it smaller in all three dimensions. Therefore, the electric field will separate the electron and hole in an exciton and decrease the time they spend in the vicinity of one
another, dramatically decreasing their probability of being in the same unit cell and, in
turn, decreasing the excitonic absorption coefficient. As the in-plane motion of an
electron around a hole is assumed to be restricted to the radially symmetric 1S orbital, the
application of an electric field implies an increase of the orbital’s radius and a decrease of
$E_B$, which is small compared to the “red shift” of the absorption edge. It is interesting to
note that excitons also contribute to the absorption in bulk, 3D semiconductors, however,
the contribution is much smaller because the exciton in the bulk material is considerably
larger. Also, the potential confinement due to the quantum well prevents the quantum
well excitons from being easily destroyed by the electric field, and the excitonic
absorption features can be observed at electric fields higher than 100 kV/cm, which is a
very useful effect for quantum well optical modulators.

Fig. 1.15 shows the effect that the electric field has on the absorption spectra for a MQW
modulator containing only two 94 Å wide GaAs–AlGaAs SQWs for the polarization of
light that is parallel to the planes of the quantum wells (TE polarization) and for the
polarization of light that is normal to the planes of the quantum wells (TM polarization)
[43]. According to the polarization selection rules for interband transitions in III–V
semiconductors [39], only the light holes contribute to the absorption of TM polarization
(i.e., there is no heavy-hole contribution), and the basic features of the absorption spectra
in Fig. 1.15(b) are similar to those of the absorption spectrum in Fig. 1.14. However, Fig.
1.15(b) shows realistic, experimental absorption spectra where the contributions of the
discrete 1S exciton state and the continuum exciton states are not separate functions (delta function and step-like function, respectively), but rather, they form smooth, continuous curves that arise due to several broadening mechanisms.

Figure 1.15: Experimental absorption spectra of a waveguide modulator containing only 2 GaAs–AlGaAs SQWs (94 Å wide wells) for: (a) TE polarization and (b) TM polarization. The curves (i)–(v) correspond to electric fields of 16, 100, 130, 180, and 220 kV/cm [43].

As will be explained below, the lowest energy transitions dominate in the absorption processes for MQWs, and only the exciton and the beginning of the continuum states
corresponding to the lowest energy $\Psi_{E1} - \Psi_{LH1}$ transition are shown in Fig. 1.15(b). The linewidth function for the broadening evident in the figure is usually well described by a Lorentzian function (for homogeneous broadening mechanisms), a Gaussian function (for inhomogeneous broadening mechanisms), or a convolution of the two (for simultaneous homogeneous and inhomogeneous broadening mechanisms). The energy width of an absorption peak reflects the resonant state of the corresponding exciton. By the uncertainty principle, the longer the lifetime of the exciton, the better defined the energy, and consequently, the corresponding absorption peak will be sharper. The absorption peak will be broadened (or the exciton lifetime will be shortened) by the following five major mechanisms. First, optical phonon scattering efficiently separates an electron from the corresponding hole (homogeneous broadening). Second, the external electric field will pull the electron and hole in opposite directions (homogeneous broadening). This effect is clearly shown in Fig. 1.15 (b). Third, in MQW modulators, any variations in the sizes of the quantum wells will contribute to the total absorption peak broadening, as each distinct quantum well will have its absorption peak at a distinct energy (inhomogeneous broadening). Fourth, if the electric-field varies across the region containing the quantum wells, each quantum well will have a slightly different response (inhomogeneous broadening). Fifth, particles have finite probabilities of tunnelling out of quantum wells, which means that many states close in energy to each bound state are possible (homogeneous broadening).
Considering the points made above, it is simple to understand the basic principle behind electroabsorption modulators. The wavelength of operation is chosen so that the corresponding energy is \(-20-30\) meV below the lowest energy exciton, and the electric field \(F\) is switched from a low value of \(F \approx 0\) kV/cm to \(F \approx 100\) kV/cm. Comparing the curve (i) in Fig. 1.15(b) to, for example, the curve (iv), it is clear that the absorption of TM-polarized light increases from a small value (the “on” state of the electroabsorption modulator) to a much larger value (the “off” state of the electroabsorption modulator). Large “red shifting” of the lowest energy exciton and its persistence for large fields needed to achieve the “red shift,” provide for large extinction ratios in electroabsorption modulators. This phenomenon is called the Quantum-Confined Stark Effect (QCSE) [44].

Most common electroabsorption modulators, however, modulate the TE light. The polarization selection rules [39], state that both the heavy holes and the light holes participate in electroabsorption for the TE polarization, where the contribution of the heavy holes dominates. Fig. 1.15(a) illustrates electroabsorption for TE polarization, which is very similar to that for TM polarization except that the lowest energy exciton peak corresponds to the \(\Psi_{E1}-\Psi_{HH1}\) transition and the second lowest peak corresponds to the \(\Psi_{E1}-\Psi_{LH1}\) transition. The light holes have smaller effective masses than the heavy holes, so that the \(\Psi_{E1}-\Psi_{LH1}\) energy separation is greater than the \(\Psi_{E1}-\Psi_{HH1}\) energy separation.
1.4.2 Electrorefraction in SQWs

Beside the possibility of quite efficient modulation of the optical absorption in SQWs, the refractive indices for the TE and TM polarizations in SQWs also depend on the applied electric field and can be efficiently modulated. The real and imaginary parts of a linear, passive system’s response function are related, and, therefore, the same is also true for the complex refractive index response function, $n + jk$. The absorption coefficient is related to the imaginary part of the complex refractive index by

$$\alpha = \frac{2\omega}{c}k,$$

and where $\omega$ and $c$ are the radian frequency and speed of light, respectively. The radian frequency of light is of course related to its energy by a simple formula $E = h\omega$,

where $h = h/2\pi$ is the reduced Planck’s constant. The refractive index at frequency $\omega$ is a weighted integral of absorption coefficients for all frequencies except for $\omega$, and it can be obtained from the Kramers–Krönig relation [44]

$$n(\omega) - 1 = \frac{c}{\pi} P \int_{0}^{\infty} \frac{\alpha(\Omega) d\Omega}{\Omega^2 - \omega^2}.$$

(1.20)

Here, the symbol $P$ stands for the Cauchy principal value of the integral [10]

$$P \int_{0}^{\infty} = \lim_{\delta \to 0} \left[ \int_{0}^{\omega - \delta} + \int_{\omega + \delta}^{\infty} \right].$$

(1.21)
The Kramers-Krönig relation thus states that electroabsorption is always accompanied by
electrorefraction. However, using the Kramers-Krönig relation in the form given in Eq.
(1.20) is impractical because the equation requires a knowledge of the absorption
coefficients for all frequencies of light. Fortunately, the spectrum of the electric-field-
induced change of the absorption coefficient in SQWs is well localized around the
frequencies corresponding to the lowest energy transitions. Consequently, it is possible to
calculate the magnitude of the electrorefraction close to the lowest energy transitions
using the following equation [44]

\[ \Delta n(\omega) = \frac{c}{\pi} P \int_{\omega_1}^{\omega_2} \frac{\Delta \alpha(\Omega) d\Omega}{\Omega^2 - \omega^2}, \]  

(1.22)

where \( \omega_1 \) and \( \omega_2 \) are the lower and upper frequency limits confining the localized change
of the absorption coefficient.

Fig. 1.16 illustrates the application of the Kramers-Krönig relation, given in Eq. (1.22),
for calculating the refractive index change spectra \( \Delta n \) from the simulated absorption
coefficient change spectra \( \Delta \alpha \) in a GaAs-AlGaAs SQW for TE polarization around
850 nm [45]. Here, the electric field is switched from 0 to 25 kV/cm, and the figure
clearly shows a positive change in \( \Delta \alpha \) for wavelengths longer than the wavelength
corresponding to the \( \Psi_{E1} - \Psi_{HH1} \) transition (labeled as ehh11 in the figure). The
electroabsorption is similar to that in Fig. 1.15 (a). Fig. 1.16 shows that \( \Delta n \) reaches a
maximum or a minimum close to the wavelength where \( \Delta \alpha \) changes sign, and vice versa.
Figure 1.16: Simulated TE absorption change (Δα) and refractive index change (Δn) in a GaAs-AlGaAs SQW for a field change from 0 to 25kV/cm [45].

This behavior is expected because Δα and Δn are actually a Hilbert-transform pair [46].

For the wavelengths just above the WEI-WHH transition, it is clear that there is a nonzero change in the refractive index. The refractive index change is quite large, and it causes electroabsorption modulators to have significant chirp [10]. Although not clearly visible in Fig. 1.16, Δα decreases exponentially for energies below the lowest energy exciton peak, changing much more rapidly than Δn, which exhibits approximately a quadratic decrease for these energies [44]. Therefore, if the amount of detuning from the exciton peak is ~60–80 meV, rather than ~20–30 meV that is typical for electroabsorption modulators, Δn will still be appreciable although Δα and α will be small. This is the basic idea behind the use of SQWs for electrorefraction modulators.
1.4.3 Electroabsorption vs. Electrorefraction MQW Modulators

For electrorefraction (ER) MQW modulators, SQWs are commonly placed in the waveguide of a Mach–Zehnder interferometer in order to convert the refractive index modulation into intensity modulation. This is different from electroabsorption (EA) modulators, where the intensity of light is modulated in a single, straight waveguide by simply modulating the absorption coefficient in the MQW region. TE light is typically modulated in both ER and EA modulators. Also, both ER and EA modulators are typically implemented in a p-i-n diode configuration, as shown in Fig. 1.17. The p-i-n diode configuration is used for providing an electric field that is

![Diagram of InGaAs-InAlAs p-i-n diode Mach–Zehnder modulator.](image)

Figure 1.17: InGaAs–InAlAs p-i-n diode Mach–Zehnder modulator.
normal to the planes of quantum wells, and for increasing the overlap between the
electric field and the thin (<0.5 μm) MQW region. The average refractive index of the
MQW region is higher than that of the surrounding semiconductor for either polarization
and provides for confinement of light in the vertical direction. However, although it can
be quite short, the p-i-n diode structure is not inherently fast, and there has been
considerable research dedicated to designing fast MQW modulators to fully realize their
potential for high-frequency operation [47], [48].

One of the most attractive properties of EA MQW modulators is their small size. They
are typically 80–300 μm long [10]. Such a small size provides for high yields per wafer,
and, therefore, a low cost of fabrication. Similar to ER MQW modulators, the choice of
the substrate and the material for the quantum well structures greatly affects the
wavelength of operation of these devices. The large band gap in GaAs constrains GaAs /
Al_xGa_{1-x}As quantum well structures on GaAs substrates to be used at wavelengths close
to 850 nm. Quantum well structures on InP substrates are used at telecommunication
wavelengths. There are two main material technologies grown on InP. These are the
In_{1-x1}Ga_{x1}As_{y1}P_{1-y1} / In_{1-x2}Ga_{x2}As_{y2}P_{1-y2} and In_{x1}Ga_{y1}Al_{1-x1-y1}As / In_{x2}Ga_{y2}Al_{1-x2-y2}As
material systems. The first material technology typically consists of In_{0.53}Ga_{0.47}As (x1 =
0.47 and y1 = 1) quantum wells lattice-matched to InP (x2 = 0 and y2 = 0) barriers and
InP substrate. The second material technology typically consists of In_{0.53}Ga_{0.47}As (x1 =
0.53 and y1 = 0.47) quantum wells lattice-matched to In_{0.52}Al_{0.48}As (x2 = 0.52 and
y2 = 0) barriers and, also, to the InP substrate. The composition of the material used for the quantum wells and barriers is chosen depending on the desired potential energies for these layers, which, in turn, determine the energies of the bound states and the wavelength of operation. As will be shown in more detail below, the compositions of the epitaxial layers can also be chosen to introduce strain in the quantum well structures and to manipulate the relative magnitude of the TE and TM polarization responses. Tensile strain has been used in many EA modulators in order to make them polarization-insensitive [10]. The In$_{x_1}$Ga$_{y_1}$Al$_{1-x_1-y_1}$As / In$_{x_2}$Ga$_{y_2}$Al$_{1-x_2-y_2}$As material system has proven to be very beneficial for EA modulators because it has a very small valence band discontinuity ratio. The valence band discontinuity ratio is defined as the ratio of the band-edge discontinuity for the valence band ($\Delta E_v$) to the band-edge discontinuity for the conduction band ($\Delta E_c$), i.e., $\Delta E_v / \Delta E_c$. For the In$_{x_1}$Ga$_{y_1}$Al$_{1-x_1-y_1}$As / In$_{x_2}$Ga$_{y_2}$Al$_{1-x_2-y_2}$As material system, $\Delta E_v / \Delta E_c \approx 30/70 \%$, which is considerably smaller than the valence band discontinuity ratio for the In$_{1-x_1}$Ga$_{x_1}$As$_{1-y_1}$P$_{y_1} /$ In$_{1-x_2}$Ga$_{x_2}$As$_{2-y_2}$P$_{y_2}$ material system ($\Delta E_v / \Delta E_c \approx 60/40 \%$) [49], [50]. Consequently, due to the small valence band discontinuity ratio, the quantum wells in the valence band are quite shallow and give the heavy holes a good chance of tunneling out of the MQW structure. Due to their large effective masses, the heavy holes tend to be very strongly confined to the quantum wells, and their accumulation due to high input optical powers screens the applied electric field and saturates the electroabsorption effect. Typically, the maximum input optical power
that can be launched into the waveguide of a MQW EA modulator is between 10 and 20 mW [10].

The large absorption in the “off” state of EA modulators also creates considerable current, which is detrimental to the operation of the high-frequency electrodes. Still, 40 Gbps devices with drive voltages lower than 3 V have been demonstrated [27]. Of all the modulator technologies, EA modulators for 40 Gbps links have the lowest drive voltages. However, for long-haul applications, EA modulators are not the strongest candidates because they have the largest chirp. The chirp parameter, \(a_h\), for EA modulators can be greater than 2 [10]. Although, the EA modulators have large inherent optical losses in the “on” state (15–20 dB/mm) [27], they are very short devices and their total fiber-to-fiber loss can be made lower than 10 dB (typically between 6 and 8 dB) using additional optics to match the small, highly elliptical mode of the EA modulator to the large, round mode of standard single-mode fiber [51]. On the other hand, the large inherent optical loss prevents the length of the EA modulator from being significantly increased for an efficient use of traveling-wave electrodes, and EA modulators have largely been used in lumped-electrode configurations. Also, for the traveling-wave electrode configurations, EA modulators tend to have low impedances (20–30 \(\Omega\)). Of course, being very short, they do not suffer from the microwave-lightwave velocity mismatch. The footprint and cost of packaged EA modulators can be further reduced by integrating them with DFB lasers [10]. Lastly, as they are operated very close to the semiconductor band edge, EA
modulators tend to be very sensitive to the temperature and wavelength of operation. Depending on the specific design and optimization of the EA modulator, its properties can change significantly across the C-band [27], [51], [52]. This is unlike the mode converter, as well as other linear electro-optic modulators, which operate very far from the band edge and have flat wavelength responses over the combined C and L bands [35].

As mentioned above, the wavelength of operation for ER MQW modulators is more detuned from the lowest energy exciton than that for EA MQW modulators. Consequently, they have smaller optical loss in the active region than EA modulators. However, because they require Y-splitters, the ER Mach–Zehnder modulators have considerably larger footprints and tend to have similar or even greater fiber-to-fiber optical loss than EA modulators. For example, the active region of a 10 Gbps lumped-electrode Mach–Zehnder modulator (InGaAsP wells and InP barriers) in [53] is only 600 μm long, whereas its total length including the Y-splitters and tapered-waveguide spot-size converters is 3 mm. The fiber-to-fiber loss for this device is ~6 dB. Having smaller absorption in the active region than the EA MQW modulators, ER MQW modulators have larger optical saturation powers. Similar to other Mach–Zehnder modulators, ER MQW modulators can be driven differentially and have small and adjustable chirp. Also, the imbalance between the two arms typically restricts their extinction ratio to about 15 dB (for a drive voltage of ~4V) [53], whereas ~20 dB extinction ratio is not typical for EA modulators [27]. As ER modulators absorb much less optical power than EA
modulators, they exhibit lower temperature sensitivity due to heating effects. The optically generated currents, therefore, interfere less with the operation of fast electrodes [27].

Although the development of high-frequency electrodes for EA and ER modulators is an active area of research, modern ER MQW modulators are mostly lumped-electrode p-i-n devices limited to 10 Gbps applications [10]. Recently, in an on-wafer experiment, an ER MQW modulator having travelling-wave p-i-n electrodes and a modulation bandwidth of 28 GHz has been demonstrated [54]. The drive voltage of this device was about 3 V, and its extinction ratio and fiber-to-fiber loss were >14 dB and ~9 dB, respectively. Also, recent modelling of ER MQW modulators having travelling-wave p-i-n electrodes has shown that modulation bandwidths exceeding 40 GHz could be achieved, although the drive voltages would be larger than 4 V and additional optical loss due to the electrode configuration would be inevitable [48]. The p-doped region in p-i-n devices introduces significant optical loss and microwave loss. The microwave loss is the main bandwidth-limiting factor of these p-i-n devices. The bandwidth could be improved with better electrode designs, which require larger thicknesses of the intrinsic regions containing the quantum wells and, therefore, provide lower electric fields to the quantum wells. These devices are likely to have Schottky-contact coplanar or microstrip electrodes [55], [56], [57]. Therefore, improving the ER effect of quantum well structures is an important requirement for future ER modulators. ER modulators based on coupled quantum wells,
rather than SQWs, are capable of providing this important benefit. The remainder of this thesis is dedicated to provide a background for the operation of coupled quantum well modulators (Section 1.5) and to provide the convincing arguments that the coupled quantum well modulators developed in this thesis will play an important role in future optical links (Chapters 2–7).

1.5 Coupled Quantum Well Structures

Coupled quantum well (CQW) structures consist of multiple quantum wells that are separated by thin barriers, which permit strong coupling between the states of the wells. In this thesis, we will be looking at CQW structures containing only two quantum wells separated by a thin barrier. The coupling creates new states, and these states exhibit electric-field dependences that are qualitatively different from those of the states in SQWs. CQW structures offer refractive index changes that have similar magnitudes to those typically obtainable in SQWs. The magnitude of the electric-field-induced refractive index change in SQWs is $\Delta n \approx 10^{-3}$ for 100 kV/cm change in the electric field [58]. In CQW structures, however, similar changes in the refractive index can be obtained for ~20 kV/cm change in the electric field, which is a significant improvement. Unlike in SQWs, in CQW structures, the electroabsorption is based on the modulation of the absorption strength associated with the exciton peaks, rather than on their “red shifting.” As CQW structures are the main focus of this thesis, the electroabsorption and
electrorefraction in these structures will be discussed in detail. However, a brief
description of the numerical models used to simulate electroabsorption and
electrorefraction in these structures will be given first.

