Access Control in XML PDMS Query Answering
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Abstract

Peer data management system (PDMS) is a decentralized system, in which each peer is autonomous and has its own schema and database. With the help of pairwise schema mapping built between any two relevant peers, a query at one peer can be rewritten and broadcast to the whole PDMS. Then answers from multiple peers are returned to the querying peer. In our thesis, we exploit the access control issues in the query-answering process of the XML PDMS. We propose a formal syntax for access control policy (ACP) to specify the fine-grained access control privileges on peers' local XML database. We also design several query-answering algorithms that aim to handle access control in the PDMS, define the algorithm properties of Information Leakage Free and Completeness, and analyze every designed query-answering algorithm on the two properties. A comprehensive cost model, which consists of the major tasks and primitive operations, is proposed by us to assess the query-answering algorithms. We implement the designed query-answering algorithms, compare their running time, and test the scalability in different facets.
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Chapter 1

Introduction

The peer data management system (PDMS) is emerging as a flexible distributed data management architecture. Moreover, with the significant increase of web data, XML is now used as the underlying data model of peers in a PDMS. However, the existing PDMS research has paid little attention to the access control requirement in each peer for its database, which might greatly affect the query-answering process in a PDMS. The access control issues in an XML PDMS will be explored in our thesis.

In this chapter, we first introduce the background knowledge of PDMS, XML, and XML queries (Section 1.1), then motivate our work by a concrete example (Section 1.2). Section 1.3 concisely states the access control problem in an XML PMDS. Our main contributions are summarized in Section 1.4.

1.1 Background

In this section, we introduce the background knowledge of our work: peer data management systems, XML and XML queries.

A peer data management system (PDMS) is a distributed database management system based on a peer-to-peer architecture. Each node in a PDMS is called a peer. A peer is autonomous, has its own database and schema. A peer can join and leave the PDMS dynamically. Unlike the data integration system, there is no server playing the central-control role in a PDMS. If two peers are considered to be similar, one of their administrators builds a mapping between the database schemas of the two peers. Such peers are called acquaintances. Thus, the topology of a PDMS is an arbitrary connected graph, in which each edge is such a pairwise mapping. A query can be put forth at any peer. The query is first evaluated at the peer’s local database, then it is passed to each of its acquaintances. When the query is passed to each acquaintance, the mapping is used to translate the query into a new query over the acquaintance’s schema. Similarly, it is then passed to all acquaintances of all those acquaintances and
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thus broadcast to the whole PDMS. Finally the answers at every relevant peer is returned to the querying peer.

As an illustration, Figure 1.1 shows a simple PDMS with four peers: Vancouver General Hospital, Montreal General Hospital, Boston General Hospital, and Toronto General Hospital. In this example, Toronto General Hospital is an acquaintance of Boston General Hospital, so a mapping is built from Toronto General Hospital Schema to Boston General Hospital Schema (the mapping is denoted by an arrow from Toronto General Hospital Schema to Boston General Hospital Schema). Similarly, other pairwise mapping are built between peers. When a query $Q$ is put forth at Toronto General Hospital, it is first evaluated locally. Then $Q$ is rewritten into $Q'$ according to the mapping from Toronto General Hospital Schema to Boston General Hospital Schema. $Q'$ is sent to Boston General Hospital and evaluated there. The answer of $Q'$ is routed back to Toronto General Hospital. By this way, rewritten queries are broadcast in the whole PDMS, and the answer from each hospital is returned to Toronto General Hospital.

XML (eXtensible Markup Language) currently is the W3C recommendation for publishing electronic data on the web. Nowadays, it is the de facto standard for web documents and data storage. An XML document is plain text interleaved with some markup, which divides the document content into character data, container elements, and attributes of the elements. There is one and only one root element in an XML document. Sub-elements are embedded within an element. Thus, an XML document is modeled as a tree structure, in which each node is an element or a character string. Normally, an XML document is
accompanied with an XML Schema, which fully specifies the structure and data type information for this document. Therefore, XML can be used as databases for peers in a PDMS. Mappings are built between schemas of XML databases residing on acquaintances.

The standard query form for XML databases is XQuery. XPath is the main functional structure of XQuery, and it is the syntax to accurately address parts of an XML document. An XPath is a path expression for a sequence of steps from one node to another node. In each step, there are three components: (1) axis specifier: '/' denotes child, '//' denotes descendant, '@' denotes attribute, etc; (2) node test: 'comment()' denotes a comment node, 'text()' denotes the text value of a node, etc; (3) predicate: a mathematic expression put in a square bracket as a filter. Predefined operators can also be used in XPath, such as '|' denoting the union of two node sets. As the first example, the XPath expression “publication//paper/*[@id='001']” selects the element, whatever its name (*), if its id attribute value of '001', who is a child ('/') of a paper element that itself is a descendant ('//') of a publication element. As a more concrete example, the Xpath expression “publication//paper/author/text()='Rachel Pottinger'” selects the paper element, if it is a descendant ('//') of a publication element and has an author child element ('/') whose text content ('text()') is Rachel Pottinger. This Xpath expression retrieves the full paper list for Rachel Pottinger. XPath queries can be categorized into several fragments according to whether including '/', '//', '[ ]', '*', '|'. Schema or DTD (another type of XML schema). In this thesis, we concentrate on the XPath fragment only with '/', '//', '[ ]'. For instance, our second XPath example “publication//paper/author/text()='Rachel Pottinger'” belongs to this XPath fragment.

The tree pattern is the key construct for modeling XPath. A tree pattern includes two components: (1) a tree, in which the nodes are labeled with variables, (2) a set of formulas, which are constraints on the tree nodes and their properties (i.e. tags, attributes, contents). The tree has two types of edges: pc (parent-child) edges and ad (ancestor-descendant) edges, which correspond to '/' and '//' in XPath.
1.2 Motivation and Challenges

As a flexible data management environment, a peer data management system is suitable for many applications, such as the public medical institutions, the international company management, and the insurance system, etc. For example, a public medical institution environment may consist of several hospitals, healthcare centers, the Ministry of Health, and emergency units. Each institution is independent, has its own database and share the data across the web. Quite often these institutions need to collaborate. For instance, when a patient is transferred between hospitals, the patient's medical history needs to be shared. Probably there is no global schema for all the hospitals, so a data integration system does not help. A PDMS is useful at this time. With the help of the pairwise schema mapping, the patient's illness history can be easily transferred from one hospital to another one. Furthermore, a query asking for one patient's information can be put forth at a peer and broadcast in the whole PDMS, and results will be retrieved from every relevant peer.

Although the existing PDMS projects [13, 35, 37, 40] can handle the problems of schema mapping and query rewriting, they do not effectively take into account the access control requirements of peers, i.e., all the data on each peer is public for other peers. This is not true for a realistic application. Because a peer is autonomous, it has the requirement to define access control privileges on its database, i.e., which peers have the right to access a specific part of its database. For example, a hospital may only allow other hospitals to access the illness history of a patient, but forbid any institution to access the personal information of a patient. Such access control requirements are so common in today's database management systems that they should not be ignored in a realistic PDMS. When access control exists in a PDMS, security problems will arise. The existing query-answering algorithm does not work well in this case.