1.5.1 Modeling of CQW Structures

In this section, the model used for simulating electroabsorption and electrorefraction in
the CQW structures studied in the thesis is described. This model is commonly used for
simulation of CQW structures as well as SQWs [38], [42], [60]. In the model, the exction
equation is used within the effective-mass, envelope-function approximation, and it is
solved using the variational method. The effective mass exciton equation can be written
as

\[
\left( H_e - H_h + E_g - \frac{e^2}{4\pi \varepsilon_s |\vec{r}_e - \vec{r}_h|} \right) \Phi(\vec{r}_e, \vec{r}_h) = E \Phi(\vec{r}_e, \vec{r}_h),
\]

(1.23)

where

\[
H_e = -\frac{\hbar^2}{2m_e} \nabla_e^2 + V_e(z_e)
\]

(1.24)

and

\[
-H_h = -\frac{\hbar^2}{2m_h} \nabla_h^2 + V_h(z_h)
\]

(1.25)
are the electron Hamiltonian and the hole Hamiltonian, respectively. Here, $m^*_e$ and $m^*_h$
are the effective masses for electrons and either light or heavy holes. It is assumed that
the electric field is applied in the $z$ direction and its effect is included in the potential
energy for both electrons and holes ($V_e$ and $V_h$, respectively). The third term on the left-
hand side of Eq. (1.23) is the band gap energy, and the fourth term is the Coulomb
potential energy, where $e$ is the elementary charge, and $\varepsilon_s$ is the permittivity of the
quantum well material. The coulombic interaction in the above equation couples the
electron and hole coordinates ($\vec{r}_e$ and $\vec{r}_h$, respectively) in all three dimensions. If it were
not for this coupling, the two-particle wave function in Eq. (1.23) would be a simple
product of the electron and hole wave functions and the equation would be separable.
Neglecting the quantum well potential ($V_e$ and $V_h$) in Eq. (1.23) would reduce it to the
well-known hydrogen atom equation [61]. Similar to the hydrogen atom problem, Eq.
(1.23) is more easily solved when recast in the center-of-mass coordinates in the plane of
the quantum wells

$$\vec{R}_t = Xx + Yy = \frac{m^*_e \vec{\rho}_e + m^*_h \vec{\rho}_h}{M} \quad (1.26)$$

and the difference coordinates in the plane of the quantum wells

$$\vec{\rho} = x\hat{x} + y\hat{y} = \vec{\rho}_e - \vec{\rho}_h \quad (1.27)$$

where

$$M = m^*_e + m^*_h \quad (1.28)$$
is the total mass corresponding the electron-hole system. Performing the transformation, and defining the reduced mass of the electron-hole system as

\[
\frac{1}{m_e} = \frac{1}{m_e^*} + \frac{1}{m_h^*},
\]

make Eq. (1.23) become

\[
\left[ -\frac{\hbar^2}{2M} \vec{\nabla}^2_{\vec{r_e}} - \frac{\hbar^2}{2m_e} \vec{\nabla}^2_{\vec{r_e}} + H(z_e) - H(z_h) - \frac{e^2}{4\pi\epsilon |\vec{r_e} - \vec{r_h}|} - (E - E_e) \right] \Phi(\vec{r_e}, \vec{r_h}) = 0, (1.30)
\]

where

\[
H(z_e) = -\frac{\hbar^2}{2m_e^*} \frac{d^2}{dz_e^2} + V_e(z_e)
\]

and

\[
-H(z_h) = -\frac{\hbar^2}{2m_h^*} \frac{d^2}{dz_h^2} + V_h(z_h)
\]

are the usual 1-dimensional electron Hamiltonian and the 1-dimensional hole Hamiltonian, respectively, from which the energies and 1-dimensional wave functions are readily obtained by solving

\[
H(z_e) f_n(z_e) = E_{en} f_n(z_e)
\]

and

\[
H(z_h) g_m(z_h) = E_{hm} g_m(z_h),
\]

using the transfer matrix method [62].
The first term in Eq. (1.30) is the only term describing the center of mass of the system, which can be regarded as a freely moving particle of mass $M$ and momentum

$$\vec{K}_e = \vec{k}_{e} + \vec{k}_{h}, \quad (1.35)$$

which is negligible for direct interband transitions. The wave function can, therefore, be written as

$$\Phi(\vec{r}_e, \vec{r}_h) = \frac{e^{i(\vec{K}_e \cdot \vec{r}_e)}}{\sqrt{A}} F(\vec{p}, z_e, z_h). \quad (1.36)$$

Using the completeness property of the free-electron and free-hole wave functions, the exciton envelope function can be written as

$$F(\vec{p}, z_e, z_h) = \sum_n \sum_m \phi_{nm}(\vec{p}) f_n(z_e) g_m(z_h). \quad (1.37)$$

After some further manipulations of the equation, it can be shown that it satisfies

$$H_B \phi_{nm}(\vec{p}) = E_B \phi_{nm}(\vec{p}), \quad (1.38)$$

where

$$H_B = \left( -\frac{\hbar^2}{2m_r} \nabla^2 + V_{nm}(\vec{\rho}) \right) \quad (1.39)$$

and

$$V_{nm}(\vec{\rho}) = \int dz_e |f_n(z_e)|^2 \int dz_h |g_m(z_h)|^2 \frac{e^2}{4\pi \epsilon_s \sqrt{\rho^2 + |z_e - z_h|^2}}. \quad (1.40)$$

Eq. (1.40) is a simpler version of a more general equation [38] and does not allow distinct subbands in the conduction band and distinct subbands in the valence band to be coupled by the coulombic interaction. In Eq. (1.38),
\[ E_B = E - \left( E_g + E_{en} - E_{hm} \right) \]  
\[ (1.41) \]

is the exciton binding energy, which is the negative quantity that was already mentioned in the discussion of electroabsorption in SQWs.

In order to obtain \( E_B \) and the wave function from Eq. (1.38), an additional approximation is made. It is assumed that the relative motion of an electron around a hole in the plane of the quantum well is restricted to the lowest energy 1S orbital, which is a reasonable assumption considering that the higher energy states make smaller contributions to the absorption coefficient, as mentioned in the discussion of electroabsorption in SQWs. The 1S state is radially symmetric in the plane of the quantum well structure

\[ \phi_{nm}(\hat{r}) = \frac{2}{\sqrt{\pi \lambda}} e^{\frac{r}{\lambda}} \],  
\[ (1.42) \]

and it has an effective radius \( \lambda \). This radius is found, and the problem is solved, using the variational method. In this method, the binding energy

\[ E_B(\lambda) = \frac{\langle \phi | H | \phi \rangle}{\langle \phi | \phi \rangle} \]  
\[ (1.43) \]

as a function of the in-plane radius as an adjustable parameter is minimized. The in-plane extension of the exciton is comparable to the length of the quantum well structure in the \( z \) direction.

In [38], it is shown how \( E_B \) can be analytically obtained from the variational method for a simple case in which no coulombic coupling of distinct subband states is allowed.
However, this minimization procedure needs to be done numerically if the coulombic coupling of distinct subband states is allowed. For example, in CQW structures, the energy separation between the two lowest energy electron wave functions, $f_1(z_e)$ and $f_2(z_e)$, and the energy separation between the two lowest energy hole wave functions, $g_1(z_e)$ and $g_2(z_e)$, can be on the order of $E_B (<10 \text{ meV})$. In such a case, the coulombic coupling of these states cannot be neglected, and the variational wave function becomes

$$F(\bar{\rho}, z_e, z_h) = \left[ a f_1(z_e) + \sqrt{1-a^2} f_2(z_e) \right] \left[ b g_1(z_h) + \sqrt{1-b^2} g_2(z_h) \right] \frac{2}{\sqrt{\pi}} \frac{1}{\lambda} e^{-\frac{\bar{\rho}^2}{\lambda}}, \quad (1.44)$$

as explained in [63]. In this case, $\lambda$, $a$, and $b$ have to be varied independently in order to find $E_B$ for the 1S excitons. As will be shown below, $f_1(z_e)$ and $f_2(z_e)$ or $g_1(z_e)$ and $g_2(z_e)$ are confined to opposite wells of a CQW structure and will switch wells when the applied electric field reaches a certain value, which is called the resonant electric field, $F_R$. One of the main effects of the coupling is to increase $F_R$ by several kV/cm.

The absorption spectra consist of the discrete and continuum exciton state contributions corresponding to both the electron-heavy-hole transitions and the electron-light-hole transitions [38]. The discrete exciton states contribution to the absorption coefficient is given as

$$\alpha_D (h\omega) = C_0 \frac{2}{L_{qw}} |\phi_{en} (\bar{\rho} = 0)|^2 |I_{nm}|^2 (\vec{e} \cdot \vec{p}_{en})^2 B(E - h\omega), \quad (1.45)$$
where a transition between an \( n \) electron state and an \( m \) hole state (light-hole or heavy-hole state) is considered. In CQW structures, it is typically sufficient to consider only the two lowest energy electron, heavy-hole, and light-hole states, and the absorption coefficients corresponding to the transitions between these conduction-band and valence-band states are simply added together. The first term in Eq. (1.45),

\[
C_0 = \frac{\pi e^2}{n_r c \varepsilon_0 \omega m_0^2},
\]  

depends on some of the already defined material parameters and fundamental constants, as well as the refractive index of the quantum well material \( n_r \), the free-space permittivity \( \varepsilon_0 \), and the free electron mass \( m_0 \). The second term in Eq. (1.45) is inversely proportional to \( L_{qw} \), which is the length of one period of the quantum well structure. The third term is the in-plane exciton envelope function of Eq. (1.42) evaluated for zero relative displacement between the electron and the hole, which is proportional to the probability of finding the electron and the hole in the same unit cell. The fourth term is the overlap integral between the 1-dimensional electron and hole wave functions, as defined in Eq. (1.18). The fifth term is determined by the polarization selection rules, given below. The vector \( \hat{e} \) is the unit vector describing the polarization of light, and the vector

\[
\bar{p}_c = \langle u_c | \bar{p} | u_c \rangle,
\]  

(1.47)
which is called the momentum matrix element. Here, $\vec{p}$ is the momentum operator and

$u_c$ and $u_v$ are the conduction-band and valence-band unit-cell wave functions, respectively. For TE polarization ($\hat{e} = \hat{x}$ or $\hat{e} = \hat{y}$),

$$|\hat{e} \cdot \vec{p}_{cv}|^2 = M_b^2 \begin{cases} \frac{3}{2} & \text{heavy – hole exciton} \\ \frac{1}{2} & \text{light – hole exciton} \end{cases},$$

and for TM polarization ($\hat{e} = \hat{z}$),

$$|\hat{e} \cdot \vec{p}_{cv}|^2 = M_b^2 \begin{cases} 0 & \text{heavy – hole exciton} \\ \frac{2}{2} & \text{light – hole exciton} \end{cases},$$

where

$$M_b^2 = \frac{m_0^2 E_g (E_g + \Delta)}{6m^* (E_g + 2\Delta/3)}$$

is the bulk matrix element (squared). In Eq. (1.50), $\Delta$ is the spin-orbit splitting energy. Eqs. (1.48) and (1.49) state, as was already mentioned, that the electron-heavy-hole transitions do not contribute to absorption for TM polarization, and they dominate the absorption for TE polarization. Finally, the last term in Eq. (1.45) is the exciton broadening function, which is represented by the Lorentzian function

$$B(E - h\omega) = \frac{\gamma}{\pi [(E - h\omega)^2 + \gamma^2]}$$

for homogeneous broadening mechanisms and by the Gaussian function

$$B(E - h\omega) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(E - h\omega)^2}{2\sigma^2}}$$
for inhomogeneous broadening mechanisms [10]. In Eq. (1.51), \( \gamma \) is the half-width-at-half-maximum (HWHM). In Eq. (1.52), the HWHM corresponds to \(-1.175\sigma\). In both of these functions \( E \) stands for the total exciton energy, as given in Eq. (1.41). In reality, the broadening function is a convolution of the broadening functions corresponding to each of the broadening mechanisms that are relevant in a specific device. In this thesis, a Lorentzian broadening function that has \( \gamma \approx 6 \) meV is used. The semi-empirical formula used to obtain this value is given in [64]. It is also stated in [64], and confirmed by many simulations in this thesis, that the choice of the broadening function for CQW modulators has no significant effect on the electrorefraction process in these devices.

In the formula for the continuum states contribution to the absorption coefficient

\[
\alpha_c(\hbar \omega) = C_0 \frac{\hbar^2}{m_c \hbar^2 \lambda_{\text{L}}^2} \left| f_{nm} \right|^2 \int_0^\infty dE \, M(E, \omega) S(E) B(E - \hbar \omega),
\]

some of the terms that appear in Eq. (1.45) can be recognized. However, because the exciton states form a continuum here, Eq. (1.53) is an integral with respect to the transverse energy

\[
E_r = \frac{\hbar^2 k^2}{2m},
\]

of the electron-hole two-body system. Also, the momentum matrix element in Eq. (1.53) is different from that in Eq. (1.45) because the momentum matrix element in Eq. (1.45) is approximated with \( k_r = 0 \), which is a commonly used approximation. In Eq. (1.53), the
momentum matrix element in the integral depends on $E$, and for TE polarization becomes

\begin{equation}
M(E_e) = \begin{cases} 
\frac{3}{4} (1 + \cos^2 \theta_{nm}) & \text{heavy - hole exciton} \\
\frac{1}{4} (5 - 3\cos^2 \theta_{nm}) & \text{light - hole exciton}
\end{cases}
\end{equation}

(1.55)

while for TM polarization, it becomes

\begin{equation}
M(E_e) = \begin{cases} 
0 & \text{heavy - hole exciton} \\
\frac{1}{2} (1 + 3\cos^2 \theta_{nm}) & \text{light - hole exciton}
\end{cases}
\end{equation}

(1.56)

In these two equations,

\begin{equation}
\cos^2 \theta_{nm} = \frac{E_{en} + |E_{hm}|}{E_{en} + |E_{hm}| + E_r}.
\end{equation}

(1.57)

Also, in Eq. (1.53)

\begin{equation}
S(E_e) = \frac{s_0}{1 + e^{-\frac{2\pi}{\sqrt{E_e/R_r}}}},
\end{equation}

(1.58)

which is the Sommerfeld enhancement factor for a 2D exciton. The Sommerfeld enhancement factor comes from the solution of $\phi_{nm} (\vec{J} = 0)$ for the continuum states of a 2D exciton. A detailed derivation of the eigenfunctions and eigenenergies of the continuum states, as well as bound states of the 3D and the 2D hydrogen atom, is given in [61]. Typically, $1 \leq s_0 \leq 2$, and $s_0 = 2$ for a purely 2D exciton. $R_r$ is the Ryberg energy.

The total exciton energy for the continuum states in $B(E - \hbar \omega)$ is given as

\begin{equation}
E = E_g + E_{en} - E_{hm} + E_r.
\end{equation}

(1.59)
Once the absorption spectra for either polarization are obtained by adding the discrete and continuum components, the corresponding refractive index changes can be obtained using the Kramers–Kronig relation given in Eq. (1.22). In the following section, the electrorefraction of a particular CQW structure is simulated using this model.

1.5.2 Electrorefraction in CQW Structures

Although the research on CQW structures has not been as intense as the research on SQWs, there has been considerable research effort dedicated to CQW structures in the last two decades. However, a large part of this effort was focused on studying the basic physics and optical phenomena in GaAs–AlGaAs CQW structures, both experimentally and theoretically [63], [65]–[71]. Compared to SQWs, there have been few attempts to develop and optimize devices based on CQW structures for EA and ER modulators, especially for 1550 nm operation. Regarding EA modulators, some of the research that did include specific device considerations, such as chirp, focused on GaAs material systems [72], [73]. A rare example of a 1550 nm CQW EA modulator, that demonstrated an improved effect compared to SQW EA modulators, was presented only recently [74] (in 2004). As regards ER modulators, the CQW structures studied have also been mainly based on GaAs material systems and have demonstrated significant improvements over SQW ER modulators, both theoretically [75] and, recently, experimentally [76], [77] (in
2001 and 2004, respectively). A 50 GHz modulator based on GaAs–AlGaAs quantum
well structures studied in [77] has already been demonstrated in [78]. The drive voltage
of the device was 3 V, which was unexpectedly large considering the theoretical
predictions of a very large electrorefraction effect. Subsequently, it was shown that the
electrorefraction effect in these structures is very sensitive to the layer thickness and
compositional variations that occur during the growth process [79], making it challenging
to realize the large electrorefraction effect predicted by theory. This is true for CQW
structures in general, and it is probably the main factor impeding the development of ER,
as well as EA, CQW modulators. In general, the CQW structures intended for 1550 nm
operation are expected to be even more sensitive to the variations than GaAs-based
structures because they contain ternary and/or quaternary epitaxial layers. So far, research
on CQW structures in these material systems has only been theoretical [45], [60], [1]–[3],
and no fabricated 1550 nm ER CQW modulators have been reported.

As will be shown in the following chapters, the two main objectives of this thesis are the
improvement of the robustness to growth of CQW structures for ER as well as EA
modulators and the facilitation of polarization modulation using these structures.
However, before addressing these two objectives, basics of electrorefraction in CQW
structures are presented.
Fig. 1.18 shows the energy-band diagram for an InGaAs-InAlAs CQW structure as well as the two lowest energy electron wave functions ($\Psi_{E1}$ and $\Psi_{E2}$), the two lowest energy light-hole wave functions ($\Psi_{LH1}$ and $\Psi_{LH2}$), and the two lowest energy heavy-hole wave functions ($\Psi_{HH1}$ and $\Psi_{HH2}$) for an electric field, $F$, of 0, 19, and 35 kV/cm. The CQW structure also confines some other, higher energy wave functions, which are not shown in Fig. 1.18 because they do not make significant contributions to the electrorefraction effect. The CQW structure has In$_{0.53}$Ga$_{0.47}$As wells and In$_{0.52}$Al$_{0.48}$As barriers, so that all of the epitaxial layers are lattice-matched to (001) InP. The left-hand side well (QW1) is 48 Å thick, and the right-hand side well (QW2) is 54 Å thick. The middle barrier is 36 Å thick, and each of the external barriers is 90 Å thick. For $F = 0$ kV/cm, $\Psi_{E1}$, $\Psi_{HH1}$, and $\Psi_{LH1}$ are localized in QW2 because it is thicker than QW1 and provides lower potential energy to these wave functions, as shown in Fig. 1.18(a). QW2 would have the same effect if it was made deeper than QW1. Compared to the other two wave functions, $\Psi_{HH1}$ is the most strongly localized because it has the largest effective mass. The second lowest energy wave functions, i.e., $\Psi_{E2}$, $\Psi_{HH2}$, and $\Psi_{LH2}$, are localized in QW1 for $F = 0$ kV/cm.