Let us observe a concrete example. It is shown in Figure 1.2. There are four peers in the XML PDMS: Vancouver General Hospital, Montreal General Hospital, Boston General Hospital and Toronto General Hospital. The schemas for their XML databases are shown in the figure. The pairwise mappings of their schemas are denoted by dash arrows. For simplicity, we call the four peers Vancouver General Hospital, Montreal General Hospital, Toronto General Hospital and Boston General Hospital separately as 'vg', 'mg', 'tg' and 'bg'. And the database residing on each peer is 'vg.xml' for 'vg', 'mg.xml' for 'mg', 'tg.xml' for 'tg', 'bg.xml' for 'bg'. The possible message routing paths are denoted by
Figure 1.2: Motivation Example for Access Control in an XML PDMS
Chapter 1. Introduction

Suppose a query “retrieve the illness history of Mary Smith” is put forth at 'vg', rewritten according to schema mappings, and broadcast to the PDMS. Let us treat ‘tg’ as the current answering peer. The rewritten query is evaluated on ‘tg.xml’ to get the ‘Event’ elements for Mary Smith. If ‘tg’ does not specify any access control on its database, i.e. any peer can access all the data of ‘tg.xml’, the answer can be routed back to ‘vg’ via either the path “tg — mg —> vg” or the path “tg — bg —> vg”. This is the existing query-answering algorithm. The case with access control may be different. Suppose in our scenario, ‘mg’ and ‘tg’ do not have a collaboration relationship such that ‘tg’ specifies the access control of forbidding ‘mg’ to access any information on it. Thus, the answer for the query “retrieve the illness history of Mary Smith” at ‘tg’ can not be routed via the path “tg — mg —> vg”. Otherwise, information leakage will arise, i.e., ‘mg’ will see data that it is forbidden to access by ‘tg’. The answer can only be routed via the path “tg — bg —> vg”. From this example, we see that the access control requirements of peers affect the PDMS query-answering process. Furthermore, access control on a peer database can be more fine-grained and complicated than the previous example, especially when XML is the data model. What is the impact of access control on the PDMS query-answering process is still unknown according to existing research work.

The major challenges we are faced with in a XML PDMS with access control include: (1) How can we specify the access control requirement for a peer’s XML database, which is fine-grained and expressive enough? (2) What is the semantics of PMDS query-answering with access control? (3) What kind of algorithms can be used for the PDMS query-answering process? (4) What is the security property of these algorithms? (5) How to build a rational cost model and assess the algorithms using this model? All these challenges will be tackled in this thesis.

1.3 Problem Statement

A peer in a realistic peer data management system probably has access control requirement on its own database. Therefore, a precise syntax for specifying a access control requirement is necessary for an XML PDMS. Furthermore, in a PDMS with access control, a naive query-answering algorithm no longer works in terms of the security issue. Thus, new query-answering algorithms
need to be designed, theoretically ensuring no information leakage and other good properties. A cost model is also required to assess any query-answering algorithm for an XML PDMS.

1.4 Contributions

The following contributions are made in this thesis:

- We propose a formal syntax for the Access Control Policy (ACP), which is fine-grained and expressive enough for specifying the access control privilege on the XML database of a peer in the PDMS. Semantics of PDMS query-answering with ACPs is also presented. (Chapter 3)

- We divide a query-answering algorithm into two parts: a (query transmitting) Strategy and an (answer routing) Option. Several strategies and options have been designed to handle the access control requirements in PDMS. (Chapter 4)

- Some novel algorithms in the strategies and options, such as (i) query rewriting algorithm in light of ACPs (ii) safe peer list finding algorithm (iii) annotating and partitioning algorithm, are presented. (Chapter 7)

- As important properties, Information Leakage Free and Completeness for an (Strategy, Option) pair are formalized. We propose the sufficient and necessary condition for the two properties, and analyze these properties for every (Strategy, Option) pair designed. (Chapter 5)

- We build a comprehensive cost model, which includes the major tasks and the corresponding primitive operations and cost units. The cost model is used to assess the (Strategy, Option) pairs designed. (Chapter 6)

- We experiment on the designed (Strategy, Option) pairs, compare their execution speed, and test the scalability in terms of ACP amount per peer, database size, etc. (Chapter 8)

1.5 Thesis Outline

The remaining of the thesis is organized as follows. Chapter 2 reviews related works on peer data management system (PDMS), query containment, and access
control on XML documents. In Chapter 3, we present the general access control problem in the XML PDMS, the formal definition of Access Control Policy (ACP), and the semantics of PDMS query-answering with ACPs. In Chapter 4, we divide a query-answering algorithm into two parts—a strategy and an option. Several strategies and options, which can handle access control, are also designed there. Chapter 5 presents the formal definitions of IL-free and completeness, the sufficient and necessary condition for each of them, and the analysis result for all \( (Strategy, Option) \) pairs designed. In Chapter 6, we propose a comprehensive cost model that is used to assess all \( (Strategy, Option) \) pairs. In Chapter 7, some novel algorithms adopted in our strategies and options are elaborated and illustrated in detail. Chapter 8 is the experimental study for algorithm comparison, algorithm scalability, etc. Finally, our conclusions are stated in Chapter 9, along with the future work.
Chapter 2

Related Work

As described in Chapter 1, the work of the thesis concentrates on the access control scheme of the XML peer data management system. Peer data management system (PDMS) is the network environment we are working in; access control is the main issue we are researching on; and query containment is a necessary theoretical tool to design the query writing algorithm in the PDMS query-answering process and to ensure the algorithm correctness.

Therefore, in this chapter we will summarize the previous research work on peer data management system (Section 2.1), query containment (Section 2.2) and access control on local XML documents (Section 2.3).

2.1 Peer Data Management System (PDMS)

Data integration systems have been researched and adopted in academia and industry for a long time [5, 8, 16, 22, 28, 29, 30, 31]. They work well for sharing information in a specific domain. However, data integration is faced with a big problem: it requires to predefine a mediated schema before all nodes can share information. Thus the mediated schema has become a bottleneck in a data integration system.

Recently, the idea of a peer data management system (PDMS) [23] has emerged as a step beyond data integration systems. A PDMS is a distributed database management system based on a peer-to-peer architecture. In such a system, each web node is an autonomous peer and has its local database management system. The PDMS satisfies the need to have a decentralized, loosely-coupled data management environment, in which any web node can have different data model and contribute data, schema or mappings among schemas. Unlike data integration systems, a PDMS does not require a central control server or a global schema. Instead, mappings are constructed between the schemas of any two related peers.

A simple example can help to understand the difference between data in-
Chapter 2. Related Work

Figure 2.1: Data Integration System Example

Figure 2.2: PDMS Example

...integration system and PDMS. It is a scenario about sharing database research-related data that is used in the Piazza project [40]. The data integration system is shown in Figure 2.1, and the PDMS having the same functionality is shown in Figure 2.2. The schema and database of each independent node are put in a dotted frame. An arrow denotes a mapping from one schema to another schema. The data integration system is a tree-based hierarchy, in which the Mediated Schema is the root node and all other machines are the leaf nodes. There exists a mapping from the Mediated Schema to each node schema (e.g. UPenn Schema). Any query can only be put forth to the Mediated Schema, rewritten into some sub-queries (according to the schema mappings) and distributed to each leaf node (i.e. Princeton peer, UPenn peer, UW peer, Stanford peer and Berkeley peer). The sub-queries are evaluated at each leaf node, then the answers are returned to the root node. On the other side, the PDMS is an arbitrary connected graph of nodes/peers. There is no such a peer who holds a global mediated schema. Mappings are built between the schemas of any two relevant peer (e.g. the mapping from Stanford Schema to Berkeley Schema). A query can be put forth at any peer. Besides evaluated at the local database, the
query is rewritten into new queries with the help of the schema mappings and broadcast in the PDMS. Answers from every peer will be returned to the querying peer. For example, if a query $Q$ is put forth at Stanford peer, $Q$ is firstly evaluated at Stanford Database. Meanwhile, $Q$ is rewritten into $Q'$ according to the mapping from Stanford Schema to Berkeley Schema, sent to Berkeley peer and evaluated there. $Q$ is also rewritten into $Q''$ and sent to UW peer. By this way, the original query $Q$ is broadcast in the whole PDMS. All answers will be returned to Stanford peer in the end.

In the following, We will analyze some important PDMS projects.

Piazza [23, 24, 40] is a classic PDMS using XML as the peer data model. Because each peer may have a different schema, Piazza provides a pairwise schema mapping language similar to XQuery [12] and a query reformation algorithm for rewriting queries between peers. Piazza recognizes and motivates the access control as an important problem for a PDMS, but the only solution to the problem is a description of general plans to use encryption to enforce security. The details of this approach were left as future work.

The Hyperion project [37] is relational database-based PDMS. Hyperion builds and manages the mapping tables between peers at run time. And both schema-level and data-level mappings are supported. Hyperion’s emphasis is query answering among heterogeneous peers, and it doesn’t address access control or security issues.

HePToX [13] is a PDMS prototype using XML as peers’ underlying databases. Peers are heterogeneous. HePToX emphasizes on semi-automatically generating Datalog-like mapping rules and the efficient query translation algorithm. Access control issue is not considered in HePToX.

PeerDB [35] is an interesting system. The underlying database for each peer is a relational database system. However, there is no mapping between peer schemas. Instead, PeerDB uses the Information Retrieval (IR) technique to retrieve answers from different peers. Thus, PeerDB is a combination of database and IR systems. No access control issue is discussed in PeerDB.

As a conclusion, we see that the existing typical PDMS systems have not studied the access control problem, although some of them have recognized it as an important issue for a realistic PDMS. That is the work we will exploit in this thesis.
Chapter 2. Related Work

2.2 Query Containment

As we mentioned at the beginning of this chapter, query containment will be used as a theoretical tool to design our query rewriting algorithm in the PDMS query-answering process. Intuitively speaking, when a query \( Q \) is rewritten into a new query \( Q' \) in light of an access control rule \( R \), it must ensure that the answer of \( Q' \) is contained by both the answer of \( Q \) and the answer of \( R \). That is why query containment is important for our work.

Query containment problem was firstly exploited for conjunctive queries. Conjunctive Query (CQ) is put forth by A.K. Chandra and P.M. Merlin [15]. A Conjunctive Query is defined as a datalog rule \( H \leftarrow G_1,...,G_n \), where \( H \) is the head, the right side hand is the body and \( G_i(i = 1..n) \) are relations, which are referred to as subgoals. The answer for a conjunctive query \( Q \) evaluated on a relational database \( D \) is denoted as \( Q(D) \). In more details, \( Q(D) \) is the set of the head got by performing a possible value substitution for variables in \( Q \), where the substitution turns every subgoal of \( Q \)'s body into a tuple in \( D \).

Example 2.1 \( p(X, Y) \leftarrow a(X, W), b(W, Z), c(Z, Y) \) is a conjunctive query \( Q \). Specifically, it states the following. The body describes the relations \( a, b, \) and \( c \). The re-use of variables indicates that the values must be the same. So the body specifies that the second attribute of \( a \) must equal the first attribute of \( b \), and that the second attribute of \( b \) must equal the first attribute of \( c \). For each set of tuples that satisfy the body requirement, the head is instantiated. In this case, a new tuple of relation \( p \) is created, and the attributes of \( p \) are given the values of \( X \) and \( Y \) from the body. E.g., given a database \( D \), there are three relational tables \( a, b, \) and \( c \) in it. In \( a \), there is one tuple \((x_1, w_1)\); In \( b \), there is one tuple \((w_1, z_1)\); In \( c \), there is one tuple \((z_1, y_1)\). Then for the substitution \( \{X = x_1, Y = y_1, Z = z_1, W = w_1\} \), each subgoal in the body of \( Q \) is a tuple in the database \( D \). Thus, the instantiated head \( p(x_1, y_1) \) is in \( Q(D) \).

Give the definition of CQ and the meaning of a CQ evaluated on a database, CQ Containment can be defined as:

\[
\text{Let } Q_1 \text{ and } Q_2 \text{ be two CQs. } Q_1 \subseteq Q_2 \iff \forall \text{ database } D: Q_1(D) \subseteq Q_2(D).
\]

There are two classic approaches to test CQ containment: (1) containment mapping, (2) canonical database. Containment Mapping can be defined as:
Chapter 2. Related Work

$Q_1$ and $Q_2$ are CQs, where $Q_1 : \text{head}_1 \leftarrow \text{sg}_1, ..., \text{sg}_k$ and $Q_2 : \text{head}_2 \leftarrow \text{SG}_1, ..., \text{SG}_m$. Then a containment mapping is a function $\mu : \text{vars}(Q_2) \rightarrow \text{vars}(Q_1)$ such that (1) $\mu(\text{head}_2) = \text{head}_1$, (2) $\forall i : \mu(\text{SG}_i) = \text{sg}_j$, for some $j$.

If $Q_1$ and $Q_2$ are CQs, then $Q_1 \subseteq Q_2$ iff there exists a containment mapping $\mu : \text{vars}(Q_2) \rightarrow \text{vars}(Q_1)$.

Example 2.2 We have two CQ's: $Q_1 : p(X, Z) \leftarrow a(X, W), b(W, Z)$ and $Q_2 : p(X, Z) \leftarrow a(X, W), b(Y, Z)$. There exists a mapping $\mu$ from $\text{vars}(Q_2)$ to $\text{vars}(Q_1)$: $W \rightarrow W$, $X \rightarrow X$, $Y \rightarrow W$, $Z \rightarrow Z$. $\mu$ makes the mapped head of $Q_2$ as $p(X, Z)$, which equals the head of $Q_1$. For $Q_2$'s subgoals, we see that $\mu(a(X, W)) = a(X, W)$, which is a subgoal in $Q_1$'s body, and $\mu(b(Y, Z)) = b(W, Z)$, which is a subgoal in $Q_1$'s body. Thus $\mu$ is a containment mapping from $Q_2$ to $Q_1$, then $Q_1 \subseteq Q_2$.

Canonical Database method is to build a small number of databases $D_1, ..., D_n$, such that $Q_1 \subseteq Q_2$ iff $Q_1(D_i) \subseteq Q_2(D_i)$, where $i = 1, ..., n$. This method is not used in our work, so we do not illustrate it here. For more details, please refer to [41].

The CQ containment problem has been recognized as NP-complete in [15]. Much attention have been devoted to finding special classes of queries that admit polynomial time algorithms for containment and minimization[6, 7, 11, 17, 26, 27, 43].

With the popularity of XML query applications, query containment research expands from CQs to XML queries. XQuery [12] is recognized as the XML query standard. But it provides too many supportive structures, such as the FLWOR expressions and constructos. To avoid being distracted by these supportive structures, researchers have concentrated on XPath and its equivalent representation Tree Pattern, which is the main functional structure of XQuery. The concept and approaches for CQ containment have evolved to the work for containment of XPath queries (or tree patterns). The difference of XPath containment from CQ containment is that the query structures are trees and the queries may have recursions.

The semantics of XPath containment is exactly the same as that of CQ containment. Existing approaches for checking CQ containment work for XPath query containment as well, but after some extension. The canonical model
(database) technique [19, 32, 33], the homomorphism (containment mapping) technique [9, 20, 33, 36, 42] are widely used in the complexity analysis and algorithm design of XPath containment. For example, homomorphism is formally redefined for tree pattern containment in [20]:

"A homomorphism $h$ from a pattern $q$ to a pattern $p$ is a total mapping from the nodes of $q$ to the nodes of $p$ such that: (1) $h$ preserves node types (i.e. $\forall u \in N_q : \lambda_q(u) \neq ' $ $\Rightarrow \lambda_q(u) = \lambda_p(h(u))$, where $u$ is a node in $q$, $N_q$ is the node set of $q$, and $\lambda()$ is the function to find a node tag); (2) $h$ preserves structural relationships (i.e. whenever $v$ is a child (resp. descendant) of $u$ in $q$, $h(v)$ is a child (resp. descendant) of $h(u)$ in $p$)."