When the electric field is increased to about 19 kV/cm, as shown in Fig. 1.18(b), $\Psi_{E1}$ and $\Psi_{E2}$ become approximately equally distributed between the two wells. For this electric field, the energy separation between the two wave functions becomes the smallest, and the electric field is called the resonant electric field for electrons, $F_E$. When the electric field is increased above $F_E$, as shown in Fig. 1.18(c), $\Psi_{E1}$ and $\Psi_{E2}$ become strongly
localized in QW1 and QW2, respectively. No similar anticrossing of $\Psi_{LH1}$ and $\Psi_{LH2}$ or $\Psi_{HH1}$ and $\Psi_{HH2}$ occurs in Fig. 1.18. These wave functions simply become more strongly localized to their quantum wells as the electric field is increased. These wave functions would anticross if the electric field was applied in the opposite direction, or if QW1 was wider than QW2 and $\Psi_{LH1}$ and $\Psi_{HH1}$ were localized in it for $F = 0$ kV/cm. The electric-field-induced anticrossing of only one type of wave function, e.g., the electron wave functions, without the anticrossing of the other types, e.g., the light-hole and the heavy-
hole wave functions, gives rise to a special electrorefraction effect largely exploited in this thesis.

Figs. 1.19(a) and (b) show the electric-field dependence of the squared overlap integrals between the conduction and valence band wave functions of Fig. 1.18. The overlap integrals are evaluated using Eq. (1.18), and, for example, the curve corresponding to the overlap integral for the $\Psi_{E1}$-$\Psi_{HH1}$ transition is labeled as “$E1$–$HH1$” in Fig. 1.19(a). In the literature, the transitions between $\Psi_{E1}$ and $\Psi_{HH1}$, $\Psi_{E2}$ and $\Psi_{HH2}$, $\Psi_{E1}$ and $\Psi_{LH1}$, and $\Psi_{E2}$ and $\Psi_{LH2}$ are sometimes referred to as the “symmetric-mode transitions” [80]. Similarly, the transitions between $\Psi_{E1}$ and $\Psi_{HH2}$, $\Psi_{E2}$ and $\Psi_{HH1}$, $\Psi_{E1}$
and $\Psi_{LH2}$, and $\Psi_{E2}$ and $\Psi_{LH1}$ are sometimes referred to as the “asymmetric-mode transitions.”

In Fig. 1.19(a), the squared overlap integrals corresponding to the electron-heavy-hole symmetric-mode transitions decrease with $F$, while the squared overlap integrals corresponding to the electron-heavy-hole asymmetric-mode transitions increase with $F$. This behavior results from the electric-field-dependent redistribution of $\Psi_{E1}$ and $\Psi_{E2}$ only, as the distributions of $\Psi_{HH1}$ and $\Psi_{HH2}$ barely depend on $F$ in the region of interest (0 ≤ $F$ ≤ 35 kV/cm). Also, the shapes of the curves in Fig. 1.19(a) suggest that the distributions of $\Psi_{E1}$ and $\Psi_{E2}$ are most sensitive to changes in $F$ when these wave functions are approximately equally distributed between QW1 and QW2, i.e., when $F \approx F_E$. In general, a distribution of any wave function in Fig. 1.18 is most sensitive to both changes in $F$ and relative changes in the thicknesses and compositions of the two wells when the wave function is approximately equally distributed between the two wells, and, conversely, it is least sensitive to these changes when the wave function is strongly confined to one of the wells. Later in this thesis, this phenomenon will be used to design CQW structures which are quite robust to the growth process.

Fig. 19(b) shows that the squared overlap integrals corresponding to the electron-light-hole transitions exhibit similar dependence on $F$ to that of the electron-heavy-hole transitions. However, the squared overlap integrals for the electron-light-hole symmetric-
mode transitions first increase as \( F \) is changed from 0 to about 7 kV/cm, and then decrease for higher \( F \). The reason for this behavior is that \( \Psi_{LH1} \) and \( \Psi_{LH2} \) are less strongly confined to their respective wells than \( \Psi_{E1} \) and \( \Psi_{E2} \) are [see Fig. 1.18(a)], and it takes a small change in \( F \) (again, about 7 kV/cm) to maximize the spatial overlaps between the wave functions for the symmetric-mode transitions before they start decreasing toward very small values. Fig. 19(b) also shows that the opposite is true for the electron-light-hole asymmetric-mode transitions. In addition, the weak confinement of \( \Psi_{LH1} \) and \( \Psi_{LH2} \) for small \( F \) makes the value of \( F \) for which the squared overlap integrals of the symmetric-mode and asymmetric-mode transitions are equal be somewhat larger than the one for the electron-heavy-hole transitions in Fig. 19(a).

Besides obtaining the electric-field dependence of the squared overlap integrals associated with the wave functions confined by CQW structures, it is essential to obtain the electric-field dependence of the exciton binding energies associated with these wave functions. This is because the contributions of the discrete exciton states to the absorption spectra [Eq. (1.45)] dominate the electroabsorption and, in turn, electrorefraction in CQW structures, and these contributions strongly depend on both the squared overlap integrals and binding energies associated with the wave functions. In Eq. (1.45), the discrete exciton state absorption spectrum, \( \alpha_c \), is proportional to the probability of an electron in state \( n \) and a hole in state \( m \) being in the same unit cell in the plane of the quantum well, \( i.e., \left| \phi_{nm}(\bar{r} = 0) \right|^2 \), which, in turn, is proportional to the exciton binding energy. Again,
according to Eq. (1.42), the exciton binding energy is inversely proportional to the exciton in-plane radius, $\lambda$. Figs. 1.20(a) and (b) show how the binding energies of the heavy-hole and the light-hole excitons depend on $F$.

![Graph](image)

Figure 1.20: Binding energies of the excitons corresponding to the transitions (a) between the two lowest energy electron and heavy holes and (b) between the two lowest energy electron and light holes.

For small values of $F$, those below $F_E$, the binding energies corresponding to the symmetric-mode transitions are large, and the binding energies corresponding to the asymmetric-mode transitions are small. For large values of $F$, those above $F_E$, the binding energies corresponding to the symmetric-mode transitions are small, and the binding energies corresponding to the asymmetric-mode transitions are large. This behavior of the binding energies in Fig. 1.20 is similar to the behavior of the squared overlap integrals in Fig. 1.19 because, as mentioned above, separating the electron and hole wave functions
of an exciton in the z direction (direction normal to the planes of the quantum wells) increases the in-plane exciton size.

Now, having obtained the electric-field dependence of the squared overlap integrals and the binding energies in CQW structures, it is easy to describe electroabsorption in these structures. Fig. 1.21 shows the absorption spectra for the TM polarization for $F = 0, 20,$ and $35 \text{kV/cm}$. According to the polarization selection rules given in Eqs. (1.48) and (1.49), heavy-hole excitons do not contribute to the TM absorption spectra, and only the light-hole exciton peaks are present in Fig. 1.21. For $F = 0 \text{kV/cm}$, the two exciton peaks in the figure are dominated by the symmetric-mode transitions, which have large squared overlap integrals and large binding energies for small $F (F < F_E)$. In the absorption spectrum, the symmetric-mode transitions are indistinguishable from the asymmetric-mode transitions, not only because the asymmetric-mode transitions have small squared overlap integrals and small binding energies for small $F$, but also because the energy separations between the symmetric-mode transitions and asymmetric-mode transitions are of the same order of magnitude as the HWHM of the broadening function. For $F = 35 \text{kV/cm}$, the heights and the energy/wavelength positions of the two peaks are similar to those for $F = 0 \text{kV/cm}$, however, for $F = 35 \text{kV/cm}$, the peaks are dominated by asymmetric-mode transitions, as they have large squared overlap integrals and large binding energies for large $F (F > F_E)$. For $F = 20 \text{kV/cm}$, however, the symmetric-mode transitions and the asymmetric-mode transitions make similar contributions to the
absorptions peaks, which are considerably lower than the absorption peaks for \( F = 0 \) and 35 kV/cm.

![Absorption spectra for the TM polarization.](image)

**Figure 1.21:** Absorption spectra for the TM polarization.

The fact that the absorption peaks are smaller when the symmetric-mode transitions and asymmetric-mode transitions make similar contributions, as compared to when one type of transition dominates, cannot be solely explained by the squared overlap integrals in Fig. 1.19. This is because there is no significant electric-field-induced change in the energies of the transitions and the total sum of the squared overlap integrals. For
example, in Fig. 1.19(b), the squared overlap integrals for the symmetric-mode transitions are ~1, and those for the asymmetric-mode transitions are ~0 for $F \approx 7 \text{kV/cm}$. Therefore, the total sum of the squared overlap integrals is ~1. When $F \approx 22 \text{kV/cm}$, the squared overlap integrals for both the symmetric-mode and asymmetric mode transitions are ~0.5, so that the total sum of the squared overlap integrals is, again, ~1. The squared overlap integrals, alone, therefore, conserve the absorption strength in Eq. (1.45).

However, the squared overlap integrals in Eq. (1.45) are scaled by the corresponding values of $|\phi_{nm}(\bar{\rho} = 0)|^2$, which are, again, proportional to the binding energies. For small $F$, the absorption peaks are large because they are dominated by the symmetric-mode transitions, which have their squared overlap integrals (~1) scaled by large $|\phi_{nm}(\bar{\rho} = 0)|^2$ calculated for large binding energies of about -5.5 meV. For $F \approx 20 \text{kV/cm}$, however, the absorption peaks are small because the squared overlap integrals for the symmetric-mode and asymmetric-mode transitions (their sum is ~1) are scaled by small $|\phi_{nm}(\bar{\rho} = 0)|^2$ calculated for small binding energies of about -4.5 meV. For $F \approx 35 \text{kV/cm}$, the absorption peaks are large again because they are now dominated by the asymmetric-mode transitions, which have their squared overlap integrals (~1) scaled by large $|\phi_{nm}(\bar{\rho} = 0)|^2$ calculated for small binding energies of about -6 meV.

Similar to Fig. 1.21, Fig. 1.22 shows the absorption spectra for the TE polarization. The electroabsorption process for the TE polarization is analogous to that for the TM
polarization, except that the polarization selection rules allow for the participation of the heavy-hole excitons as well. Because the heavy holes have larger masses than the light holes, the heavy-hole excitons typically have lower transition energies than the light-hole excitons. This point is also illustrated in Fig. 1.23, which shows the transition energies/wavelength for the heavy-hole and light-hole excitons. For $F < F_E$, the absorption spectra for both polarizations are dominated by the symmetric-mode transitions, and the energies of these transitions change only slightly with $F$. As $F$ is increased above $F_E$, the symmetric-mode transitions show a certain amount of red shift.
(E1-HH1 and E1-LH1 transitions) or blue shift (E2-HH2 and E2-LH2 transitions).

Here, however, the absorption spectra are dominated by the asymmetric-mode transitions, which do not display significant red or blue shifts. Consequently, the absorption peaks do not move left or right on the horizontal axis in response to changes in $F$. Rather, the absorption peaks only move up and down, creating large changes in the areas below the absorption spectra. Such behavior is very desirable for obtaining large electrorefraction effects in CQW structures [60].

Figure 1.23: Transition energies and wavelengths for the heavy-hole and light-hole excitons.
Figs. 1.24(a) and (b) show the change of the absorption coefficient and the refractive index for the TM polarization when \( F \) is switched between 0 and 20 kV/cm and between 20 and 35 kV/cm, respectively. Because there is no significant blue or red shifting of the absorption peaks, the absorption coefficient changes in Figs. 1.24(a) and (b) are well localized in wavelength. For the same reason, the absorption coefficient changes in Figs. 1.24(a) and (b) are almost entirely negative and positive, respectively. Consequently, for the wavelengths that are longer than the wavelength corresponding to the lowest energy exciton peak, the Kramers–Krönig relation in Eq. (1.22) predicts large refractive index changes.
changes that are respectively also negative and positive, as shown in Figs. 1.24(a) and (b). The same is true for the absorption coefficient change and the refractive index corresponding to the TE polarization, as shown in Figs. 1.25(a) and (b).

Figure 1.25: TE polarization absorption coefficient change and refractive index change when $F$ is switched between (a) 0 and 20 kV/cm and (b) 20 and 35 kV/cm.

Unlike in CQW structures, in SQWs, an application of the electric field causes large red shifts of the absorption peaks, so that both large positive and large negative changes of the absorption spectra are created (see Fig. 1.15). The opposite-sign changes of the absorption coefficients in SQWs create opposite-sign changes in the refractive indices at higher wavelengths, which is highly undesirable [60].
Fig. 1.26 shows the electric-field-dependent refractive index changes for three different wavelengths across the C-band. Disregarding the increase of the refractive indices for the TM polarization around $F \approx 7 \text{kV/cm}$, which are due to the increase of the light-hole absorption peaks mentioned above, the refractive indices decrease with $F$ in the region below $F_E$ and increase with $F$ in the region above $F_E$ for all curves in Fig. 1.26. The “V” shapes of the curves are characteristic for CQW structures. For any wavelength in Fig. 1.26, the electrorefractive effect is larger for the TE polarization than for the TM
polarization because the heavy-hole excitons participate in the electrorefraction for the 
TE polarization and are closer to the wavelength of operation than the light-hole excitons. 
Consequently, the CQW structures are typically intended for TE Mach–Zehnder 
modulators, where either the negative slope of the refractive index change below $F_E$ or 
the positive slope of the refractive index change above $F_E$ can be used [60], [80]. 

In Fig. 1.26, the refractive index change shows relatively small dependence on the 
wavelength of operation across the C-band. If this dependence was required to be 
decreased even further, detuning of the lowest energy excitons from the wavelength of 
operation would need to be increased. The exciton energies could simply be increased by 
decreasing the thicknesses of the quantum wells in the CQW structure. Unfortunately, the 
larger the detuning, the smaller the electrorefraction effect. Both of these trends are 
evident from Fig. 1.26, where the TM polarization exhibits a smaller dependence on the 
wavelength of operation as well as a smaller electrorefraction effect. Also, due to the 
larger detuning of the corresponding excitons, the TM polarization exhibits smaller 
optical loss and modulation of the optical loss at the wavelength of operation than the TE 
polarization does. However, the magnitude of the optical loss is not easily modeled as it 
strongly depends on the broadening function used in the model. The Gaussian broadening 
functions tend to underestimate the loss, while the Lorentzian broadening functions tend 
to overestimate the loss. For example, the semi-empirical Lorentzian broadening function 
used for modeling of the CQW structure analyzed above, and all of the CQW structures
in this thesis, has a HWHM of about 6 meV [64] and predicts the absorption coefficients for the two polarizations to be in the 10s of cm$^{-1}$ at 1550 nm. However, if a Gaussian broadening function with the same value for the HWHM is used, the corresponding absorption coefficients are several orders of magnitude smaller for both polarizations, again at 1550 nm. Nevertheless, the choice of the broadening function has little (practically no) effect on the refractive index change at the wavelength of operation. Fig. 1.27 compares the refractive index changes obtained using the Gaussian and the Lorentzian broadening functions at 1550 nm, showing no appreciable difference between the two. It turns out that no appreciable difference between the two broadening functions

![Figure 1.27: Comparison of the 1550 nm refractive index changes obtained using the Gaussian and the Lorentzian broadening functions.](image)

is seen even if the HWHMs of the broadening functions are changed. The refractive
index changes are insensitive to the choice of the broadening function because the choice of the broadening function does not significantly affect the areas under the absorption spectra for relatively large wavelength detunings. According to the Kramers–Krönig relation given in Eq. (1.22), it is these areas that affect the magnitudes of the refractive index changes.

Unfortunately, due to the lack of experimental reports on the absorption spectra in InGaAlAs-based CQW structures, choosing the appropriate broadening function for the modeling of these structures is a somewhat challenging task. One way of ensuring small optical losses at the wavelengths of operation is to allow for large wavelength detunings that are comparable to those used in typical 1550 nm ER MQW modulators. For example, in [81], an optical waveguide of a p-i-n diode contained multiple repetitions of 85 Å thick InGaAsP quantum wells and 85 Å thick InP barriers in the 0.4 μm thick intrinsic region. Detuning of the lowest energy exciton in the SQWs from the 1550 nm wavelength of operation was 133 nm. Optical waveguide loss for the TE polarization was measured to be $\sim 1 \text{ cm}^{-1}$ (~0.4 dB/mm) for zero applied voltage. Due to the large red shift of the lowest energy exciton, which is characteristic for SQWs, a 4 V change in the applied voltage induced more than a three-fold increase in the measured waveguide loss and less than $4 \times 10^{-4}$ increase in the measured effective refractive index. A similar behavior was observed in [82] for a p-i-n diode containing twenty 103 Å InGaAsP wells and 80 Å InP barriers in the intrinsic region, which formed ~60 % overlap with the optical mode. A
voltage change from 0 to 5 V induced a red shift of the lowest energy exciton from \(~1440\) nm to \(~1480\) nm, resulting in a large refractive index change (\textit{i.e.}, large phase change across the device) as well as a large optical loss increase for 1557 nm wavelength in a 0.6 mm long waveguide, as shown in Fig. 1.28. As can be seen in the figure, optical loss for small voltages is only a fraction of a decibel and increases to \(~1.5\) dB for a half-wave voltage of \(~4.5\) V. As the excitons in CQW structures do not exhibit significant red shifts for the small changes in \(F\) that are typically applied to them, the optical loss at the wavelength of operation stays relatively independent of \(F\). For example, let's look at a half-wave phase change

![Figure 1.28: Optical loss and phase shift for 1557 nm wavelength in a 0.6 mm long section of an optical waveguide containing twenty InGaAsP–InP SQWs. The squares and triangles are experimentally obtained data points, while the lines come for theoretical models that use fitting parameters [82].](image)
in an optical modulator at $\lambda = 1550$ nm, if we assume that the optical mode has an overlap factor of $\Gamma = 0.60$ for the CQW region, which provides a refractive index change of $\Delta n = 10 \times 10^{-4}$, the interaction length would need to be $L = 1.3$ mm. Consequently, the optical loss of the CQW modulator can be estimated to be below 1 dB for a wavelength detuning that is somewhat larger than 100 nm. Even smaller losses can be expected in CQW modulators that are not based on p-i-n diode structures. The p-doped regions are lossy not only for the electrical signal, but also for the optical mode. The optical loss due to the p-doped region, $\alpha_p \approx (25 \times 10^{-18}$ cm$^2) \times \Gamma_p \times p$, depends on the overlap that the region makes with the optical mode, $\Gamma_p$, as well as the amount of doping, $p (\sim 10^{18}$ cm$^{-3}$) \cite{52}. Besides $\alpha_p$, another major contribution to the residual, wavelength-independent loss is the photon scattering due to the imperfections of the optical waveguide geometry. For example, in a p-i-n diode having a reactive-ion-etched optical waveguide and $p = 2 \times 10^{17}$ cm$^{-3}$, the residual loss for the TE polarization was measured to be $\sim 0.3$ dB/mm \cite{83}. The contribution of the wavelength-dependent loss due to the 0.4 $\mu$m thick InGaAlAs–InAlAs MQW region was $\sim 0.2$ dB/mm for $\sim 130$ nm wavelength detuning.

In addition to the above discussion on optical loss in CQW structures, there are two remaining aspects of them that should be addressed in this chapter before proceeding to the following chapters, where the contributions of this thesis to the state-of-the-art in CQW modulators are given.
First, as will be explained in more detail in Chapters 4 and 5, increasing the thickness of the middle barrier decreases the magnitude of \( F \) needed for switching in CQW structures. Unfortunately, increasing the thickness of the middle barrier also increases the sensitivity to the thickness (~3 Å) and compositional variations (1–2 %) that can be expected to occur in the CQW epitaxial layers during the growth process. In the CQW structures that have switching fields smaller than ~20 kV/cm, the layer thickness and compositional variations can be very detrimental to the electrorefraction effect. For example, Fig. 1.29 illustrates the effect of a 3 Å increase in the thickness of QW2 for the CQW structure.