Checking query containment for many XPath fragments has been verified to be extremely hard. Fortunately, for some XPath fragments we can still find polynomial time algorithms. All the complexity results for containment of different XPath fragments are summarized in [38]. As mentioned in Section 1.1, in the thesis we deal with an XPath fragment only with '/', '//', '[ ]', which is shown in [38] to have a polynomial time algorithm for finding a query containment. Most XPath expressions in usual XML queries fall into this fragment and it is a good start for us to design algorithms for this XPath fragment.

2.3 Access Control on XML Documents

Access control in an XML PDMS is the main problem we are working on. It is necessary for us to analyze the existing approaches for securing XML documents.

With the development of web-based applications, XML has become the de facto standard of semi-structured data representation. It provides an easy way to publish information. Selective distribution and sharing of XML documents requires enforcement of access control. This ensures that specific information is accessible only to authorized entities or roles.

Different access control approaches for local XML documents have been proposed. Among them, access control policy model is widely recognized as an expressive, fine-grained method. An Access Control Policy is a rule defined to permit or deny the use of some objects/elements in an XML document by a subject/user.

XACML[39] presents an XML schema for specifying access control policies on XML documents. However, it is very complicated and even requires a spe-
cific processing model to interpret the access control policies. Paper [25] defines an access control language using the concept of role, which is an abstract representation of a set of privileges and could be assigned to users. It supports both read/write and positive/negative policies. Paper [21] formalizes access control policies in a SQL security model compatible manner, but it doesn't support negative policies. For all these work, the permission/prohibition on an element is automatically propagated to its subelements. The above work concentrate on the formal expression of an access control policy, not on its usage.

Access control policies can also be manipulated in different ways. The method of [18] is view-based. It allows the definition and enforcement of access control directly on XML documents, then produces a separate view on the document for each user. The method of [10, 34] are encryption-based. They define a formal syntax of access control policies for XML documents, and encrypt different portions of the same document according to different encryption keys. Then various users can use their own encryption keys to get the desired portion of the same encrypted document. Paper [14] is the first step to handle querying XML data in light of access control policies. Its access control policies are XML-compatible. But only very simple XQueries can be transformed to directly incorporate restrictions of access control policies on XQuery variables.

In later chapters, we will see that our access control policy model supports both read/write and positive/negative privileges, and it plays an important role in the query rewriting algorithm.
Chapter 3

Access Control in XML PDMS

In Section 2.3, we have summarized the work of access control on local XML documents. However, the existing research work does not reveal what problems will arise in a PDMS, where access control on distributed XML data sources are required.

In Section 3.1, we describe a general view of the access control problems in a PDMS. Then we concentrate on our solution – Access Control Policy (ACP) in the XML PDMS. We present the ACP formal syntax in Section 3.2, the ACP examples in Section 3.3, and the semantics of PDMS query answering under ACPs in Section 3.4.

3.1 The Problem in General

Access control and its subsequent problems arise not only in local XML documents, but in peer data management systems. As the owner of a database, a peer is not always ready to publish all its data for any other peer. Peers need to control their data in fine-granularity, i.e., which part of data can be accessible by which peers.

When access control exists in peers of a PDMS, some problems will arise. In Section 3.1.1 we will present the general sense of two important problems in access control: information leakage and answer completeness.

There are multiple methods that can be used to enforce access control. Different possibilities have different characteristics. In Section 3.1.2, we analyze a few typical methods. In Section 3.1.3, we use an example to illustrate what the differences are in these methods.
3.1.1 General Sense of Information Leakage and Completeness

Generally speaking, information leakage means that some protected data are accessed by unauthorized subjects. Given certain access control requirements in a PDMS, information leakage must be avoided. It is the basic security issue for a PDMS. Information leakage in a PDMS mainly include the following aspects:

- in the query-answering process, an answer tuple is routed to a peer, who is not authorized to see this tuple according to any access control rule;
- some data is malevolently exposed to peer \( p_1 \) by peer \( p_2 \), even \( p_1 \) is not authorized to see these data by access control rules of the original data owner;
- access control instances are improperly distributed to unauthorized peers.

The first aspect is our focus, which can be effectively avoided by a well designed query-answering algorithm. The other two aspects are not issues that can be solved at an algorithm level. So they will not be in the scope of our work.

Completeness refers to the answer completeness. After a query is put forth by a peer in a PDMS, completeness refers to that the maximum answer set will be retrieved. Given enough time, network bandwidth and powerful local computation capability, we expect the requesting peer can get back the theoretically maximum answer set. A good query-answering algorithm for a PDMS can ensure the maximum and sound answer set to return.

3.1.2 General Methods of Access Control

Now we have a general idea about access control. We need to know more about how access control can be enforced in a PDMS. Let us briefly study the general methods that can be used in the PDMS access control.

(1) Encryption vs. No Encryption.

When the intermediate answer is routed back to the source peer, the system must ensure no information leakage in this process. To ensure that there is no information leakage, either encryption or non-encryption method can be used. Using the encryption method means to encrypt the answer at the target peer, and decrypt the answer when it arrives at the source peer. Using the non-encryption method means to route the original answer from the target peer to
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the source peer via a selected path (maybe answer transformations are needed during the process), while ensuring that every peer in the path have right to access the answer.

Using the encryption method, the answer can be routed along any path. Its overhead is that the answer needs to be encrypted at the target peer and decrypted at the source peer. Furthermore, the target peer needs to know who is the source peer for each incoming query, such that the decryption key can be distributed. Using the non-encryption method, there is no overhead caused by the encryption and decryption, but there exists a risk of information leakage and if steps are taken to reduce it, the returned answer set may be incomplete. Thus, the answer routing algorithm should be carefully designed.

In a PDMS, any peer can be a source peer or a target peer, so the aforementioned decryption key distribution in the encryption method is a heavy burden. Moreover, because of scheme heterogeneity, when an answer set is routed among peers, it is decrypted and rewritten adhering to the database schema of each passing peer, and then encrypted for routing to the next peer. That means, decryption and encryption are needed at each routing peer. This is another heavy burden. Thus, in the thesis we concentrate on query-answering algorithms without encryption.

(2) Evaluating vs. Rewriting

How is a query handled and computed in a PDMS with access control? There are two different methods: evaluating and rewriting. Evaluating a query means passing along a query as initially written (presumably along with some annotation of what the passing peers are), and then the target peer that is returning the answer is responsible for extracting only the tuples that are relevant according to the access control requirements. Rewriting a query means taking the query along the way and changing the query at each peer such that it adheres to the access control requirements for the peer.

Using evaluating, the query is enforced with access control rules once at the target peer. But it requires to keep record of all peers along a query transmitting path. Using rewriting, the query is enforced with access control rules at every peer along the query transmitting path. Rewriting requires all access control rules have been distributed to peers where they are needed.
3.1.3 Example

Let us take a small example to illustrate the methods in Section 3.1.2. There is a PDMS with four peers (a, b, c, C2); whose topology is shown in Figure 3.1. In the PDMS, a is the source peer that puts forth a query Q, and b is the target peer that answers Q. For simplicity, we assume (1) all peers have the same schemas, (2) the database on b is a relational database. The database on b holds one table T, in which there are only two tuples t1 and t2. Peer b defines the access control rules R1 and R2:

- R1: only peer a and c1 have access to tuple t1.
- R2: only peer a and C2 have access to tuple t2.

The query Q is "SELECT * from T". The access control rules R1 and R2 ensure that a can access to all tuples in table T, i.e., t1 and t2. Thus, the final answer set arriving at a should be \{t1, t2\}.

First, let us consider the encryption and non-encryption methods for answer routing. If the encryption method is used, the target peer b evaluates the incoming query Q, gets the answer set S = \{t1, t2\}, and encrypts S as S'. Then the S' can be routed back to a along either the path b → c1 → a or the path b → C2 → a. The encryption ensures no information leakage. When S' arrives at a, it is decrypted back to S. If the non-encryption method is used, the target peer b evaluates the incoming query Q, and gets the answer set S = \{t1, t2\}. Pick the path b → c1 → a and route t1 back via this path, because
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peer c₁ just has access to t₁ (according to R₁) but no access to t₂. Similarly, pick the path b → c₂ → a and route t₂ back via this path, because peer c₂ just has access to t₂ (according to R₂) but no access to t₁.

Secondly, let us consider the evaluating and rewriting methods. Suppose we use the non-encryption answer routing method and route the computed answer backtracking the query incoming path. Consider the path a → c₁ → b. If the evaluating method is used, the query Q is routed along a → c₁ → b as initially rewritten, keeping an annotation of all passing peers {a,c₁}. When Q arrives at b, b notices the annotation {a,c₁} and uses the relevant access control rules R₁ and R₂ to rewrite Q into Q'. The answer is evaluated from Q' and routed back along b → c₁ → a. If the rewriting method is used, we must make sure that R₁ has been distributed to a and c₁, and R₂ has been distributed to a and c₂. Consider the path a → c₁ → b. The query Q is first rewritten into Q' at a according to rules R₁ and R₂, which ensures the answer of Q' can be accessed by a. Next, when Q' arrives at c₁, it is rewritten into Q'' according to R₁, which ensures the answer of Q'' can be accessed by c₁. Thus Q'', which will finally arrive at b, ensures its answer can be accessed by both a and c₁. After Q'' is computed at b, the answer can be safely routed back to a via b → c₁ → a.

3.2 Access Control Policy (ACP) Formal Definition

Having a general idea about the access control problems in a PDMS, we will take the first step into our own solution.

As shown in Chapter 2, access control policy (ACP) is a flexible, expressive and fine-grained approach. Once specified, ACPs are platform-independent and can be easily transformed and distributed in a PDMS environment. Thus our work adopts ACP as the access control model for peer databases. Our whole access control scheme is based on such an ACP model.

Let us propose the ACP formal definition and syntax for the XML PDMS:

**Definition 3.1 (Access Control Policy (ACP))** An access control policy ACP is defined in the following form: \( +/ - R(u,x) \leftarrow SLA(target,u), q(x) \). Such a policy defines that a set of peers u has read access to some target data elements x under the restrictions of service level agreement SLA(target, u) and object constraint q(x).
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- +/- denotes authorize/deny access.

- $R$ denotes that it is a READ ACP. That means, the authorized peers will have the READ privilege of the target data elements.

- $u$ denotes the set of subject/user/role, which are the identifiers of users in the system and often refer to peers.

- $x$ denotes the set of target data elements. Here we define target schema as the data schema on which the ACP has effect. Target data elements are some elements in the data schema, which are those elements that the ACP is allowing or denying access to.

- $\text{target}$ refers to the target peer, who is the owner of the target schema.

- $\text{SLA}(\text{target}, u)$ denotes a predicate that tests the role of the peers, i.e. whether peers $u$ have a service level agreement with the target peer. If $u$ satisfies $\text{SLA}(\text{target}, u)$, $u$ will have the access privilege defined by this ACP.

- $q(x)$ is the DB predicate or value constraints, which expresses the constraints on the target XML document. $q(x)$ can be a conjunction of atoms. An atom can be a variable binding, a relational expression of equality or inequality. However, the expression of $q(x)$ doesn't mean these constraints only have the domain of the target elements $x$, normally they are the constraints on all related elements. In this abstract expression, we don't treat $x$ as the domain of $q(x)$.

- The authorize/deny access on an element $x$ is automatically propagated to its subelements. We believe it makes sense to be consistent with the semantics of XQuery answers.

- Similarly, we use $W(u, x)$ to denote a WRITE/EDIT ACP. That means, the authorized peers will have the WRITE privilege of the target data elements.

Without any specification, the strength of $\text{SLA}(\text{target}, u)$ in an ACP may become boundless. We place a limit on what $\text{SLA}(\text{target}, u)$ can contribute: $\text{SLA}(\text{target}, u)$ only checks the agreement relationship between peers, i.e. which peers are authorized the privilege on target database by this ACP. In some cases, an ACP needs to match the peer's ID with an element value in the target
database. For example, assume there is an element in the database of my peer about the visitor’s ID. My peer defines an ACP that only the classmate peers have access to my database information. The ACP needs a way to compare the visitor peer’s ID with the element value in my database. In our ACP syntax, we use a function \textit{compatible}(x, y) to deal with the match of a peer ID and an element value in the target database. The basic ACP structure and use of the \textit{SLA}(target, u) and \textit{compatible}(x, y) functions are illustrated in the examples of next section.

3.3 PDMS Scenarios with ACP Examples

In the previous section, we introduced the formal syntax of an ACP. In this section we illustrate it with some concrete PDMS scenarios and ACP instances. The examples show that the ACP syntax is XPath-based and XQuery-compatible. It makes a good basis for our later XML query rewriting algorithm.

The first example illustrates the basic structure of the READ ACP. The scenario is a hospital PDMS from the HePToX project [13]. It is shown in Figure 3.2.

![Figure 3.2: Hospital PDMS Example](image)

The Vancouver General, Montreal General and Toronto General are the three peers in this PDMS. For simplicity, we call Vancouver General, Montreal General, Toronto General separately as ‘vg’, ‘mg’ and ‘tg’. Suppose there is only one XML database on each peer and they are ‘vg.xml’ for ‘vg’, ‘mg.xml’
for ‘mg’, ‘tg.xml’ for ‘tg’.

Suppose there are two access control requirements on the schema of ‘mg’:

1. peer ‘vg’ has READ access to patient’s admission and process information later than Jan 1, 1990 of peer ‘mg’;
2. Nobody has read access to patients’ admission and progress information later than Jan 1, 2004.

Then we can create the corresponding ACPs for the above requirements:

R1: 
\[ +R(u,a,p) \leftarrow SLA('mg', u), \]
\[ \text{doc}('mg.xml')/MG/Admission a, \]
\[ \text{doc}('mg.xml')/MG/Progress p, \]
\[ a/ID = p/PatRef, \]
\[ p/Symptom/Date > 'Jan 1, 1999'. \]
Where only \( u = 'vg' \) satisfying SLA('mg', u).

R2: 
\[ -R(u,a,p) \leftarrow SLA('mg', u), \]
\[ \text{doc}('mg.xml')/MG/Admission a, \]
\[ \text{doc}('mg.xml')/MG/Progress p, \]
\[ a/ID = p/PatRef, \]
\[ p/Symptom/Date > 'Jan 1, 2004'. \]
Where for every peer \( u \) there is a ('mg',u) tuple satisfying SLA.