![Figure 1.29](image-url)

Figure 1.29: (a) 1550 nm refractive index changes for the TE and TM polarizations in the CQW structure of Fig. 1.18 (same as Fig. 1.26) and (b) the same for a 3 Å increase in the thickness of QW2.

shown in Fig. 1.18. The 3 Å thickness variation increases \( F_E \) and places the negative
slope of the refractive index change in the electric-field region in which it is supposed to be positive. Randomly distributed thickness variations (of approximately ±3 Å) are unavoidable between the epitaxial layers in CQW structures [58], and therefore, the total change in the refractive index that the optical mode experiences will be an average of the contributions to the refractive index changes that correspond to each variation. Many of these contributions will have opposite signs and diminish the total, average refractive index change in CQW structures. Again, methods for decreasing the sensitivities of CQW structures to thickness and compositional variations, without compromising the drive electric fields, will be presented in Chapters 4 and 5.

Second, in order to increase the difference between the electrorefraction effects for the TE and TM polarizations, and, thus, achieve efficient polarization modulation, as will be discussed in Chapters 2, 3, and 6, the epitaxial layers in CQW structures need to be slightly strained.

1.5.3 Strain in CQW Structures grown on (001) InP

The lattice constant of InP is $a_0 = 5.869$ Å [84], [85]. Therefore, unless the epitaxial layers in CQW structures are intended to be strained, their compositions have to be chosen so that their lattice constants match that of the (001) InP substrate. For example, In$_{0.53}$Ga$_{0.47}$As and In$_{0.52}$Al$_{0.48}$As are both lattice-matched to (001) InP. If an epitaxial layer
having a lattice constant \( a (\neq a_0) \) is grown on top of a (001) InP substrate, or some other epitaxial layer (or a stack of layers) having lattice constant \( a_0 \), the new epitaxial layer will stretch to accommodate to the lattice constant of the thick bottom layer. Strictly speaking, this is true only if the thickness of the top layer is smaller than the critical thickness, \( h_c \), which is the maximum allowed thickness of the epitaxial layer that can be accommodated by the system without generating any material dislocations and defects [86]. The in-plane strain, \( i.e., \) in-plane fractional distortion of the lattice,

\[
\varepsilon_g = \varepsilon_{xx} = \varepsilon_{yy} = \frac{a_0}{a} - 1
\]  

(1.61)

is the same in both \( x \) and \( y \) directions for cubic semiconductors (\( e.g., \) InP and GaAs) that have their lattice constants the same in all directions [85]. The strain in Eq. (1.61) is called biaxial tension or biaxial compression depending whether \( a \) is smaller or larger than \( a_0 \), respectively. The biaxial strain is accompanied by strain in the growth direction

\[
\varepsilon_\perp = \varepsilon_{zz} = -2 \frac{c_{12}}{c_{11}} \varepsilon_{\parallel},
\]  

(1.62)

where \( c_{12} \) and \( c_{11} \) are elastic stiffness constants [85].

One of the main properties of strained epitaxial layers is energy splitting of otherwise degenerate heavy-hole and light-hole band edges. Fig. 1.30 illustrates this effect for InGaAs and InAlAs layers grown on (001) InP. In both cases, the light-hole band edge is above the heavy-hole band edge for tensile strain, and it is below the heavy-hole band edge for compressive strain. Consequently, it is possible to design the depths of QW1 and
QW2 in CQW structures to be different for light holes and heavy holes, and thereby it is possible to manipulate the relative magnitudes of the electrorefraction effect for the TE and TM polarizations, as will be shown in Chapters 2, 3, and 6. The nature of the band-edge splitting is the same for the quaternary layers studied in these chapters. Also, opposite-sign biaxial strains in some of the layers in these CQW structures are used to balance the strains in neighboring layers and increase $h_c$ of the overall structure.

There is another important property of strained layers that is used in Chapter 4 to decrease the sensitivities of CQW structures to the compositional variations that are expected to occur during the growth process. It is obvious from Figs. 1.30(a) and (b) that

![Diagram showing band-edge energies for In$_{(1-x)}$Ga$_x$As and In$_{(1-z)}$Al$_z$As](image-url)
\(\pm 2\%\) variation in composition from the nominally unstrained In\(_{0.53}\)Ga\(_{0.47}\)As and In\(_{0.52}\)Al\(_{0.48}\)As layers will have a smaller effect on the light-hole band edge than on the electron or heavy-hole band edges. This is particularly true for the In\(_{0.53}\)Ga\(_{0.47}\)As layer shown in Fig. 1.30(a). Therefore, if the electrorefraction effect in a CQW structure having In\(_{0.53}\)Ga\(_{0.47}\)As quantum wells is based on anticrossing the light holes, rather than electrons or heavy holes, the CQW structure should be the least sensitive to compositional variations. Similar effects are characteristic of nearly-lattice-matched quaternary compounds.

The small sensitivity of the light-hole band edge to the lattice-mismatch-induced strain is due to the opposite-sign contributions of the hydrostatic and shear components of the strain, as can be explain using the model-solid theory presented below [50], [85]. The strain-dependent electron, heavy-hole, and light-hole band edges are given as

\[
E_C = E^0_{v,AV} + \frac{\Delta^0}{3} + E^0_{o} + \Delta E^h_c, \quad (1.63)
\]

\[
E_{1HH} = E^0_{v,AV} + \frac{\Delta^0}{3} + \Delta E^h_{AV} + \Delta E^{sh}_{1HH}, \quad (1.64)
\]

\[
E_{2HH} = E^0_{v,AV} + \frac{\Delta^0}{3} + \Delta E^h_{AV} + \Delta E^{sh}_{2HH}, \quad (1.65)
\]

respectively, where the quantities having “0” superscripts correspond to unstrained materials. The first term in Eqs. (1.63)–(1.65) is called “the average valence-band
energy," as it is literally obtained as an average of the energies for the heavy-hole, light-
hole, and split-off bands, i.e.,

$$E_{V, AV} = \frac{E_{HH}^0 + E_{LH}^0 + E_{SO}^0}{3}.$$  \hspace{1cm} (1.66)

The average valence-band energy is used as an absolute energy level for each of the two
materials across the heterojunction and, thus, determines the band-edge discontinuities. In
the second term in Eqs. (1.63)–(1.65), $\Delta^0$ is the spin-orbit splitting energy. The
conduction band energy in Eq. (1.63) is different from the heavy-hole and light-hole band
energies in Eqs. (1.64) and (1.65), respectively, because it contains the band-gap energy
term ($E_G^0$), and because its hydrostatic strain contribution term

$$\Delta E_C^{hy} = a_c (2\varepsilon_a + \varepsilon_\perp)$$  \hspace{1cm} (1.67)

is proportional to the conduction-band hydrostatic deformation potential, $a_c$, rather than
the valence-band hydrostatic deformation potential, $a_v$, which is the case for the
hydrostatic strain contribution to the valence bands, i.e.,

$$\Delta E_{V, AV}^{hy} = a_v (2\varepsilon_a + \varepsilon_\perp).$$  \hspace{1cm} (1.68)

The strain-induced change of the average valence-band energy in Eq. (1.68) changes the
energies of the light-hole band edge and the heavy-hole band edge in the same manner
and does not lift their degeneracy. It is the shear-strain component of the total strain, not
the hydrostatic-strain component, that lifts the degeneracy. The shear-strain effect on the
heavy-hole and the light-hole band edges is represented by
and

\[
\Delta E_{_{\text{LH}}}^{_{\text{th}}} = -\frac{1}{2} \Delta E_{_{\text{th}}}^{_{\text{th}}}
\]

respectively, where

\[
\Delta E_{_{\text{LH}}}^{_{\text{th}}} = -\frac{1}{2} \Delta^0 + \frac{1}{4} \delta E_{_{\text{th}}}^{_{\text{th}}} + \frac{1}{2} \sqrt{(\Delta^0)^2 + \Delta^0 \delta E_{_{\text{th}}}^{_{\text{th}}} + \frac{9}{4} (\delta E_{_{\text{th}}}^{_{\text{th}}})^2},
\]

The quantity \( b \) in Eq. (1.71) is the "tetragonal shear deformation potential." As \( b \) is a negative number and \( a_v \) is a positive number, \( \Delta E_{_{\text{LH}}}^{_{\text{th}}} \) and \( \Delta E_{_{\text{V},{A_V}}}^{_{\text{th}}} \) have opposite signs and make \( E_{_{\text{LH}}} \) less sensitive to strain than \( E_{_{\text{HH}}} \). In this thesis, as is typical for ternary and quaternary strained layers [50], [85], the various quantities used in this theory are interpolated from their theoretically or experimentally obtained binary equivalents.

1.6 Thesis Outline

The following five chapters of this thesis (Chapters 2–6) present manuscripts that have been published, have been submitted for publication, or will shortly be submitted for publication in journals. More specifically, Chapter 2 (article published in IEEE Photonics Technology Letters) presents the initial design for a push-pull polarization modulator, which contains two types of InGaAlAs–InGaAlAs CQW structures in its waveguide. One of these two structures (TS structure) mainly increases the refractive index for the TM
polarization, via the anticrossing of the two lowest energy light holes, while the other structure (CS structure) mainly decreases the refractive index for the TE polarization, via the anticrossing of the two lowest energy heavy holes. In Chapter 3 (article published in Journal of Vacuum Science and Technology A), numerical simulations show that the TS structure is very insensitive to the layer thickness and compositional variations, while the CS structure is quite sensitive to these variations. In Chapter 4 (article published in IEEE Electron Device Letters), the mechanisms responsible for the decreased sensitivity of the TS structures to the layer variations are fully recognized. The anticrossing of the two lowest energy light holes, rather than the two lowest energy heavy holes or the two lowest energy electrons, is shown to be the mode of operation that is least sensitive to the layer variations, and, therefore, the most desirable technology for future CQW modulators. Chapter 5 (manuscript that will shortly be submitted for publication) presents a design method that can be used for improving the robustness to growth of CQW structures in general, including those that have their EA or ER effects based on the anticrossing of electrons or of light holes. In Chapter 6 (manuscript submitted to IEEE Photonics Technology Letters, moderate revisions have been requested), the robustness to growth of the initial design of the push-pull polarization modulator given in Chapter 2 is improved using the knowledge obtained in the work presented in Chapters 3–5. Here, besides several changes that are made to the original design, the CS structure is replaced by a more robust CQW structure that mainly decreases the refractive index for the TE polarization via the anticrossing of the two lowest energy electrons, not the heavy holes.
Chapter 7 is the concluding chapter of the thesis and contains discussion of the thesis' findings and recommendations for the future work.

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2.1 Introduction

Electrorefraction (ER) modulators based on asymmetric coupled quantum-well (ACQW) structures exhibit an electric-field-induced refractive index change that can be an order of magnitude larger than in structures based on square quantum wells [1], [2]. Compared to electroabsorption modulators, ACQW modulators, as well as ER quantum well intensity modulators, in general, are typically implemented in a directional coupler or Mach–Zehnder configuration, and they can provide lower temperature and wavelength sensitivities, lower carrier generation rates, as well as push-pull modes of operation with

adjustable chirp [3]. In this letter, we propose a novel type of ER modulator, which, in a single optical waveguide, contains multiple repetitions of two novel InGaAlAs–InAlAs ACQW structures, grown on (001) InP. By applying an appropriate bias field in the [001] direction, in one of the structures a change in the applied field can be made to cause an increase in the refractive index for TM-polarized light without a commensurate increase in the refractive index for TE-polarized light. In a similar manner, in the other structure the same change in field will cause a decrease in the refractive index for TE light without a commensurate decrease in the refractive index for TM light. Since each structure provides unequal refractive index changes for the two polarizations, if either structure were placed in an optical waveguide, a change in polarization state at the output relative to the state at the input, i.e., polarization conversion, could be achieved (provided that, at the input, light is coupled into both the TE and TM modes). Typically, the powers in the two modes would be matched at the output so that a 90° polarization rotation could be obtained. To achieve push-pull polarization conversion, the effective refractive index change for the TE mode should be opposite in sign to the change for the TM mode [3]. Incorporating both of our structures into an optical waveguide will allow for the design of new push-pull-type quantum well polarization conversion (QWPC) modulators. In addition to traditional applications such as on-off keying, these modulators would likely find applications in areas not typical for quantum well modulators [4].
2.2 Device Basics

A schematic illustration of the compositions and the thicknesses of the layers in the two ACQW structures is shown in Fig. 2.1. The figure also illustrates the direction of the applied electric field $F$. Each structure has In$_{0.53}$Al$_{0.47}$As barriers, which are lattice-matched to the InP substrate, as well as one lattice-matched In$_{0.53}$Ga$_{0.47}$As well. The In$_{0.46}$Ga$_{0.52}$Al$_{0.02}$As well in Fig. 2.1(a) is under ~0.50 % of tensile strain (TS), and the In$_{0.58}$Ga$_{0.37}$Al$_{0.05}$As well of the structure in Fig. 2.1(b) is under ~0.34 % of compressive strain (CS). Because of these lattice-mismatch-induced biaxial strains, the structures of Fig. 2.1(a) and (b) will be referred to as the TS structure and the CS structure, respectively.

<table>
<thead>
<tr>
<th>Layer Composition</th>
<th>Thickness (Å)</th>
</tr>
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<tbody>
<tr>
<td>In$<em>{0.53}$Al$</em>{0.47}$As</td>
<td>~50</td>
</tr>
<tr>
<td>In$<em>{0.53}$Ga$</em>{0.47}$As</td>
<td>72</td>
</tr>
<tr>
<td>In$<em>{0.53}$Al$</em>{0.47}$As</td>
<td>36</td>
</tr>
<tr>
<td>In$<em>{0.46}$Ga$</em>{0.52}$Al$_{0.02}$As</td>
<td>66</td>
</tr>
<tr>
<td>In$<em>{0.53}$Al$</em>{0.47}$As</td>
<td>~50</td>
</tr>
</tbody>
</table>

(a)

<table>
<thead>
<tr>
<th>Layer Composition</th>
<th>Thickness (Å)</th>
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</thead>
<tbody>
<tr>
<td>In$<em>{0.53}$Al$</em>{0.47}$As</td>
<td>~50</td>
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<tr>
<td>In$<em>{0.53}$Ga$</em>{0.47}$As</td>
<td>69</td>
</tr>
<tr>
<td>In$<em>{0.53}$Al$</em>{0.47}$As</td>
<td>12</td>
</tr>
<tr>
<td>In$<em>{0.58}$Ga$</em>{0.37}$Al$_{0.05}$As</td>
<td>45</td>
</tr>
<tr>
<td>In$<em>{0.53}$Al$</em>{0.47}$As</td>
<td>~50</td>
</tr>
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</table>

(b)

Figure 2.1: Schematic for layers (a) TS structure and (b) CS structure. Outside barriers of each structures are ~50 Å in order to ensure ~100 Å decoupling between any two neighboring structures. Direction of applied electric field $F$ is indicated as well.
2.2.1 TS Structure

As mentioned above, for a well-chosen bias field, the TS structure provides a large electric-field-induced refractive index increase for TM light and a smaller electric-field-induced refractive index increase for the TE light. In ER modulators, typically, the refractive index change for TE light is somewhat larger than the one for TM light simply because the lowest energy light holes are at higher energies than the lowest energy heavy holes [2]. Although in some quantum well modulators the polarization dependence of the refractive index has been decreased by lowering the light-hole energies with a tensile strain [2], to the best of our knowledge, no other biaxially strained ACQW structure for use in 1550 nm ER waveguide modulators has been designed to provide a dominant TM-polarization refractive index change.

Fig. 2.2 shows the two lowest energy electron wave functions ($\Psi_{E1}$ and $\Psi_{E2}$), heavy-hole wave functions ($\Psi_{HH1}$ and $\Psi_{HH2}$), and light-hole wave functions ($\Psi_{LH1}$ and $\Psi_{LH2}$) of the TS structure of Fig. 2.1(a) as well as the band edge diagram for its conduction and valence bands for $F = 0, 13, \text{ and } 35 \text{ kV/cm}$. The band gap in the figure is not to scale, and the strain-induced band edge splitting between the heavy-hole and the light-hole bands in the quantum well under tensile strain is illustrated by drawing the heavy-hole band edge with a full line and the light-hole band edge with a dashed line. The material parameters for the structures are calculated using the model-solid theory [5], [6], and the exciton
energies and wave functions are obtained using the effective-mass envelope-function approximation that includes intersubband mixing [7].

\[ F = 0 \text{ kV/cm} \quad F = 13 \text{ kV/cm} \quad F = 35 \text{ kV/cm} \]

\( F = 0 \text{ kV/cm} \)
\( F = 13 \text{ kV/cm} \)
\( F = 35 \text{ kV/cm} \)

(a) (b) (c)

Figure 2.2: Energy band diagram of TS structure of Fig. 1(a) and two lowest energy electron, heavy-hole, and light-hole wave functions at applied electric fields of (a) 0, (b) 13, and (c) 35 kV/cm. Lowest energy electron wave function (\( \Psi_{EI} \)) and heavy-hole wave function (\( \Psi_{HHI} \)) are shown as full thick lines, whereas second lowest energy electron wave function (\( \Psi_{E2} \)) and heavy-hole wave function (\( \Psi_{HH2} \)) are shown as full thin lines. Lowest energy light-hole wave function (\( \Psi_{LHI} \)) is shown as dashed thick line, and second lowest energy light-hole wave function (\( \Psi_{LH2} \)) as dashed thin line. Light-hole band edge is indicated with dashed line. Band gap is not shown to scale.

For low electric fields, \( \Psi_{EI}, \Psi_{HH1}, \) and \( \Psi_{LH1} \) are predominantly localized in the wider unstrained well [see Fig. 2.2(a)]. Therefore, the \( \Psi_{EI}-\Psi_{LH1} \) and the \( \Psi_{E2}-\Psi_{LH2} \) excitons are direct, and the \( \Psi_{EI}-\Psi_{LH2} \) and the \( \Psi_{E2}-\Psi_{LH1} \) excitons are indirect. Since for low fields the overlaps between the electron and the light-hole wave functions of the direct excitons are
large and those of the indirect excitons are small, the direct excitons will dominate the light-hole absorption spectra for both polarizations [1].