In this example, we see the basic structure of a READ ACP. The first ACP R1 is positive, which authorizes a peer to have the READ privilege on elements \( a \) and \( p \) under restrictions. The second ACP R2 is negative, which denies a peer to have the READ privilege on elements \( a \) and \( p \). Assume there is an SLA database. There is only one tuple < 'mg', 'vg' > for R1 in the SLA database, but every peer \( u \) has a tuple < 'mg', u > for R2 in the database. We also see any legal arithmetic expression in XQuery, such as \( p/Symptom/Date > 'Jan 1, 2004' \), can be used in an ACP.

The second example illustrates the use of the compatible() function. The scenario is an academic conference proceeding. The target peer is named 'conf', and the XML database on this peer is 'conf.xml'. The schema of 'conf.xml' is shown in Figure 3.3.
Suppose we want to express the following access control requirements on this database schema:

1. Every PC member has READ access to all papers in his area of expertise.
2. No PC member has READ access to any of his own papers regardless of his area.

The corresponding ACPs are listed as follows:
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R1:
\[ +R(u, p) \leftarrow SLA('conf', u), \]
\[ \quad doc("conf.xml")/PC/Member pm, \]
\[ \quad doc("conf.xml")/Papers/paper p, \]
\[ \quad compatible(u, pm/Name), \]
\[ \quad pm/Area = p/Area. \]

Where \( SLA('conf', u) \) defines the membership relation of any user for the conference, the function \( compatible() \) checks matching of a peer ID \( u \) and a PC member's name.

R2:
\[ -R(u, p) \leftarrow SLA('conf', u), \]
\[ \quad doc("conf.xml")/PC/Member pm, \]
\[ \quad doc("conf.xml")/Papers/paper p, \]
\[ \quad p/Author pa, \]
\[ \quad pa = pm/Name, \]
\[ \quad compatible(u, pm/Name). \]

Where \( SLA('conf', u) \) defines the membership relation of any user for the conference, \( compatible() \) checks matching of a peer ID \( u \) and a PC member's name.

In this example, we see the use of the function \( compatible() \). As described in Section 3.2, the function \( compatible() \) checks if a peer ID matches an element in the target database.

The third example illustrates the WRITE ACP and the negative use of the \( compatible() \) function. The scenario is a company management PDMS. This company has several departments. Each department server is an autonomous peer. Each department has a manager and some employees. (The manager is also an employee.) The database schema for one department peer is shown in Figure 3.4:

We name the peer in the figure as 'd', its XML database as 'department.xml'. Suppose we need to express the following access control requirements on the schema of 'd':
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Figure 3.4: Company Management PDMS Example

1. Every manager has WRITE access to any employee's full information in his department.

2. Every manager is denied WRITE access to any employee's information in other departments.

3. Every employee has READ access to his own information.

4. Every employee is denied READ access to other's salary information.

Then the corresponding ACPs are specified as follows:
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R1:
\[ +W(u, e) \leftarrow SLA('d', u), \]
\[ \text{doc("department.xml")/Department/Employee e,} \]
\[ \text{doc("department.xml")/Department/Manager m,} \]
\[ \text{compatible(u, m/ID),} \]
\[ m/\text{DeptID} = e/\text{DeptID}. \]

Where \( SLA('d', u) \) defines the relation for membership in this company, the function \( \text{compatible()} \) checks matching of a peer ID \( u \) and a manager's ID, \( m/\text{DeptID} = e/\text{DeptID} \) shows the manager and the employee are in the same department.

R2:
\[ -W(u, e) \leftarrow SLA('d', u), \]
\[ \text{doc("department.xml")/Department/Employee e,} \]
\[ \text{doc("department.xml")/Department/Manager m,} \]
\[ m/\text{DeptID} = e/\text{DeptID}. \]

Where \( SLA('d', u) \) defines the relation for membership in this company, \( m/\text{DeptID} = e/\text{DeptID} \) shows the manager and the employee are not in the same department.

R3:
\[ +R(u, e) \leftarrow SLA('d', u), \]
\[ \text{doc("department.xml")/Department/Employee e,} \]
\[ \text{compatible(u, e/EID).} \]

Where \( SLA('d', u) \) defines the relation for membership in this company, the function \( \text{compatible()} \) checks matching of a peer ID \( u \) and an employee's ID.

R4:
\[ -R(u, s) \leftarrow SLA('d', u), \]
\[ \text{doc("department.xml")/Department/Employee e,} \]
\[ e/\text{Salary s,} \]
\[ \text{NOT compatible(u, e/EID).} \]

Where \( SLA('d', u) \) defines the relation for membership in this company, the function \( \text{compatible()} \) checks matching of a peer ID \( u \) and an employee's ID.

In this example, we see the positive and negative WRITE ACPs (R1 & R2). And we also see that \( \text{compatible()} \) function can be used with "NOT" to represent mismatching (R4).
3.4 Semantics of PDMS Query-Answering under ACPs

Given that all ACPs are specified and distributed as needed, what is the answer semantics of the PDMS query-answering? More specifically, what kind of answer do we expect to get after a query is put forth at a peer in a PDMS? In this section, we will formalize the semantics of PDMS query answering under ACPs.

The access control issue is orthogonal to the issue of schema heterogeneity. Thus, to simplify the problem, we assume that all peers use the same schema. This allows us to tackle access control without adding in the complications of schema heterogeneity. We leave the addition of schema heterogeneity to the problem as future work. Besides, we do not distinguish a peer with a requester. Several requesters may put queries on a peer to the whole PDMS. We assume all queries are put forth by a same peer. This simplification will help us to see the nature of the semantics problem.

Firstly let us start with the answer semantics of a PDMS without access control. Given a PDMS with $n$ peers ($p_1, p_2, ..., p_n$), each peer has a local database $DB_{pi}$ ($i = 1..n$). In a practical PDMS, there may be some peers who are virtual nodes and do not have a local database. However, this case is not considered here. Suppose a query $Q$ is put on $p_1$. The full answer set returned at $p_1$ is the union of the answer set from every peer. For each peer $p_i (i = 1..n)$, the partial answer set is $Q(DB_{pi}) (i = 1..n)$. Thus, the semantics of answer returned by the PDMS is $\bigcup_t Q(DB_{pi}) (i = 1..n)$.

Next let us add the factor of access control. Let $AV_{pi}(DB_{pi})$ be the access view for peer $p_i$ on peer $p_i$’s database, which holds for a centralized system using any access control policy model. For each peer $p_i (i = 1..n)$, the answer that $p_i$ has the permission to see on $DB_{pi}$ is $Q(AV_{pi}(DB_{pi}))$. Thus, naively, one might expect the full answer returned to $p_1$ to be $\bigcup_t Q(AV_{pi}(DB_{pi}))$, where $i = 1..n$. But it is not correct. Because any answer tuple needs to be routed from the answering peer $p_i$ to $p_1$ via some other peers. It must ensure that an answer tuple can be accessed by every peer along the routing path. Consider this problem in another way: when a query is transmitted from $p_1$ to $p_i$, the query will pass via some other peers, and these peers will add access control constraints on the access view of $p_i$ to make the final answer set smaller than $Q(AV_{pi}(DB_{pi}))$.

Consider the following example. Figure 3.5 is a PDMS topology. Suppose
Figure 3.5: Example for Semantics of PDMS Query Answering under ACPs

$p$ sends a query $Q$, and peer $q$ returns partial result by several routing paths. The label attached to each edge denotes the policy constraint. E.g. $(p, 1, 2)$ denotes a query through this path can only be evaluated on the access view $AV_p(DB_q) \cap AV_1(DB_q) \cap AV_2(DB_q)$, or simply as $AV_{(p,1,2)}(DB_q)$. Thus the final result returned from $q$ to $p$ is $Q(AV_{(p,1,2)}(DB_q)) \cup Q(AV_{(p,1,2,3)}(DB_q)) \cup Q(AV_{(p,3,2)}(DB_q)) \cup Q(AV_{(p,3)}(DB_q))$, or simply as $\bigcup_{P_{pq}} Q(AV_{P_{pq}}(DB_q))$, where $P_{pq}$ is a path from $p$ to $q$. This answer is different from $AV_p(DB_q)$.

Generalize the above result for a PDMS with $n$ peers $p_1, ..., p_n$, where $p_1$ puts forth a query $Q$ and every peer answers it. The final answer set returned to $p_1$ is $\bigcup_i \bigcup_{P_{pi}} Q(AV_{P_{pi}}(DB_{pi}))$ (i = 1..n), where $P_{pi}$ is a path from $p_1$ to $p_i$. This is the semantics of the PDMS query-answering under ACPs.
Chapter 4

Strategies and Options for the Query-Answering Process

Chapter 3 presented the syntax of the access control policy and showed that it is expressive enough to specify fine-grained access control on peers' local database. But we have not described how to enforce ACPs, or say, how ACPs are used in the PDMS query answering process.

Intuitively, a query-answering process can be clearly divided into two parts: query transmitting and answer routing. Thus we separate a query-answering algorithm into two parts: a (query transmitting) strategy and an (answer routing) option.

Study on the general methods for access control (Section 3.1.2) inspires our designing strategies and options. In this chapter, we present the intuition (Section 4.1) and formal definitions of a strategy and an option (Section 4.2), then describe the basic assumptions (Section 4.3) and our designed strategies and options that make use of access control polices (Section 4.4).

4.1 Intuition

The security problem arising in a PDMS concentrates on the query-answering process. Such a query-answering process is under the control of a distributed, runtime algorithm. The algorithm distributes the query or its rewritten form from the source peer to many target peers and retrieves answers from these target peers to the source peer. The example used in Section 3.1.3 is helpful for illustrating the problem. Please refer to Figure 3.1. The example setting is exactly the same, including the topology, peers, ACPs, query, and so on. Assume a non-encryption query-answering algorithm controls the query-answering pro-
cess of the PDMS. When a query $Q$ is put forth at peer $a$, the query-answering algorithm transmits $Q$ via every path from peer $a$ to peer $b$, and for each path $Q$ is rewritten to a new query according to relevant ACPs. Let the rewritten query via path $a \rightarrow c_1 \rightarrow b$ be $Q'$, the rewritten query via path $a \rightarrow c_2 \rightarrow b$ be $Q''$. Then the answer set for $Q'$ is $\{t_1\}$, and the answer set for $Q''$ is $\{t_2\}$. If the query-answering algorithm routes $\{t_1\}$ back to $a$ via $b \rightarrow c_2 \rightarrow a$, the information leakage arises. Because peer $c_2$ is not authorized to access $t_1$ by any ACP. Thus, to ensure no information leakage, the query-answering algorithm must route $\{t_1\}$ back to $a$ via $b \rightarrow c_1 \rightarrow a$. Likely, the query-answering algorithm must route $\{t_2\}$ back to $a$ via $b \rightarrow c_2 \rightarrow a$.

To study the problem, we concentrate on the basic building block: transmitting a query asked by a single source peer to a single target peer, and then routing the answer set from that target peer back to the source peer. When a query $Q$ is posed at a source peer $c$, the answer set for $Q$ from any target peer containing relevant data needs to be computed and routed to $c$, modulo ACPs. Thus, the overall problem is built up on basis of the simpler problem of single source peer and single target peer.

The above pair-wise idea makes clear the building block of the query-answering algorithm. Next, let us consider the query-answering process for a pair of given source peer and target peer. The process can be clearly divided into two sequential, non-overlapping parts:

I. query transmitting: informally speaking, transmitting the rewritten queries of the original query from the source peer to the target peer via some paths;

II. answer routing: informally speaking, routing back the set of answer tuples from the target peer to the source peer via some paths.

From now on, we call an algorithm handling Part I as Query Transmitting Strategy, or Strategy; and an algorithm handling Part II as Answer Routing Option, or Option. Then a distributed query-answering algorithm is composed of a Strategy and an Option. We will use a $(Strategy, Option)$ pair to denote a query-answering algorithm, simply as an $(S, O)$ pair. The properties of an $(S, O)$ pair are those of the corresponding query-answering algorithm.
4.2 Formal Definitions for Strategy and Option

In this section, we will present the formal definitions for a Strategy and an Option. First of all, we define some terminology, which will be widely used in later discussion:

- ACP of \( x \) for \( y \): \( x \)'s definition of what \( y \) can have access to \( x \)'s data, where \( x \) and \( y \) are both peers
- associated peer \( c \) of ACP \( A \): peer \( c \) is defined in ACP \( A \) to access some data of another peer
- \( V \): a set of peers in a graph
- \( a \): the source peer
- \( b \): the target peer
- \( D \): a database
- \( D_b \): the database residing on \( b \)
- \( Q \): a query
- \( Q(D) \): the database to hold the answer of evaluating \( Q \) on \( D \).
- \( t \): an (answer) tuple in some \( Q(D) \). Here the word "tuple" refers to the building block of \( Q(D) \). For example, if \( D \) is a relational database and \( Q \) is a SQL query, \( t \) is a tuple in the relation \( Q(D) \); if \( D \) is an XML database and \( Q \) is an XQuery, \( t \) is an XML subtree or a combination of variable values.
- \( p_L(D) \): a new database, which defines part of database \( D \) that can be accessed for all peers in the set \( L \). If \( L \) contains just one peer \( c \), \( p_L(D) \) can be simply written as \( p_c(D) \) instead of \( p_{L(c)}(D) \).
- \( P \): a path (sometimes it also refers to the set of all peers in a path if there is no ambiguity). Note that throughout we assume that any path conforms to the given topology.
- \( P_{a\rightarrow b} \): a path from \( a \) to \( b \)
- \( P_{a\rightarrow b} \): the set of all paths from \( a \) to \( b \)
The formal definitions for Strategy and Option that are used to transmit queries and answers over a single source peer and target peer set are shown in Definition 4.1 and 4.2. As mentioned in the previous section, this is the building block of the general case of one source peer and many target peers.

**Definition 4.1 (Strategy)** Given source peer $a$, target peer $b$, query $Q$, choose a set of paths from $a$ to $b$, and $\forall$ such path: transmit some rewritten query $Q'$ to $b$.

**Definition 4.2 (Option)** Given source peer $a$, target peer $b$, query $Q$, a set of tuples $S$ at $b$, choose a set of paths $P_{b\rightarrow v}$ from $b$ to $V$, where $V$ is a set of peers, and send each tuple $t \in S$ down $0$ or more paths $\in P_{b\rightarrow v}$.

These definitions are at an abstract level. Note that "choose a set of paths" refers to the fact that the strategy or option will decide which paths the query or tuples will be sent down and does not reply that the path will be chosen apriori. The combination of a strategy and an option decides the distributed, runtime features of the query-answering process in a PDMS. Because there is little complication for query evaluation (i.e. generating answer tuples at the target peer), it is regarded as a separate phase between a Strategy and an Option, and not included in either of them.

### 4.3 Basic Assumptions

To evaluate the approach, we created a number of general strategies and options. These strategies and options cover quite a broad spectrum, so we believe that most other strategies and options are variants of them. In this section, we propose a few important assumptions, which build the basis for our strategies and options.