At ~13 kV/cm, the direct and the indirect excitons start anticrossing as $\Psi_{LH1}$ and $\Psi_{LH2}$ are approximately equally distributed between the two wells [see Fig. 2.2(b)]. The $\Psi_{E2^-LH1}$ and the $\Psi_{E2^-LH2}$ excitons actually anticross at a somewhat different resonant electric field than the $\Psi_{E1^-LH1}$ and the $\Psi_{E1^-LH2}$ excitons. For thin middle barriers, however, these fields are close enough to be treated as one resonant electric field ($F_R$). At $F_R$, both the direct and the indirect light-hole excitons contribute to the light-hole absorption spectra, although their total contribution is smaller than it was for low electric fields because $\Psi_{LH1}$ and $\Psi_{LH2}$ are further delocalized [1]. In fact, at $F_R$, the area underneath the absorption spectrum of the $\Psi_{E1^-LH1}$, $\Psi_{E1^-LH2}$, $\Psi_{E2^-LH1}$, and $\Psi_{E2^-LH2}$ excitons will be at its minimum for either polarization. For fields greater than $F_R$, the $\Psi_{E1^-LH1}$ and $\Psi_{E2^-LH2}$ excitons become indirect and the $\Psi_{E2^-LH1}$ and the $\Psi_{E1^-LH2}$ excitons become direct [see Fig. 2.2(c)]. The area underneath the absorption spectrum of the light-hole excitons, for either polarization, will increase to be approximately as large as it was for very low fields. Similar anticrossings of the heavy-hole excitons do not occur as the tensile strain in the strained well makes the well effectively shallower for $\Psi_{HH1}$. $\Psi_{HH1}$ consequently stays localized to the unstrained well for the electric fields of interest here.
Considering that the heavy-hole momentum matrix element is practically zero for TM light, the area underneath the total absorption spectrum (including both the heavy-hole and the light-hole excitons) for the TM polarization will change in the same manner as the area underneath the light-hole excitons [3]. Also, there will be a similar, although smaller, change of the area underneath the total absorption spectrum for the TE polarization. The change is smaller because the momentum matrix element for the anticrossing light-hole excitons is one quarter of its value for TM polarization, and the heavy-hole excitons, although having a large momentum matrix element for TE polarization, remain stationary and inactive for the electric fields of interest.

As the two quantum wells are narrow enough to prevent the light-hole excitons from sizable “red shifting,” the change of refractive index for TM light ($\Delta n_{TM}$), at wavelengths higher than the wavelength corresponding to the absorption peak of the $\Psi_{EI}$-$\Psi_{LH1}$ exciton ($\lambda = 1394$ nm for $F = 0$ kV/cm), will follow the change of area underneath the TM polarization absorption spectrum in a straightforward manner [1]. As the electric field is increased toward $F_R$, the slope of $\Delta n_{TM}$ will be negative, and as the electric field is increased above $F_R$, the slope will be positive. The change of the refractive index for TE light ($\Delta n_{TE}$) will behave similarly, following the smaller change of the area underneath the TE polarization absorption spectrum.
Fig. 2.3 illustrates how $\Delta n_{TM}$ and $\Delta n_{TE}$ of the TS structure, plotted relative to their zero-electric-field values, depend on the electric field. The two curves are plotted for operation at $\lambda = 1550$ nm and are labeled $\Delta n_{TM(TS)}$ and $\Delta n_{TE(TS)}$, respectively. Similarly, Fig. 2.3 also depicts $\Delta n_{TE}$ and $\Delta n_{TM}$ of the CS structure ($\Delta n_{TE(CS)}$ and $\Delta n_{TM(CS)}$, respectively).

![Figure 2.3: Refractive index changes of TS and CS structures, for both TE and TM polarizations, plotted relative to zero-electric-field values at $\lambda = 1550$ nm. $\Delta n_{TM(TS)}$ and $\Delta n_{TE(TS)}$ are labels for refractive index changes for respective TM and TE polarizations of TS structure. Similarly, $\Delta n_{TE(CS)}$ and $\Delta n_{TM(CS)}$ are refractive index changes for TE and TM polarizations of CS structure.](image)
2.2.2 CS Structure

Fig. 2.4 depicts the band edge diagram and the two lowest energy electron, heavy-hole, and light-hole wave functions of the CS structure of Fig. 2.1(b), as was done for the TS structure in Fig. 2.2, now for $F = 0$, 27, and 35 kV/cm. In this case, however, it is the light-hole excitons that are stationary because the compressive strain in the right-hand side well makes it effectively shallower for the light holes. The CS structure is designed so that $F_R \approx 27$ kV/cm for the heavy-hole excitons. Considering that the heavy-hole momentum matrix element for the TM polarization is zero and that it is dominant for the TE polarization, the slopes of $\Delta n_{TE(CS)}$ on either side of $F_R$ will have larger magnitudes as
compared to those of $\Delta n_{\text{TM(CS)}}$ for the electric fields of interest, as shown in Fig. 2.3. Here, the wavelength corresponding to the absorption peak of the $\Psi_{\text{EI}} - \Psi_{\text{HH1}}$ exciton, for $F = 0$ kV/cm, is $\lambda = 1465$ nm.

2.3 Low-Chirp Push-Pull QWPC Modulator

Between $F \approx 15$ kV/cm and $F \approx 25$ kV/cm, the TS structure mainly contributes a positive slope of $\Delta n_{\text{TM(TS)}}$ (with a much smaller positive slope of $\Delta n_{\text{TE(TS)}}$), and the CS structure mainly contributes a negative slope of $\Delta n_{\text{TE(CS)}}$ (with a much smaller negative slope of $\Delta n_{\text{TM(CS)}}$). Placed together in an optical waveguide of a QWPC modulator, multiple repetitions of the two structures will cause the effective refractive index seen by the fundamental TM mode ($n_{\text{eff,TM}}$) to increase and the effective refractive index seen by the fundamental TE mode ($n_{\text{eff,TE}}$) to decrease, providing a push-pull polarization conversion for input light that contains both polarizations.

Each structure's relative contribution to the changes in $n_{\text{eff,TM}}$ and $n_{\text{eff,TE}}$ depends on the structure's overlap with the TM and TE modes, respectively. These optical overlaps can be controlled by adjusting the number of repetitions of each structure in the waveguide, by adjusting the position and order of the repetitions of the two structures, and/or by adjusting the waveguide's geometry. For example, if one were to form a symmetric slab waveguide consisting of an In$_{0.53}$Al$_{0.47}$As substrate, six repetitions of the TS structure,
five repetitions of the CS structure, six repetitions of the TS structure, and an 
In\textsubscript{0.53}Al\textsubscript{0.47}As superstrate, \textit{i.e.}, an In\textsubscript{0.53}Al\textsubscript{0.47}As/6×TS/5×CS/6×TS/In\textsubscript{0.53}Al\textsubscript{0.47}As structure, 
in a 3.4 mm long waveguide, a 90° polarization rotation could be achieved when the 
electric field was increased from 20 to 25 kV/cm. Here, the magnitudes of the changes in 
n_{\text{eff,TM}} and n_{\text{eff,TE}} are relatively closely matched so that only a small chirp α<sub>1</sub> < 0.1 [3] 
should arise due to nonlinear refractive index and absorption changes in the two 
structures. Also, a similar result would be obtained or an 
In\textsubscript{0.53}Al\textsubscript{0.47}As/10×TS/6×CS/In\textsubscript{0.53}Al\textsubscript{0.47}As structure. In both examples, the linear electro-
optic contributions have been taken into account.

References

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effect in a five-step asymmetric coupled quantum well with modified potential,” \textit{IEEE J. 


Chapter 3
Robustness of Push-Pull CQW Polarization Modulator

3.1 Introduction

Studies on optimization of electro-optic [1] and nonlinear [2] properties of asymmetric coupled quantum well (ACQW) structures have been performed for many years now. Together with three-step quantum well structures [3], ACQW structures [4] have been shown to provide electrorefractive responses that are considerably greater than the ones of square quantum wells.

Recently, the authors proposed two InGaAlAs–InAlAs ACQW structures, grown on (001) InP, which, due to their electrorefractive properties, could be used in polarization-
conversion as well as intensity-modulation applications [5]. In one of the two structures, which contains a quantum well that is under tensile strain, the TS structure, a change in an applied electric field will increase the refractive index seen by TM-polarized light significantly more than the refractive index seen by TE-polarized light. In the other structure, which contains a quantum well that is under compressive strain, the CS structure, the same change in applied electric field will decrease the refractive index seen by TE-polarized light significantly more than the refractive index seen by TM-polarized light. Because each of the structures primarily affects only one of the supported polarizations, and thereby only one of the modes, placing multiple repetitions of either structure in an optical waveguide can facilitate an electric-field-induced change in the polarization state of the output light for input light that contains both the fundamental TE and TM modes. At the output of the waveguide, the powers of the two modes must be matched in order to achieve switching between two orthogonal polarization states (i.e., to achieve 90° polarization rotation). However, if multiple repetitions of both the TS and CS structures are placed in the optical waveguide of a modulator, the two structures can be made to provide an opposite-sign, and approximately equal-magnitude, change of the effective refractive indices for the two modes. Such a device, which we refer to as a quantum well polarization-conversion (QWPC) modulator, should provide push-pull type of polarization modulation, a mode of operation that is not typical for quantum well modulators and that will find use in an ever-increasing number of polarization-modulation applications [5]–[7].
Figures 3.1(a) and (b) illustrate the thicknesses and compositions of the layers in the TS and CS structures, respectively, as well as the direction of the applied electric field $F$ [5]. By placing appropriate numbers of repetitions of these TS and CS structures, so as to give overlap factors of $\sim 0.41$ and $\sim 0.22$ for the fundamental TE and TM modes in a waveguide forming a QWPC modulator, respectively, a push-pull polarization conversion giving a small chirp parameter, i.e. $\alpha_H \approx 0.05$ [8], should be possible to achieve in a 3.0 mm long device when the electric field is switched from 20 to 25 kV/cm. This chirp would mainly be due to nonlinearities in the absorption and refractive index changes in the two structures [5].

![Figure 3.1:](a) TS structure containing a quaternary quantum well which is under $\sim 0.50$ % of tensile strain and (b) CS structure containing a quaternary quantum well which is under $\sim 0.34$ % of compressive strain.)
3.2 Influence of Layer Variations

As the next step in developing the TS and CS structures for use in a QWPC modulator, we investigate how the electrorefractive properties of these structures depend on the thickness and compositional variations of their layers. The investigation reveals the trends and issues pertaining to the variations, and it indicates the design objectives for optimizing the performance of the structures. For each structure, the thickness of its unstrained quantum well, \( w_1 \), and the thickness of its strained quantum well, \( w_2 \), are varied by \( \pm \Delta w_1 \) and \( \pm \Delta w_2 \), respectively. The gallium mole fractions in both quantum wells, \( x_1 \) and \( x_2 \), are varied by the same amount, \( \pm \Delta x \), and the aluminum mole fraction in the quaternary, strained quantum well, \( z_2 \), is varied by \( \pm \Delta z \). Even when neglecting the compositional and thickness variations for the barriers in each structure, the remaining two thickness and three compositional variations necessitate \( 3^5 (=243) \) different simulations of each structure in order to obtain the statistical average absorptions and refractive indices of the two structures [4]. The statistical average responses, as figures of merit for the layer thickness and compositional variation effects on the TS and CS structures, are calculated as described below.

If in one of the variations of a structure, say structure \( i \), \( x_1 \) is decreased by \( \Delta x \), \( z_2 \) is increased by \( \Delta z \), and \( w_2 \) is increased by \( \Delta w_2 \), the probability of its occurrence will be

\[
P_i = (1 - p_{w_1}^- p_{w_1}^+) p_{x_1}^- p_{w_2}^+ (1 - p_{x_2}^- p_{x_2}^+) p_{z_2}^+.
\] (3.1)
Here, $p_{w_1}^+$ and $p_{w_1}^-$ are the probabilities of $w_1$ changing by $+\Delta w_1$ and $-\Delta w_1$, respectively, and $p_{x_1}^-$ is the probability of $x_1$ changing by $-\Delta x$. Similarly, $p_{w_2}^+$ and $p_{x_2}^-$ are the probabilities of $w_2$ and $x_2$ changing by $+\Delta w_2$ and $+\Delta x$, respectively, while $p_{x_2}^+$ and $p_{x_2}^-$ are the probabilities of $x_2$ changing by $+\Delta x$ and $-\Delta x$, respectively. In the rest of the discussion, we will assign the probability $p_w$ to $p_{w_1}^+$, $p_{w_1}^-$, $p_{w_2}^+$, and $p_{w_2}^-$. Similarly, we will assign the probability $p_c$ to $p_{x_1}^+$, $p_{x_1}^-$, $p_{x_2}^+$, $p_{x_2}^-$, and $p_{x_2}^-$. Also, the statistical average absorption at wavelength, $\lambda$, and electric field, $F$, of a structure for either polarization is calculated as

$$\bar{\alpha}_{\text{pol(str)}}(\lambda, F) = \sum_{i=1}^{P_4} P_i \alpha_{\text{pol(str)}}^i(\lambda, F),$$

(3.2)

where $\alpha_{\text{pol(str)}}^i(\lambda, F)$ is the absorption for the $i$th structure for either polarization (pol = TE or TM) and structure (str = TS or CS) [4]. The statistical average refractive index for either polarization and structure, $\bar{n}_{\text{pol(str)}}(\lambda, F)$, is obtained from $\bar{\alpha}_{\text{pol(str)}}(\lambda, F)$ via the Kramers–Krönig relations, and both quantities are calculated relative to their values at $F = 14$ kV/cm, which is taken as the lower limit of the region of interest for the electric field.
3.2.1 TS Structure

The TS structure was first analyzed by allowing the thicknesses of its two quantum wells to change by ±5% and allowing x in both wells and z in the strained well to change by ±0.02. At the wavelength of operation $\lambda = 1550$ nm and for electric fields between $F = 14$ and 28 kV/cm, where the positive change of its refractive index for TM polarization $\Delta n_{TM(TS)}$ [5] is larger than the positive change of its refractive index for TE polarization $\Delta n_{TE(TS)}$ [5], Fig. 3.2(a) compares $n_{TM(TS)}$ obtained for $p_c = 0$ and $p_w = 0$ ($\bar{n}_{TM(TS)}^{0.0}$) with $n_{TM(TS)}$ obtained for $p_c = 0.10, 0.20, 0.33$ and $p_w = 0.33$. Similarly, Fig. 3.3(a) compares

\[ \bar{n}_{TM(TS)} \]

Figure 3.2: $\bar{n}_{TM(TS)}$ for (a) $\Delta w_1 = \pm 5\%$ of $w_1$, $\Delta w_2 = \pm 5\%$ of $w_2$, $\Delta x = \Delta z = \pm 0.02$, (b) $\Delta w_1 = \Delta w_2 = \pm 1$ Å, and $\Delta x = \Delta z = \pm 0.01$, and (c) $\Delta w_1 = \Delta w_2 = \pm 1$ Å, and $\Delta x = \Delta z = \pm 0.005$. 
$\tilde{n}_{TE(TS)}$ with $\tilde{n}_{TE(TS)}^{0.0}$ for the same $p_c$ and $p_w$ values. $\tilde{n}_{TM(TS)}^{0.0}$ and $\tilde{n}_{TE(TS)}^{0.0}$ therefore represent the electric-field-induced refractive index changes of the nominally designed structure, when they are adjusted to be zero for $F = 14$ kV/cm, as shown in the two figures. In Fig. 3.2(a), the obtained $\tilde{n}_{TM(TS)}$ curves behave similarly to $\tilde{n}_{TM(TS)}^{0.0}$. This is not true for $\tilde{n}_{TE(TS)}$ of Fig. 3.3(a), which is seen to have a pronounced zigzag pattern. The reason for this zigzag pattern is that the confinement of the lowest energy heavy-hole wave function ($\Psi_{HH1}$) [5] will be weakened for any structure variation that decreases the nominal depth or thickness of the unstrained well or increases the nominal depth or the thickness of the strained well. $\Psi_{HH1}$ will, therefore, transfer to the strained well for lower values of the electric field than it would in the nominal structure contributing to a refractive index change for the TE polarization [9]. Due to the large heavy-hole mass and

![Graphs](image-url)
the large thickness of the middle barrier, these $\Psi_{HH1}$ transfers, i.e., heavy-hole exciton anticrossings [1], [5] will occur for very small electric-field increments causing the rapid changes in $n_{TE(TS)}$. Fig. 3.3(a) does not capture all of the features of $n_{TE(TS)}$ as the data in the figures have been obtained and plotted in 1 kV/cm increments in $F$.

Similar to Figs. 3.2(a) and 3.3(a), Figs. 3.2(b) and 3.3(b) show $n_{TM(TS)}$ and $n_{TE(TS)}$ for the same values of $p_c$ and $p_w$ except that now $\Delta w_1 = \Delta w_2 = \pm 1$ Å, $\Delta x = \pm 0.01$, and $\Delta z = \pm 0.01$. Even though, for these smaller variations, the refractive index for TM-polarized light changes less from its nominal value, the variations are still not small enough to eliminate the heavy-hole exciton anticrossings that contribute to $n_{TE(TS)}$.

However, here, the number of variations of the structure that result in the heavy-hole exciton anticrossings for the electric fields between $F = 14$ kV/cm and $F = 28$ kV/cm is smaller than in Fig. 3.3(a) so that none of the resulting zigzag features of the $n_{TE(TS)}$ curves are captured. However, decreasing the compositional variations in the structure even further, [see Fig. 3.2(c) and Fig. 3.3(c)], so that $\Delta w_1 = \Delta w_2 = \pm 1$ Å, $\Delta x = \pm 0.005$, and $\Delta z = \pm 0.005$ does eliminate the zigzag pattern successfully and makes the $n_{TM(TS)}$ and $n_{TE(TS)}$ curves overlap almost entirely with the $n_{TM(TS)}^{0,0}$ and $n_{TE(TS)}^{0,0}$ curves. Here, the absence of the zigzag pattern in $n_{TE(TS)}$ is real, and it is not an artifact of the sampling, as it was in Fig. 3.3(b). This is confirmed by simulating the most extreme variation of the structure, which is the one that gives the narrowest and shallowest unstrained well and
the widest and deepest strained well, and observing that $\Psi_{HH1}$ does not transfer to the strained well for the electric fields of interest.

3.2.2 CS Structure

Similar to Figs. 3.2 and 3.3, Figs. 3.4 and 3.5, show $n_{TE(CS)}$ and $n_{TM(CS)}$ of the CS structure for the same well thickness and compositional variations. Compared to the TS structure, $n_{TE(CS)}$ for the CS structure deviates significantly from its nominal value, even for the smallest thickness and compositional variations, [see Fig. 3.4(c)]. The CS structure has a greater sensitivity to the compositional and thickness variations because the CS structure, for its operation, relies on the heavy holes, i.e., the anticrossing of the

Figure 3.4: $n_{TE(CS)}$ for the same variations as Fig. 3.2.
Figure 3.5: $\bar{n}_{TM(CS)}$ for the same variations as Fig. 3.2.

heavy-hole excitons, and the TS structure on the light holes, i.e., the anticrossing of the light-hole excitons. The heavy holes, because of their greater mass, are closer to bottoms of the quantum wells and more susceptible to changes of the wells' compositions and widths. Also, the heavy-hole band edge ($E_{HH}$) and the conduction band edge ($E_C$) change more dramatically than the light-hole band edge ($E_{LH}$) when a variation in composition occurs [10]. For example, for the strained well of the CS structure, $E_{LH}$ will change much less than $E_{HH}$ and $E_C$ when $x$ is changed from its nominal value of 0.37. In fact, $E_{LH}$ will increase (toward positive energies) by less than 1 meV when $x$ is increased to 0.39. For the same change in $x$, $E_{HH}$ will decrease by ~9 meV, and $E_C$ will increase by ~7 meV. It is, therefore, not surprising that $\bar{n}_{TM(TS)}$ and $\bar{n}_{TM(CS)}$ show better performance than $\bar{n}_{TE(TS)}$ and $\bar{n}_{TE(CS)}$, both of which strongly depend on the behaviour of the heavy holes.
3.3 Discussion

In analyzing the TS and CS structures of Fig. 3.1, each of which could be used separately, or both of which could be combined to form a push-pull QWPC modulator, the electrorefractive properties of the TS structure prove to be less sensitive to the structure variations provided that it has been designed so that no variation of the structure allows the heavy-hole excitons to anticross. The electrorefractive properties of the TS structure will then barely deviate from their nominal values for compositional variations that are smaller than or equal to ~0.01 and for the well thickness variations of ~1 Å. This structure would be useful in any device requiring that upon the application of a (001) electric field the refractive index change for TM-polarized light be significantly greater than the refractive index change for TE-polarized light.

The current design of the CS structure is significantly more sensitive to small variations in thickness and composition than that of the TS structure. For example, considering the effect of a 1 Å thickness and 0.005 compositional variation on the performance of a QWPC modulator for all the different values of $p_c$ and $p_w$ used in the figures above, we find that as $p_c$ increases from 0 to 0.10, 0.20, and 0.33 (again, here, $p_w = 0.33$ for all values of $p_c$ except for the nominal structure, where they are both zero), the length of the
QWPC modulator needed to maintain a low drive electric field of 5 kV/cm increases from 3.0 mm to 3.7, 4.1, and 4.9 mm, respectively. Also, the chirp parameter corresponding to $p_e = 0.10$, 0.20, and 0.33 will approximately increase to 1, 1.5, and 3, respectively. While we conclude that very tight control of the fabrication tolerances would be needed for the CS structure in a low-chirp QWPC modulator, this study has shown that a practical TS structure should be possible and provides the motivation for further investigation into the design of the CS structure.

References


Chapter 4
Robust CQW Electrorefraction Modulator

4.1 Introduction

Similar to square quantum well (SQW) structures, coupled quantum well (CQW) structures have been studied for their use in both electroabsorption and electrorefraction (ER) modulators made in the InP and GaAs material systems [1]–[4]. Although, in ER modulators, the magnitude of the electric-field-induced refractive-index change achievable with CQW structures is similar to that achievable with SQW structures, CQW structures have the advantage that they exhibit no significant absorption modulation [1]. An additional advantage of CQW structures is that they provide the refractive-index

change for considerably lower applied electric field $F$ (leading to much lower drive voltages in devices using them) [1]–[3]. Until now, CQW structures have had the disadvantage that they are typically very sensitive to layer thickness and compositional variations [2], [3], [5]. Here, we introduce an InGaAs/InAlAs CQW structure (structure #1) that is very robust to these layer thickness and compositional variations. To achieve this robustness, this structure has its ER effect based on the anticrossing of the lowest energy light-hole wave function ($\Psi_{LH1}$) with the second lowest energy light-hole wave function ($\Psi_{LH2}$) and, consequently, is more appropriate for use in transverse magnetic (TM) ER modulators [6]. We compare our structure to a similar InGaAs/InAlAs CQW structure (structure #2) that has its ER effect based on the anticrossing of the lowest energy electron wave function ($\Psi_{E1}$) with the second lowest energy electron wave function ($\Psi_{E2}$), and as such, the structure is more appropriate for use in transverse electric (TE) ER modulators [1]. In our comparison, we show that structure #1 has superior robustness, because its ER effect is based on the anticrossing of the light-hole wave functions. We also offer an explanation as to why designing an InGaAs/InAlAs CQW structure that has its ER effect based on the anticrossing of light holes rather than electrons, or heavy holes should provide for better robustness to layer thickness and compositional variations.
4.2 Influence of Layer Variations

In our model, the energy bands are obtained using the model-solid theory [7]. The absorption spectra are obtained using the variational method to solve the exciton equation in the effective-mass approximation [8]. The Lorentzian broadening function used in the model is described in [9], and the refractive-index changes are obtained using the Kramers–Krönig relation [1]. Our model is very similar to that used in [3] and [10] except that, in our model, the refractive-index changes are obtained for a whole period of a CQW structure and not only for the quantum well layers.

Fig. 4.1(a) illustrates $\Psi_{E1}$, $\Psi_{E2}$, $\Psi_{LH1}$, $\Psi_{LH2}$, and the two lowest energy heavy-hole wave functions ($\Psi_{HH1}$ and $\Psi_{HH2}$), as well as the band-edge diagram of structure #1 for $F = 0$, 15, and 35 kV/cm. The structure has In$_{0.52}$Al$_{0.48}$As barriers and In$_{0.53}$Ga$_{0.47}$As wells, both of which are lattice-matched to (001) InP. The thickness of each of the two external barriers is 90 Å, while the thickness of the middle barrier is 27 Å. The thicknesses of the left-hand side well (QW1) and the right-hand side well (QW2) are 72 and 60 Å, respectively (i.e., structure #1 is a 90-72-27-60-90 structure).

As shown in Fig. 4.1(a), for $F = 0$ kV/cm, $\Psi_{LH1}$ and $\Psi_{E1}$ will be mainly localized in the wider QW1, while $\Psi_{LH2}$ and $\Psi_{E2}$ will be mainly localized in the narrower QW2. As $F$ is
increased to 15 kV/cm, $\Psi_{LH1}$ and $\Psi_{LH2}$ will become approximately equally distributed between the two wells, while $\Psi_{E1}$ and $\Psi_{E2}$ will become more strongly localized to the same wells as they were previously. As $F$ is further increased to 35 kV/cm, $\Psi_{LH1}$ will switch to QW2 and $\Psi_{LH2}$ will switch to QW1, while $\Psi_{E1}$ and $\Psi_{E2}$ will be yet more strongly localized to their respective wells. Similar to [6], here, the electric field at which the anticrossing of $\Psi_{LH1}$ and $\Psi_{LH2}$ occurs is called the resonant electric field for the light holes $F_{LH}$ (below, we will also use $F_E$ for the resonant electric field for the electrons). For structure #1, $F_{LH} \approx 15$ kV/cm. Consequently, above $F_{LH}$, the electric-field-induced
The refractive-index change for the TM polarization ($\Delta n_{TM1}$) will have a smooth positive slope and the electric-field-induced refractive-index change for the TE polarization ($\Delta n_{TE1}$) will also have a smooth positive, although considerably smaller, slope [6] as shown in Fig. 4.2. Here, $\Delta n_{TE1}$ and $\Delta n_{TM1}$ (shown relative to their zero-electric-field values) are plotted for $\lambda = 1550$ nm and the energy separation between $\Psi_{E1}$ and $\Psi_{LH1}$ corresponds to $\lambda = 1402$ nm for $F = 0$ kV/cm. Below $F_{LH}$, $\Delta n_{TM1}$ and $\Delta n_{TE1}$ will have smooth negative slopes except at $F \approx 4.5$ kV/cm, where there is a large dip in $\Delta n_{TE1}$. The dip is due to the anticrossing of $\Psi_{HH1}$ and $\Psi_{HH2}$ at $F_{HH} \approx 4.5$ kV/cm, and it does not appear in $\Delta n_{TM1}$ as the heavy-hole momentum matrix element is zero for TM light. The
dip is very sharp because of the large effective masses of $\Psi_{HH1}$ and $\Psi_{HH2}$ and the relatively large thickness of the middle barrier [10].

Analogous to structure #1, structure #2 is a 90-51-30-54-90 lattice-matched structure, and its wave functions and the band-edge diagram are shown in Fig. 4.1(b) for $F = 0, 10,$ and $35 \text{ kV/cm}$. Unlike structure #1, which is designed for modulation of TM light via the anticrossing of $\Psi_{LH1}$ and $\Psi_{LH2}$, structure #2 is designed for modulation of TE light via the anticrossing of $\Psi_{E1}$ and $\Psi_{E2}$ ($F_E \approx 10 \text{ kV/cm}$), while all other wave functions remain localized to their respective wells for the electric fields of interest. In structures of this type, the refractive-index change for TE light is somewhat larger than the refractive-index change for TM light and the structures are, therefore, better suited for use in TE modulators [1]. Here, $\Delta n_{TE2}$ and $\Delta n_{TM2}$ (shown relative to their zero-electric-field values) are also plotted for $\lambda = 1550 \text{ nm}$ and the energy separation between $\Psi_{E1}$ and $\Psi_{HH1}$ corresponds to $\lambda = 1395 \text{ nm}$ for $F = 0 \text{ kV/cm}$. Note: For the purpose of comparison, structure #1 and structure #2 were designed to have similar magnitudes of $\Delta n_{TM1}$ and $\Delta n_{TE2}$ above their corresponding resonant fields and similar resonant fields for light holes and electrons and, furthermore, they were designed to have nearly equal wavelength detunings of their lowest energy anticrossing wave functions from the wavelength of operation ($\lambda = 1550 \text{ nm}$), which should yield similar absorption coefficients at the wavelength of operation.
To compare sensitivities to the layer variations, in each structure, the thicknesses of the
two quantum wells and the middle barrier are changed by $\pm 3 \text{ Å}$. In [3], it is shown that
even such small thickness variations can significantly modify the distributions of wave
functions in CQW structures and, in turn, influence the absorption spectra and the
refractive-index changes in these structures. Similarly, the InAs mole fractions in the
three barriers and each quantum well are changed by $\pm 0.02$. Treating the compositional
and thickness variations separately amounts to $3^5 (= 243)$ compositional and $3^3 (= 27)$
thickness variations of each of the two structures. Each thickness variation is assigned the
same occurrence probability of $1/27$, and similarly, each compositional variation is
assigned the same occurrence probability of $1/243$. The refractive-index changes for
either polarization corresponding to each of the variations are multiplied by the
probability of the variation’s occurrence and then added together in a statistical average,
which is, again, obtained separately for the thickness and the compositional variations.

Prior to any variations of structure #1, $\Delta n_{TM1}$ is plotted as $\Delta n_{TM1}^O$ in Fig. 4.3(a) relative to
its value at $F = 25 \text{ kV/cm}$ for electric fields between $F_{LH}$ and $F = 35 \text{ kV/cm}$. The average
refractive-index changes for the thickness variations ($\Delta n_{TM1}^T$) and for the compositional
variations ($\Delta n_{TM1}^C$) are also plotted in Fig. 4.3(a). Similarly, Fig. 4.3(b) shows the
corresponding curves for $\Delta n_{TE2}$ for structure #2 as $\Delta n_{TE2}^O$, $\Delta n_{TE2}^T$, and $\Delta n_{TE2}^C$,
respectively. It is shown in Fig. 4.3(b) that there will be certain variations (only
compositional variations for this particular design of structure #2) that will allow $\Psi_{1LH1}$
and $\Psi_{1LH2}$ to anticross in the electric-field region of interest, which creates the sharp dip
shown in the TE curve (the data in Fig. 4.3 are obtained and plotted in 1 kV/cm increments of \(F\), which has resulted in loss of detail as regards the features of this dip).

![Refractive Index Change](image)

Figure 4.3: (a) Dependence of structure #1 refractive-index changes for TE and TM polarizations on the thickness and the compositional variations and (b) the same for structure #2.

Even ignoring the heavy-hole anticrossings, it is clear from Fig. 4.3 that \(\Delta n_{TM1}\) is less sensitive to both thickness and compositional variations than \(\Delta n_{TE2}\). Here, \(\Delta n_{TM1}^O\) and \(\Delta n_{TM1}^C\) are practically indistinguishable for all electric fields, which means that structure #1 shows practically no sensitivity to the compositional variations. The same cannot be said for structure #2, as in the region of the greatest slope of \(\Delta n_{TE2}^O\) (15 kV/cm \(\leq F \leq 25\) kV/cm), \(\Delta n_{TE2}^O = 7.3 \times 10^{-4}\), and it is \(~77\%\) larger than \(\Delta n_{TE2}^C\). Structure #1 is also far less sensitive to the thickness variations than structure #2. In the region of the greatest
slope of $\Delta \eta_{TM1}^O$ (20 kV/cm $\leq F \leq 30$ kV/cm), $\Delta \eta_{TM1}^O = 8.7 \times 10^{-4}$, and it is only $\sim 11\%$ larger than $\Delta \eta_{TM1}^T$, whereas in the region of the greatest slope of $\Delta \eta_{TE2}^O$, $\Delta \eta_{TE2}^O$ is $\sim 157\%$ larger than $\Delta \eta_{TE2}^T$. Above $F \approx 25$ kV/cm, $\Delta \eta_{TE2}$ does not seem greatly influenced by the variations, however, its slope in this region is considerably smaller than its maximum slope.

The use of decoupled random variations of the layer thicknesses and compositions is intended to illustrate the robustness of structure #1 to such variations, but it is not intended to model any specific growth process. The main reason for the smaller sensitivity of structure #1 to thickness variations is that the barriers confining the anticrossing $\Psi_{LH1}$ and $\Psi_{LH2}$ in structure #1 are significantly lower than the barriers confining the anticrossing $\Psi_{E1}$ and $\Psi_{E2}$ in structure #2. When close to their respective resonances, $\Psi_{LH1}$ and $\Psi_{LH2}$ are thus spread out over a larger region in space than $\Psi_{E1}$ and $\Psi_{E2}$, and $\Psi_{LH1}$ and $\Psi_{LH2}$ are less influenced by small thickness variations of the quantum well layers because they overlap less with these layers. For the same reason, any compositional variations will also have a smaller effect on $\Psi_{LH1}$ and $\Psi_{LH2}$ in structure #1 than they will on $\Psi_{E1}$ and $\Psi_{E2}$ in structure #2. Our simulations show that InGaAs/InAlAs CQW structures based on the anticrossing of $\Psi_{HH1}$ and $\Psi_{HH2}$ [6], [11] do not benefit from the small valence band discontinuity ratio to the extent that structure #1 does, because the effective masses of $\Psi_{HH1}$ and $\Psi_{HH2}$ are much larger than those of $\Psi_{LH1}$ and $\Psi_{LH2}$ and, thus, $\Psi_{HH1}$ and $\Psi_{HH2}$ are very sensitive to layer variations [5]. Also, even though the light
holes have larger effective masses than the electrons, their reduced localizations make them less sensitive to the layer variations. Another reason for the smaller sensitivity of structure #1 to thickness variations is that its quantum wells are thicker than those in structure #2 so that the $\pm 3 \, \text{Å}$ thickness variations represent smaller percentage changes to the thicknesses of the quantum wells in it. In order for structure #1 and structure #2 to have similar wavelength detunings, structure #1 has to have thicker quantum wells because the energy separation between $\Psi_{LH1}$ and $\Psi_{E1}$ is larger than that between $\Psi_{HH1}$ and $\Psi_{E1}$ in lattice-matched CQW structures. In addition to the benefit that small valence band discontinuity ratio has on the sensitivity of structure #1 to compositional variations, these variations will have considerably smaller effects on the energy levels of the light-hole band edge than they will on the energy levels of the electron or the heavy-hole band edges because of the opposite-sign contributions of the hydrostatic and the shear strain components to the light-hole band edge [7].

Any wave function in a CQW structure will be far less sensitive to the layer variations when it is strongly localized to one of the two wells, as opposed to when it is approximately equally shared by both of the wells [5], which is the case when it is close to resonance and anticrossing with its counterpart of opposite symmetry. Consequently, for the electric fields of interest for structure #1, the variations will have very small effects on the otherwise sensitive $\Psi_{E1}$, $\Psi_{E2}$, $\Psi_{HH1}$, and $\Psi_{HH2}$ as they are strongly localized. This is unlike other CQW structures that have the disadvantage of basing their ER effects
on anticrossing of either $\Psi_{E1}$ and $\Psi_{E2}$ or $\Psi_{HH1}$ and $\Psi_{HH2}$, rather than the insensitive $\Psi_{LH1}$ and $\Psi_{LH2}$.

References


Chapter 5
Improving Robustness in CQW Structures

5.1 Introduction

The coupled quantum well (CQW) structures used in electrorefraction (ER) and electroabsorption (EA) modulators can offer lower drive electric fields, i.e., lower drive voltages, than the square quantum well (SQW) structures typically used in these devices [1], [2]. Increasing the thickness of the middle barrier separating the two quantum wells in a CQW structure can be used to further increase the sensitivities of the structure’s electronic states to changes in the applied electric field, $F$, leading to lower drive voltages [3]. However, it has been shown that increasing the thickness of the middle barrier

A version of this chapter will be submitted for publication. S. Ristic and N. A. F. Jaeger, “Improving robustness to layer thickness and compositional variations of coupled quantum well structures,” J. Vac. Sci. Technol. A-Vacuum, Surfaces, and Films.
increases the sensitivity of the electronic states to any thickness and compositional variations that may occur in the quantum well layers during the growth process [4], and the operation of devices using CQW structures can, therefore, be seriously compromised. Conversely, the middle barrier in CQW structures used in modern EA modulators is quite thin, and the potential of CQW structures to provide very low drive voltages is not fully realized [2]. In this article, we show how decreasing the depth of the quantum wells and simultaneously increasing the thickness of the middle barrier in a CQW structure can be used to reduce the sensitivities of the electronic states to the layer variations without sacrificing their sensitivities to changes in $F$.

5.2 Robustness improvement approach

The CQW structure of interest here, structure $S_A$, is lattice-matched and contains two 51 Å In$_{0.53}$Ga$_{0.47}$As wells that are separated by a 30 Å In$_{0.52}$Al$_{0.48}$As middle barrier and enclosed by 90 Å In$_{0.52}$Al$_{0.48}$As external barriers. The energy difference between the wells and the barriers in the conduction band is $\Delta E_C = 481$ meV [5]. The electron effective mass used in the wells and the barriers is $m_e^* / m_0 = 0.0427 + 0.0328 / 0.48 \times z$, where $z$ represents the Al mole fraction in In$_{(1-z)y}$Al$_z$Ga$_y$As [6]. The ground state electron wave function, $\Psi_E$, in the CQW structure is obtained by solving the one-dimensional, single-particle, time-independent Schrödinger equation using the transfer matrix method [7]. In order to make sure that the results presented here are not influenced by the
particular method of solving the Schrödinger equation, the results have also been confirmed using the finite-difference method [8], where $S_A$ is enclosed in a larger quantum well with infinite barriers.

Fig. 5.1(a) shows $S_A$ and $\Psi_E$ for $F = 0$ kV/cm before (full lines) and after (dashed lines) the thickness of the left-hand side well ($t_{w1}$) has been increased by 3 Å. Before the increase in $t_{w1}$, $\Psi_E$ will be equally distributed between the two wells because $S_A$ is a

![Diagram](image)

Figure 5.1: (a) $S_A$ structure and its electron ground state wave function shown for $F = 0$ kV/cm before (full lines) and after (dashed lines) the thickness of the left-hand side well is increased by 3 Å and (b) same for $S_B$ structure.
symmetric structure. After the increase in $t_{w1}$, $\Psi_E$ will be more strongly localized to the wider well. One way of quantifying the localization of $\Psi_E$ in one of the two wells is to use the “localization parameter” $P$ [4] which is defined as $P = (p_1 - p_2) / (p_1 + p_2)$, where $p_1$ and $p_2$ are the probabilities of finding the ground state electron in the left-hand side well and the right-hand side well, respectively. For example, in Fig. 5.1(a), for $\Psi_E$, $P = 0$ before the increase in $t_{w1}$ and $P = 0.60$ after the increase in $t_{w1}$.

Fig. 5.1(b) shows how $\Psi_E$ responds to a 3 Å change in $t_{w1}$ for $F = 0$ kV/cm after the heights of the barriers have been decreased to $\Delta E_C = 219$ meV (i.e., for In$_{0.52}$Al$_{0.24}$Ga$_{0.24}$As lattice-matched barriers), and the thickness of the middle barrier (t$_{mb}$) has been increased to 46 Å. This new structure is labeled S$_B$. It is clear from Fig. 5.1(b) that the localization of $\Psi_E$ does not change as much in S$_B$ as it does in S$_A$ for the same change in $t_{w1}$ for $F = 0$ kV/cm; now $P$ changes from 0 to 0.37. Furthermore, the larger thickness of the shorter middle barrier in S$_B$ causes the localization of $\Psi_E$ in S$_B$ to have the same response to changes in $F$ as the localization of $\Psi_E$ in S$_A$ does, as shown in Fig 5.2. This behaviour is both interesting and useful.

In Fig. 5.2, the electric-field dependences of localizations of $\Psi_E$ in S$_A$ and $\Psi_E$ in S$_B$ are illustrated by plotting the values of $P$ for S$_A$ and S$_B$, respectively. The two curves are practically indistinguishable for all values of $F$. In a similar fashion, it is also shown in Fig. 5.2 that $\Psi_E$ in S$_B$ is less sensitive to a 3 Å thickness variation ($\Delta t_{w1} = +3$ Å) than $\Psi_E$
Figure 5.2: Localization parameters corresponding to structures $S_A$ and $S_B$ for a 3 Å increase of the thickness and a 10 meV decrease of the depth of the left-hand side well.

in $S_A$ is, for all values of $F$. In addition, the remaining two curves in Fig. 5.2 show that $\Psi_E$ in $S_B$ will also be less susceptible to changes in the depth of the quantum wells. Here, the depths of the left-hand side wells in $S_A$ and $S_B$ have been decreased by 10 meV ($\Delta d_{w1} = -10$ meV) by making the wells out of quaternary compounds, here $\text{In}_{0.52}\text{Al}_{0.01}\text{Ga}_{0.46}\text{As}$ wells. Compared to $\Psi_E$ in $S_A$, $\Psi_E$ in $S_B$ is less sensitive to thickness and compositional variations in the quantum wells because the barriers in $S_B$ are shorter than the barriers in $S_A$. Consequently, $\Psi_E$ will be located in the external barriers to a greater extent, see Fig
5.1(b), and it will be less influenced by any changes that occur in the quantum wells, while still providing the same response to the applied field.

Fig. 5.3 shows that similar changes to the thicknesses and compositions of the middle barriers in \( S_A \) and \( S_B \) will have smaller effects on \( \Psi_E \) than the changes in the quantum wells do. Here, the thicknesses of the middle barriers are increased by 3 Å (\( \Delta t_{\text{mb}} = +3 \, \text{Å} \)), and \( S_B \), with its thicker barrier, performs somewhat better than \( S_A \). When the heights of the middle barriers are decreased by 10 meV (\( \Delta h_{\text{mb}} = -10 \, \text{meV} \)), the effects on \( \Psi_E \) are

![Graph showing localization parameters](image)
even smaller. Here, $S_A$ performs better than $S_B$, but only slightly, when the middle barriers are In$_{0.52}$Al$_{0.47}$Ga$_{0.01}$As and In$_{0.52}$Al$_{0.23}$Ga$_{0.25}$As, respectively. Lastly, Fig. 5.4 shows that decreasing the height of the left-hand side external barrier by 10 meV ($\Delta h_{lb} = -10$ meV) will also have small effects on $\Psi_E$ in $S_A$ and $\Psi_E$ in $S_B$. Here, $S_A$ again performs only slightly better, and that is because the probability of finding $\Psi_E$ in the external barriers is lower for $S_A$. Nevertheless, these marginally increased sensitivities of $S_B$ to the compositional variations in the middle and external barriers by no means outweigh the
benefits of the structure’s decreased sensitivities to the remaining possible layer variations.

5.3 Discussion

We have presented insights that form a basis for developing CQW structures that are robust to growth processes. As modern growth processes are becoming increasingly capable of achieving tight control of quaternary compounds [9], the approach to the design of CQWs should, in turn, allow the design of efficient ER and EA modulators.

References


Chapter 6
Improved Push-Pull CQW Polarization Modulator

6.1 Introduction

Traditionally associated with LiNbO$_3$ or GaAs modulators based on the linear electro-optic effect, polarization modulation has been used to improve the performance of both digital and analog optical communication systems [1]. Recently, we proposed a push-pull polarization-modulation scheme using InGaAlAs-InAlAs CQW structures, which, compared to the traditional polarization-modulation schemes, could provide significant reductions of drive electric fields and waveguide lengths for devices based on it [2]. In this scheme, an electric field, $F$, is applied to the optical waveguide containing multiple

repetitions of two types of CQW structure, which, in this manuscript, we will refer to as structure #1 and structure #2. As a result, structure #1 provides a large, positive change of the refractive index for TM-polarized light ($\Delta n_{TM1}$), accompanied by a smaller change of the refractive index for TE-polarized light ($\Delta n_{TE1}$). Similarly, structure #2 provides a large, negative change of the refractive index for TE-polarized light ($\Delta n_{TE2}$), accompanied by a smaller change of the refractive index for TM-polarized light ($\Delta n_{TM2}$).

Placed together in an optical waveguide, the two structures could provide equal-magnitude and opposite-sign changes of the effective refractive indices for the fundamental TE and TM modes ($\Delta n_{eff(TE)}$ and $\Delta n_{eff(TM)}$) and enable push-pull polarization modulation [2]. Subsequent investigation into the effect that layer thickness and compositional variations have on the two CQW structures revealed that structure #2 is quite sensitive to these variations, which would make polarization modulators using this structure challenging to grow reliably [3]. The main reason for the poor robustness of structure #2 is that its electrorefraction is based on anticrossing of the two lowest energy heavy-hole wave functions ($\Psi_{HH1}$ and $\Psi_{HH2}$), which have large masses and are thus very sensitive to the variations [3]. Here, we show how to redesign structure #2 [see Fig. 6.1(b)] to obtain a structure with dramatically improved robustness by designing its electrorefraction to be based on the anticrossing of the two lowest-energy electron wave functions ($\Psi_{E1}$ and $\Psi_{E2}$), which have much smaller masses. We also show how structure #1 [see Fig. 6.1(a)], with its electrorefraction based on anticrossing of the two lowest-energy light-hole wave functions ($\Psi_{LH1}$ and $\Psi_{LH2}$), could be improved. Modeling of each
structure is performed for 1550 nm light and is based on the variational method to solve the exciton equation in the effective-mass approximation [4].

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Figure 6.1: Schematic of layers for (a) structure #1 and (b) structure #2.

### 6.2 Improved Structure #1 and Structure #2

Fig. 6.2(a) illustrates the band edge diagram and the wave functions for structure #1, for $F = 15$ and $30$ kV/cm. The left-hand side well (QW1) is made wider in order for $\Psi_{E1}$ and $\Psi_{LH1}$ to be mainly localized in it for $F \approx 0$ kV/cm. As $F$ is increased, $\Psi_{LH1}$ and $\Psi_{LH2}$ anticross at the resonant field $F_{LH} \approx 8$ kV/cm. Similar to [2], the electric field region of interest ($15$ kV/cm $\leq F \leq 30$ kV/cm) is above the resonant field, and $\Delta n_{TM1}$ has a positive slope [see Fig. 6.3(a)]. This is because at $F_{LH}$ both the 1S excitons corresponding to the symmetric-mode transitions ($\Psi_{E1}-\Psi_{LH1}$ and $\Psi_{E2}-\Psi_{LH2}$) and the asymmetric-mode
transitions ($\Psi_{E1} - \Psi_{LH2}$ and $\Psi_{E2} - \Psi_{LH1}$) have large radii (i.e., small binding energies) and make small contributions to the TM-polarization absorption coefficient, and, in turn, via the Kramers–Krönig relation, to the refractive index [2]. As $F$ is increased, the refractive index also increases, as the absorption coefficient is dominated by the asymmetric-mode excitons that become well confined and thus have small radii. As also shown in Fig. 6.3(a), $\Delta n_{TE1}$ has a positive, although much
smaller, slope because the light-hole momentum matrix element is smaller for the TE polarization, and $\Psi_{\text{HH}}$ and $\Psi_{\text{HH2}}$ do not anticross and make a negligible contribution to the electrorefraction [2].

Compared to structure #1 in [2], our new structure #1 offers two main improvements. First, QW1 and QW2 are under tensile strain in order to increase the energy separation between the electron and the heavy-hole wave functions. Consequently, the absorption coefficient for the TE polarization at the wavelength of operation is decreased. The compressive strain in the barriers is added to balance the total strain in structure #1 and

![Figure 6.3: Effects of the layer variations on (a) $\Delta n_{\text{TE1}}$ and $\Delta n_{\text{TM1}}$ and (b) on $\Delta n_{\text{TE2}}$ and $\Delta n_{\text{TM2}}$ for 1550 nm operation wavelength.](image-url)
structure #2. Second, for the electric field region of interest, $\Psi_{HH1}$ is localized in the right-hand side well (QW2) rather than QW1. The lowest energy $\Psi_{E1} - \Psi_{HH1}$ transition is, therefore, indirect, which should further reduce the TE polarization absorption. Here, the $\Psi_{E1} - \Psi_{HH1}$ energy separation corresponds to $\lambda = 1439$ nm for $F = 15$ kV/cm, and, similarly, the $\Psi_{E1} - \Psi_{LH1}$ energy separation corresponds to $\lambda = 1411$ nm. Considering these large energy separations and the fact that the high-energy asymmetric-mode excitons dominate the optical absorption above $F_{LH}$, the optical losses at 1550 nm should be small [5]. Also, localization of $\Psi_{HH1}$ in QW2, rather than in QW1, offers another important benefit. For the electric fields of interest, it is easier to confine $\Psi_{HH1}$ to QW2 than to QW1, so that the 3 Å thickness and 1% compositional variations considered below cannot redistribute the heavy-hole wave functions and cause sharp dips in the refractive index change curves for the TE polarization [3].

We study the effects of the thickness and compositional variations on structure #1 separately, with no intention to model any specific growth process. To do so, the thicknesses of QW1, QW2, and the middle barrier are changed by ±3 Å independently (i.e., 27 variations). For both polarizations, the refractive index change corresponding to each variation is multiplied by the variation's occurrence probability of $1/27$ and added in the average refractive index change for TE polarization ($\Delta n_{TE1}$) or TM polarization ($\Delta n_{TM1}$). This is equivalent to having $p_w = 1/3$ in [3]. Similarly, the InAs composition in
all five layers is changed by ±0.01 (i.e., 243 variations) and, using $p_c = 1/3$ [3], we obtain the average refractive index changes for each polarization ($\Delta n_{TE1}^C$ and $\Delta n_{TM1}^C$).

As illustrated in Fig. 6.3(a), structure #1 is quite insensitive to both thickness and compositional variations. Its insensitivity to compositional variations is, in part, due to the insensitivity of the light-hole band edge to these variations [3]. Also, the structure’s insensitivity to both thickness and compositional variations is, in part, due to the small valence-band discontinuity ratio of the InGaAs–InAlAs material system [4]. The confinement of the anticrossing light-hole wave functions to the quantum well layers is, thus, small and the light-hole wave functions are, in turn, less sensitive to the thickness and compositional variations that occur in these layers.

The band edge diagram and the wave functions for structure #2 are shown in Fig. 6.2(b). Here, it is $\Psi_{HH1}$ and $\Psi_{HH3}$ that are shown in the figure as they make the main contributions to the electrorefraction ($\Psi_{HH2}$ has negligible magnitude in QW1 and a node in QW2). The function of the small In$_{0.52}$Ga$_{0.20}$Al$_{0.28}$As barriers is to decrease the confinement of the anticrossing electron wave functions and decrease their sensitivities to the layer variations [4]. The large In$_{0.52}$Al$_{0.48}$As barriers are sufficiently far from QW1 and QW2 to significantly affect the sensitivities of the wave functions, and they help to confine the wave functions and decouple neighboring CQW structures. As shown in Fig. 6.2(b), the compressive strain in QW2 is used to make it deeper for $\Psi_{E1}$ and $\Psi_{HH1}$.
confining them for \( F = 15 \text{ kV/cm} \), while the tensile strain in QW1 is used to make it only slightly deeper for \( \Psi_{\text{LH1}} \), confining it for \( F = 15 \text{ kV/cm} \) and allowing it to move toward QW2 for larger \( F \). The wavelengths corresponding to the \( \Psi_{\text{E1}}-\Psi_{\text{HH1}} \) and \( \Psi_{\text{E1}}-\Psi_{\text{LH1}} \) energy separations are 1391 nm and 1312 nm, respectively. As \( F \) is increased to 30 kV/cm, \( \Psi_{\text{E1}} \) and \( \Psi_{\text{E2}} \) become approximately equally shared by QW1 and QW2 giving the largest heavy-hole exciton radii and the smallest refractive index for the TE polarization [4] [see Fig. 6.3(b)]. Simultaneously, \( \Psi_{\text{LH1}} \) becomes approximately equally shared by the two wells, also giving largest exciton radii and smallest refractive index for the TM polarization. However, unlike in the CQW structures mentioned above, here, both the conduction-band, \( i.e., \) electron, and the valence-band, \( i.e., \) light-hole, wave functions exchange wells as \( F \) is increased. Consequently, the overlaps between \( \Psi_{\text{E1}} \) and \( \Psi_{\text{LH1}} \) as well as \( \Psi_{\text{E2}} \) and \( \Psi_{\text{LH2}} \) reach their maxima for \( F \approx 25 \text{ kV/cm} \), and \( \Delta n_{\text{TM2}} \) does not have the smooth, negative slope typical for CQW structures. Rather, it is a nonlinear function [see Fig. 6.3(b)], and a desirable large difference between \( \Delta n_{\text{TE2}} \) and \( \Delta n_{\text{TM2}} \) is achieved.

As illustrated in Fig. 6.3(b), structure #2 is not very sensitive to 3 Å thickness variations (\( p_w = 1/3 \)), but it is somewhat sensitive to the compositional variations (\( p_c = 1/3 \)). Since structure #2 has more layers than structure #1, most of which are also quaternary compounds, only the variations in the quantum wells are considered in order to keep the number of simulations manageable. Simulations show that the thickness and the compositional variations in the barriers, as compared to the wells, have much smaller
effects on the distributions of the wave functions, which justifies the approximation.

Also, the effects of compositional variations are well approximated by restricting the changes of the Ga and Al mole fractions in each well to have the same magnitudes but opposite signs. Fig. 6.3(b) also shows the effect of treating the thickness and compositional variations as being coupled ($\Delta n_{\text{TE}2}^{TC}$ and $\Delta n_{\text{TM}2}^{TC}$).

Fig. 6.4(a) shows the effects that the layer variations have on $\Delta n_{\text{eff(TE)}}$ and $\Delta n_{\text{eff(TM)}}$ of the 1D waveguide in Fig. 6.4(b). $\Delta n_{\text{eff(TE)}}$ and $\Delta n_{\text{eff(TM)}}$ are obtained using the designed values for refractive index change curves ($\Delta n_{\text{TE1}}$, $\Delta n_{\text{TM1}}$, $\Delta n_{\text{TE2}}$, and $\Delta n_{\text{TM2}}$), biasing the electric field at $F_B = 23$ kV/cm, and applying an electric field change of $\Delta F = \pm 3$ kV/cm. The magnitudes of $\Delta n_{\text{eff(TE)}}$ and $\Delta n_{\text{eff(TM)}}$ are very similar, and polarization switching between two orthogonal states could be achieved for an electrode length of $L = 3.2$ mm. However, if for the same $F_B$, $\Delta F$, and $L$ we consider the effects of the layer variations on polarization modulation, Fig. 6.3 shows that the magnitudes of the effective index changes for the TE and TM polarizations ($\Delta n_{\text{eff(TE)}}$ and $\Delta n_{\text{eff(TM)}}$) become very different. Here, the actual variations that can be expected in the epitaxial layers are approximated by $\Delta n_{\text{TE1}}^{T}$ and $\Delta n_{\text{TM1}}^{T}$ in structure #1 and by $\Delta n_{\text{TE1}}^{TC}$ and $\Delta n_{\text{TM1}}^{TC}$ in structure #2. Due to the nonlinear shape of $\Delta n_{\text{TM2}}$, the magnitudes of the two effective index changes can be matched by changing the values of $F_B$ and $\Delta F$. In addition, if the long electrode is split into two equal-length electrodes ($L_1 = L_2 = 1.6$ mm), each having a different bias field.
Figure 6.4: (a) Effects of the layer variations on $\Delta n_{\text{eff(TE)}}$ and $\Delta n_{\text{eff(TM)}}$ in a (b) 1-dimensional waveguide containing 6 periods of structure #1 and 10 periods of structure #2. In each CQW region, $\Gamma_T$ and $\Gamma_M$ are the optical confinement factors for the TE and TM fundamental modes.

$F_{B1} = 20$ kV/cm and $F_{B2} = 27$ kV/cm) and the same field change $\Delta F = \pm 5$ kV/cm, not only would the effective index changes ($\Delta n_{\text{eff(TE)}}$ and $\Delta n_{\text{eff(TM)}}$) have closely matched magnitudes, but also the curvatures of the TM response would cancel themselves to an extent, making the TM response more linear [see Fig. 6.4(a)]. The nominal polarization switching efficiency in [2] is somewhat better than here, considering that the structures in [2] have smaller values for $\Gamma_T$ and $\Gamma_M$ ($\Gamma_T = 0.43$ and $\Gamma_M = 0.37$ for 10 periods of the old structure #1 and $\Gamma_T = 0.19$ and $\Gamma_M = 0.17$ for 6 periods of the old structure #2, respectively) and still provide a smaller $\Delta F \times L$ product (5 kV/cm $\times$ 3.5 mm). However, the new structures are more robust to the layer variations and provide for the possibility
of matching the magnitudes of $\Delta n_{\text{eff(TE)}}$ and $\Delta n_{\text{eff(TM)}}$ even in the presence of these variations.

References

Chapter 7
Summary, Conclusions, and Suggestions for Future Work

7.1 Summary

It was clear in the early stages of the research presented in this thesis that ER modulators based on CQW structures would be strong competitors to other modulator technologies in future-generation digital and analog optical links. For example, compared to SQWs, CQW structures can provide similar refractive index changes for considerably lower drive electric fields. In addition, the exciton absorption peaks in CQW structures exhibit smaller red shifts, so that ER modulators based on CQW structures are expected to have smaller absorption coefficients and electric-field-induced changes of the absorption coefficients at the wavelength of operation than ER modulators based on SQWs. Consequently, ER CQW modulators have great potential to exceed the performance of ER SQW modulators in applications requiring ultra-fast intensity modulation. The same is true for polarization modulators. Push-pull polarization modulators based on CQW
structures are expected to have ultra-wide electro-optic bandwidths, low drive voltages, low differential group delays, and small voltage-dependent changes in the absorption. When compared to EA SQW modulators, ER CQW intensity modulators are expected to have lower chirp and lower drive voltages. Also, as they operate at wavelengths that are further from the lowest energy exciton (i.e., they are more detuned) and, thus, absorb less light, the ER CQW intensity modulators are expected to have smaller temperature and wavelength dependences and higher optical saturation powers.

The thesis presents, in a chronological order, work aimed at improving the state-of-the-art of electro-optic modulators based on CQW structures. In Chapter 2, a design for the first quantum-well-based push-pull polarization modulator was presented. The conceptual push-pull polarization modulation was achieved by placing multiple repetitions of two different InGaAlAs–InAlAs CQW structures in the optical waveguide of the modulator. The electroabsorption in these CQW structures, and also in all of the InGaAlAs-based CQW structures designed in this thesis, was modeled by solving the 1S exciton equation in the effective-mass envelope-function approximation using the variational method, and the electrorefraction was obtained using the Kramers–Krönig relations. One of the two structures contains a small amount of tensile strain (TS structure) and provides a large increase of the refractive index for the TM polarization and only a small increase of the refractive index for the TE polarization. The other structure contains a small amount of compressive strain (CS structure) and provides a large decrease of the refractive index for
the TE polarization and only a small decrease of the refractive index for the TM polarization. The novel function of biaxial strain in each of the two structures was to achieve a large difference in the refractive index changes for the TE and TM polarizations. Placing 10 repetitions of the TS structure and 6 repetitions of the CS structure in a slab waveguide, similar-magnitude and opposite-sign changes of the effective refractive indices for the TE and TM modes were predicted for an electric-field change of 5 kV/cm, providing a 90° polarization rotation in a 3.4 mm long waveguide.

In Chapter 3, the sensitivities of the TS and CS structures to thickness and compositional variations were studied. Although the wave functions that contribute to the electrorefraction effects in CQW structures become less sensitive to the variations when the thicknesses of the middle barriers are decreased [1], doing so also decreases the slopes of the electric-field-induced refractive index changes [2]. The goal of the study in Chapter 3 was to obtain a better understanding of the TS and CS structures’ sensitivities to the layer variations, and, eventually, based on the knowledge obtained from the study, minimize the effects of the layer variations without resorting to very thin middle barriers. It was found that the CS structure is very sensitive to the layer variations because its electrorefraction effect is based on the anticrossing of the two lowest energy heavy-hole wave functions and that the TS structure is quite insensitive to the layer variations because its electrorefraction effect is based on the anticrossing of the two lowest energy light-hole wave functions. The effective masses of the heavy-hole wave functions are
considerably larger than those of the light-hole wave functions, and distributions of heavy-holes wave functions in CQW structures are, therefore, more susceptible to any thickness or compositional variations in the CQW structures [1]. Although the CS structure provides a very large change of the refractive index change for the TE polarization and a very small change of the refractive index change for the TM polarization, which is very desirable in polarization modulators, it was clear from the study that major improvements of the CS structures needed to be done because of their great sensitivities to the layer variations. It was also learned from the study that the TS structure was quite insensitive to the compositional variations because the energy of the light-hole band edge depends less on the compositional variations than do the energies of the heavy-hole and electron band edges. It was anticipated that the TS structure could be made very robust to the layer variations if slightly redesigned in order to prevent the undesirable anticrossing of the two lowest energy heavy holes, which caused undesirable dips in the refractive index response for the TE polarization.

In Chapter 4, inspired by the robustness of the TS structure, a lattice-matched InGaAs-InAlAs CQW structure (structure #1) that has it electrorefractive effect based on the anticrossing of the two lowest energy light-hole wave functions, and is, thus, more appropriate for TM modulation, was compared with a similar lattice-matched InGaAs-InAlAs CQW structure (structure #2) that has it electrorefractive effect based on the anticrossing of the two lowest energy electron wave functions, and is, thus, more
appropriate for TE modulation. It was demonstrated that structure #1 is considerably less sensitive to the 3 Å thickness variations and the 2 % compositional variations and that InGaAlAs-based CQW structures that have their electrorefraction effects based on anticrossing of the light holes are a preferable technology for the future ER modulators. Besides the insensitivity of the light-hole band edge to compositional variations, it was seen in this study that there was an additional mechanism which contributed to structure #1's small sensitivity to both thickness and compositional variations. It was shown that a small valence band discontinuity ratio in InGaAlAs-based systems makes anticrossing light-hole wave functions quite insensitive to relative differences in thickness and composition between the two quantum wells because shallow quantum wells provide only weak confinement to the light-hole wave functions. Consequently, the magnitudes of the light-hole wave functions in the quantum well layers are relatively small, and so are the probabilities that the relative distributions of the wave functions between the two quantum wells can be affected by the thickness and compositional variations in the two quantum wells.

In Chapter 5, building on the findings in Chapter 4, it was shown that decreasing the confinements of electron wave functions in CQW structures could be used to improve the robustness to growth of EA and ER modulators that have their respective electroabsorption and electrorefraction effects based on anticrossing of electron wave functions. A lattice-matched CQW structure (S_A) that has ternary wells (In_{0.53}Ga_{0.47}As)
and ternary barriers (In$_{0.52}$Al$_{0.48}$As) was compared to another lattice-matched CQW structure (S$_B$) that has ternary wells (In$_{0.53}$Ga$_{0.47}$As) and quaternary barriers (In$_{0.52}$Ga$_{0.24}$Al$_{0.24}$As). The middle barrier in S$_B$ was made wider than the one in S$_A$ in order to compensate for its smaller height and provide the same sensitivities of the lowest energy electron wave functions in the two structures to the same change in the electric field. Although the lowest energy electron wave function in S$_B$ has the same sensitivity to the electric field as the lowest energy electron wave function in S$_A$, it is considerably less sensitive to the 3 Å thickness variations and only slightly more sensitive to the 10 meV potential energy variations that can be expected to occur in the quantum well and barrier layers during growth. Consequently, increasing the thicknesses of the middle barriers in CQW structures and decreasing the confinements of the anticrossing electron wave functions by decreasing the potential energies of all barriers (or increasing the potential energies of the quantum wells) can be used as a design method for improving the overall robustness to growth in these structures. The same is true for the CQW structures where the anticrossing of the light-hole wave functions is used. However, as was shown in Chapter 3, anticrossing of the heavy-hole wave functions should be avoided because their large effective masses make them extremely sensitive to layer thickness and compositional variations.

In Chapter 6, the design method presented in Chapter 5 was used to improve the performance of the CS structure in Chapters 2 and 3. Although it is designed to achieve
the same effect as the CS structure, i.e., large electric-field-induced decrease of the refractive index for the TE polarization without a commensurate decrease of the refractive index for the TM polarization, the new structure (structure #2) has two important characteristics that distinguish it from the original CS structure.

First, the large refractive index change for the TE polarization and the small refractive index change for the TM polarization in structure #2 are achieved via anticrossing electron wave functions, rather than heavy-hole wave functions. The small effective masses of the anticrossing electron wave functions in structure #2 make them considerably less sensitive to layer thickness and compositional variations than the anticrossing heavy-hole wave functions in the CS structure. However, the large refractive index change for the TE polarization and the small refractive index change for the TM polarization is an effect that is not easily achieved via anticrossing electron wave functions. The large negative change of the refractive index for the TE polarization is achieved by anticrossing the two lowest energy electron wave functions and preventing the heavy-hole wave functions from making any significant electric-field-induced redistribution between the two wells of structure #2, as is typically done in ER CQW modulators [2], [3]. However, in order to achieve only a small change of the refractive index for the TM polarization, considering that the anticrossing of the electron wave functions is used, a small, controllable redistribution of the two lowest energy light-hole wave functions is allowed. The redistribution of the light-hole wave functions
accompanied by a lack of redistribution of the heavy-hole wave functions is facilitated by using tensile strain in the left-hand side well and compressive strain in the right-hand side well. The opposite-sign strains provide unequal potential energies for the heavy-hole and light-hole wave functions, strongly confining the heavy-hole wave functions and allowing the light-hole wave functions to slowly redistribute between the two wells. The electric-field-induced movement of the light-hole and electron wave functions does not provide the typical monotonic decrease or increase of the overlap integrals between these wave functions. Rather, the overlap integrals have an "S-shape" dependence on the electric field, which is also evident in the refractive index change for the TM polarization. Consequently, the refractive index change for the TM polarization remains small in the electric field region of interest.

Second, unlike the CS structure, the new structure #2 has very small quaternary barriers in the vicinity of two quantum wells in order to decrease the confinement of the anticrossing electron wave functions and, ultimately, improve the structure's sensitivity to the layer variations. Simulations show that the heights of the barriers far from the quantum wells, where the magnitudes of the electron wave functions are small, do not affect the wave functions' sensitivities to the layer variations. Consequently, the barriers in these regions are made ternary in order to provide better decoupling between the neighboring structures and to provide confinement to the second lowest energy light-hole
wave function and the third lowest energy heavy-hole wave function, both of which are included in the modeling of electrorefraction.

Structure #1 in Chapter 6 is not fundamentally different from the TS structure in Chapters 2 and 3. Similar to the TS structure, the main function of structure #1 is to provide a large increase of the refractive index for the TM polarization without a commensurate increase of the refractive index for the TE polarization, and this effect is achieved by anticrossing the two lowest energy light-hole wave functions. However, in structure #1, the lowest energy heavy-hole wave function is confined to the right-hand side well and not the left-hand side well. This configuration is more energetically favorable for the heavy holes, and the undesirable heavy-hole anticrossing evident in Chapter 3 is extinguished for the 3 Å thickness and 1 % compositional variations used in Chapter 6. Also, confining the lowest energy heavy-hole wave function to the right-hand side well in the electric field region of interest decreases the optical absorption strength associated with the lowest energy electron-heavy-hole transition (E1–HH1) and effectively decreases the optical loss for the TE polarization at the wavelength of operation. In addition, tensile strain is used in both wells of structure #1 in order to increase the wavelength detuning of the heavy-hole excitons, which typically have lower energies than the light-hole excitons, and to further decrease the optical loss for the TE polarization. The compressive strain in the barriers of structure #1 is used to balance the overall strain in structure #1 and structure #2. Although structure #1 is very insensitive to the 3 Å thickness and the 1 %
compositional variations, structure #2 still shows a certain degree of sensitivity to the compositional variations. However, it is pointed out in Chapter 6 that two inline, separately biased electrodes can be used to match the magnitudes as well as to linearize the opposite-sign refractive index changes for the TE and TM polarizations, further reducing the sensitivities of modulators based on structure #1 and structure #2 to layer variations.

7.2 Conclusions

As mentioned above, CQW structures have the potential to provide large electroabsorption and electrorefraction effects, which will allow devices using them to have short lengths and, consequently, ultra-wide electro-optic bandwidths, while maintaining small drive voltages. Also, unlike in SQWs, in which the electrorefraction effect is based mainly on red shifting the lowest energy excitons, in CQW structures, the electrorefraction effect is based on changing the overlaps between the conduction and valence wave functions, and there is no appreciable red shifting that causes electric-field-induced increases of the optical absorption. Besides these two benefits of CQW structures, the work presented in this thesis reveals at least four additional properties of CQW structures that will be important when designing future CQW modulators.
First, as the electrorefraction effect in a CQW structure is based on the electric-field-induced transfer of particles (electrons, light holes, or heavy holes) between the two wells, it is relatively easy to select which particles are allowed to transfer by manipulating the strain and geometry of the layers in the CQW structure. Consequently, CQW structures can provide for efficient polarization modulators because, again, electron-light-hole transitions solely contribute to the TM-polarization response and electron-heavy-hole transitions dominate the TE-polarization response.

Second, in InGaAlAs-based CQW structures, because of the very small dependence of the light-hole band edge on compositional variations in the quantum wells, because of the relatively small effective masses of light holes, and because of the small valence band discontinuity ratio, the anticrossing light-hole wave functions are far less sensitive to layer thickness and compositional variations than the anticrossing electron or heavy-hole wave functions. Consequently, an InGaAlAs-based CQW structure can be made to be quite sensitive to the electric field, by allowing the middle barrier to be fairly thick, and still remain quite insensitive to the layer thickness and compositional variations that are expected to occur during the growth process. As the light-hole momentum matrix element for the TM polarization is considerably larger than that for the TE polarization, CQW structures that utilize anticrossing of light-hole wave functions are suitable for TM phase and intensity modulators, such as structure #1 in Chapter 4, or polarization modulators, such as structure #1 in Chapter 6. Therefore, if the designers of future phase
and intensity modulators desire to use TM light in their devices, the best choice for these devices would be simple lattice-matched, ternary InGaAs–InAlAs CQW structures, which utilize the anticrossing of light holes (such as structure #1 in Chapter 4). In addition, if the designers want to make very efficient polarization modulators that are not necessarily push-pull devices, the best choice for these devices would be simple strained, ternary InGaAs–InAlAs CQW structures, which utilize the anticrossing of light holes (such as structure #1 in Chapter 6).

Third, certain devices, such as surface-normal modulators used in optical interconnects, free-space optical communications, and optical links requiring large-area and/or polarization insensitive devices, do not have optical waveguides. For example, in the surface-normal electroabsorption modulator in [4], light enters the stack of InGaAs–InAlAs CQW structures through a p-doped region at normal incidence and, thus, its electric-field vector is parallel to the planes of the quantum wells. This device is polarization-independent because the CQW structures provide the same electroabsorption effect for all directions of the electric-field vector around the optical axis. For this device and other devices requiring modulation of plane-parallel light, the anticrossing of electrons is a more efficient mode of operation than the anticrossing of light holes because the light-hole momentum matrix element for the plane-parallel light is relatively small. Of course, the anticrossing of electrons in a CQW structure is more efficient than the anticrossing of light holes only if the CQW structure can be designed so that the
electron wave functions are not significantly more sensitive to the layer thickness and compositional variation than the light-hole wave functions. Chapter 5 presents a method that designers of devices that modulate the plane-parallel light can use to make CQW structures based on the anticrossing of electrons more robust to the layer variations. The method requires barriers or quantum wells in CQW structures to be quaternary in order to weaken the confinement of the electron wave functions to the quantum well layers and allow them to tunnel to a greater extent into the external barriers. As argued in Chapter 5, the small increase of the wave functions' sensitivities to the compositional variations in the barriers is small compared to the large decrease of their sensitivities to both the thickness and compositional variations in the quantum well layers.

Fourth, as mentioned above, the CQW structures that utilize the anticrossing of light-hole wave functions, such as structure #1 in Chapter 6, can be used in polarization modulators because these structures provide large phase changes for the TM polarization, accompanied by only small phase changes for the TE polarization. On the other hand, for those applications that may require devices that provide large phase changes for the TE polarization accompanied by only small phase changes for the TM polarization, a CQW structure similar to structure #2 in Chapter 6 could be used. Again, in Chapter 6, the structure #2 was used together with structure #1 for a particular purpose, which is a realization of a robust CQW push-pull polarization modulator.
7.3 Suggestions for Future Work

In order to fully realize the potential that the CQW structures developed in this thesis have for improving the state-of-the-art in optical modulators, additional work will be necessary. This future work will include: (a) Growth and fabrication of CQW modulators, (b) Systematic performance tests of these devices, (c) Improvement of their electro-optic bandwidth, and (d) Integration of CQW modulators with other devices. Compared to the polarization modulators that could be realized using the CQW structures in Chapter 6, TM-phase modulators that could be realized using the robust structure #1 in Chapter 4 are the simplest to build and are the most likely to provide good results in the short term. Therefore, initial future research should likely focus on TM CQW modulators.

(a) Multiple repetitions of the CQW structure could be grown using Molecular Beam Epitaxy in a typical Mach–Zehnder p-i-n diode configuration, as illustrated in Fig. 1.17. The shape of the optical waveguide could be patterned using reactive ion etching. Each wafer can contain many Mach–Zehnder interferometers with 1–2 mm long branches. In order to avoid Fabry-Perot resonances, the optical waveguide facets could be angle-cleaved or antireflection coated.

(b) Mach–Zehnder interferometers containing multiple repetitions of the CQW structure should be tested for their basic operation, and their low-frequency electro-optic transfer
functions should be obtained. Extinction ratios greater than 15 dB and drive voltages lower than 1 V are expected. Should more details of the electroabsorption and the electrorefraction properties of the CQW structures be required (e.g., in order to compare the experimental results with the modeling), the photocurrent spectra of single branches of the Mach–Zehnder interferometers could be obtained. The single-branch experiments may also include more detailed phase and absorption measurements [5]. All measurements should be performed across the communication wavelength bands using a tunable laser, and the modulator is expected to show a flat response at least across the C-band. More than one modulator design will likely be needed to cover the whole telecommunication spectrum.

(c) Once the basic functionality and moderately wide electro-optic bandwidths of the p-i-n devices are demonstrated, additional work should be focused on the design, fabrication, and testing of the traveling-wave electrodes that will provide ultrahigh bandwidths (~100 GHz). These electrodes will not necessarily be of the typical p-i-n diode configuration. They may be coplanar strip or coplanar waveguide electrodes with Schottky contacts [6], or the new type of substrate-removed microstrip-like electrode recently introduced [7], [8].

(d) In order for CQW modulators to be competitive in future optical links, it will also be important to eventually integrate them with other devices (e.g., lasers, photodetectors,
wavelength converters, optical amplifiers, etc.) on a single chip. The monolithic integration of several optoelectronic devices on a single chip reduces the cost of packaging, reduces the coupling losses between devices, reduces the power consumption, and improves the circuit reliability. How the integration will be achieved will depend on the photonic integrated circuit of interest [9].

Growth, fabrication, and testing procedures for the TE-polarization intensity modulators will be basically the same as those for the TM-polarization modulators. As CQW polarization modulators contain multiple repetitions of two types of CQW structure, each type of CQW structure should be grown, fabricated, and tested separately in procedures similar to the ones described above. Only when the electroabsorption and the electrorefraction properties of each type of CQW structure are well known, should the two structures can be put together in the optical waveguide of a polarization modulator for further optimization and testing. Also, if a polarization modulator is not intended to be used in the push-pull mode of operation, the device can be based on only one for the two structures presented in Chapter 6, e.g., structure #1. Although the CQW polarization modulators based on the strained structures presented in Chapter 6 are more difficult to realize than the TM-phase modulators based on structure #1 presented in Chapter 4, both types of device are expected to provide state-of-the-art performance predicted by the modeling.
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