1. **Databases residing on all peers have the same schema.** Although this assumption is not true for a realistic PDMS, schema heterogeneity will not affect the essence of security problem. Query rewriting or data transformation among different schemas is orthogonal to access control. This assumption simplifies the linguistic expressions, and allows us to concentrate on security issues in the query-answering process. So in later discussion, we ignore the query rewriting only with respect to schema heterogeneity. We leave the addition of schema heterogeneity to the problem as future work.
2. When a query $Q$ is transmitted along a path $P$, $P$ is noted for $Q$. Assume there is a trivial way to record passing peer ID's with the routed query $Q$. It is handy and costs little. We ignore the cost of this task in later discussion.

3. **Peers don't collude with each other.** In other words, peers will not viciously share information to seek unauthorized data. Given peers $c_1$, $c_2$, $c_3$, tuple $t \in D_{c_1}$, and $c_2$ has got $t$ from $c_1$, which is authorized by $c_1$'s ACPs. Then $c_2$ can not share $t$ with $c_3$ unless $c_2$ have enough knowledge (annotations, ACPs) from $c_1$ to verify $c_3$'s right to access $t$. Else we call it an illegal behavior. We don't consider such illegal behaviors, even when we discuss information leakage in Section 5.1.

4. Assume a tuple $t$ can be accessed by peer $c_1$ and has been routed to $c_1$. $t$ can be distributed from peer $c_1$ to another peer $c_2$, only if $c_1$ has sufficient witness from $t$'s source peer $s$, on whose database $t$ is computed. That means, even $c_1$ has the right to access $t$, it doesn't have the right to willfully distribute $t$. The concrete cases we are concerned include: (1) $c_1$ must respect $t$'s annotation. More specifically, if $t$ has been routed to $c_1$ together with its annotation $A_t$ (the set of safe peer ID's), $c_1$ obeys $t$'s annotation only to share it with peers $d \in A_t$. (2) $c_1$ must have all ACPs of $s$ for $c_2$ to determine if $c_2$ can access $t$. The precondition for this assumption is: each peer behaves legally according to the query-answering algorithm and trusts data from other peers. More specifically, if peer $c_1$ receives tuple $t$, $c_1$ trusts any information about $t$ received from other peers.

5. Let $A_1$ be an ACP of the target peer $b$ for peer $c_1$. If $A_1$ is required for rewriting a query $Q$ at $c_1$, $A_1$ must have been distributed to $c_1$ in a safe way. According to the definition, Strategy is a runtime algorithm. Distributing ACPs to requiring peers is the preparation for a strategy. Although we don't consider how to perform this work in a strategy, it is indeed a precondition of a strategy. Later we will elaborate on this task and count in its cost in the cost model and in $(Strategy, Option)$ pairs' costs.

6. Let $A_1$ be an ACP of the target peer $b$ for peer $c_1$. Assume $c_1$ and $c_2$ are adjacent peers in the P2P network, and $c_2$ attempts to route an answer tuple $t$ to $c_1$. If $A_1$ is required at $c_2$ to determine
whether $c_1$ has access to tuple $t$, $A_1$ must have been distributed to $c_2$ in a safe way. One might think it is risky to distribute the ACP $A_1$ for peer $c_1$ to peer $c_2$, which will cause information leakage. But in fact it is safe on condition of Assumption 3 and Assumption 4. Under Assumption 3 and 4, even $c_2$ knows ACP $A_1$, there is no way for $c_2$ to get illegal data from $c_1$. Because $c_1$ will use ACPs of target peer $b$ for $c_2$ to determine whether send $b$'s data to $c_2$. According to the definition, an option is a runtime algorithm. Distributing ACPs to requiring peers is just the preparation for an option. We don't consider how to conduct it in an option. But later we will elaborate on this task and count in the cost of it in our cost model and in (Strategy, Option) pairs' costs.

Without special claim, Assumption 1 to 4 hold for any strategy and option. Assumption 5 and 6 hold when the “if” conditions are met.

### 4.4 Strategies and Options Designed

In this section, we will present the strategies and options we designed. The terminology for these strategies and options is listed at the beginning of Section 4.2. The basic assumptions are listed in Section 4.3.

The following are the strategies we worked out, which make use of ACPs. We use $S_1$ to $S_4$ to denote them.

- **$S_1$ Proactive Rewriting:** Assumption 5 holds. $\forall$ path $P \in \mathcal{P}_{a \rightarrow b}$, $S_1$ transmits $Q$ along $P$ by: at each peer $c \in P$, when the query, thus far $Q'$, is transmitted to it, it transmits $Q''$ to the next peer in $P$, where $Q'' = Q'$ rewritten to adhere to ACPs of $b$ for $c$.

- **$S_2$ Lazy Rewriting – Dumb:** For one path $P \in \mathcal{P}_{a \rightarrow b}$, $S_2$ transmits $Q$ via $P$. When $Q$ is transmitted at $b$, $Q$ is rewritten into $Q' = Q$ rewritten to adhere to ACPs of $b$ for all peers in the PDMS.

- **$S_3$ Lazy Rewriting – Path:** $\forall$ path $P \in \mathcal{P}_{a \rightarrow b}$, $S_3$ transmits $Q$ via $P$. When $Q$ is transmitted at $b$, $Q$ is rewritten into $Q' = Q$ rewritten to adhere to ACPs of $b$ for all peers in $P$.

- **$S_4$ Jobless:** $\forall$ path $P \in \mathcal{P}_{a \rightarrow b}$, $S_4$ just transmits $Q$ via $P$. 


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In order to make $S_i$ ($i=1..4$) work well, there are necessary obligations for peers in the PDMS:

- For $S_1$, $\forall$ peer $c$ (except the target peer $b$): $c$ use all ACPs of $b$ for $c$ to correctly rewrite the received query $Q'$ into the new query $Q''$ and $c$ route $Q''$ to the next peer.

- For $S_2$ and $S_3$, $\forall$ peer $c$ (except the target peer $b$): $c$ forwards the received query $Q$ to the next peer. For the target peer $b$: $b$ correctly rewrites the received query using required ACPs.

- For $S_4$, $\forall$ peer $c$ (except the target peer $b$): $c$ forwards the received query $Q$ to the next peer.

The following are the options we designed, which make use of ACPs. We use $O_i$ to $O_6$ to denote them.

$O_1$ Whole — Backtracking: Given target peer $b$, database $D$ at $b$, query $Q$ that has been transmitted at $b$ via some path $P \in \mathbb{P}_{a\rightarrow b}$, $Q$ and $P$ have been chosen by some strategy. $Q(D)$ is regarded at $b$ as the answer set. Annotate answer set $Q(D)$ with path $P$. At each peer $c \in P$, $c$ routes $Q(D)$ to the previous peer in $P$ until $c = a$.

$O_{2A}$ Whole — Sub1: Given target peer $b$, database $D$ at $b$, query $Q$ that has been transmitted at $b$ via some path $P \in \mathbb{P}_{a\rightarrow b}$, $Q$ and $P$ have been chosen by some strategy. $p_p(Q(D)) \subseteq Q(D)$ is regarded as the answer set at $b$. Annotate answer set with path $P$. Choose a path $P'$ s.t. $P' \in \mathbb{P}_{b\rightarrow a}$ and $P' \subseteq P$. Route $p_p(Q(D))$ down $P'$.

$O_{2B}$ Whole — Sub2: Given target peer $b$, database $D$ at $b$, query $Q$ that has been transmitted at $b$ via some path $P \in \mathbb{P}_{a\rightarrow b}$, $Q$ and $P$ have been chosen by some strategy. $Q(D)$ is regarded as the returned answer set at $b$. Annotate answer set with path $P$. Choose a path $P'$ s.t. $P' \in \mathbb{P}_{b\rightarrow a}$ and $P' \subseteq P$. Route $Q(D)$ down $P'$.

$O_3$ Whole — Target Annotating: Given target peer $b$, database $D$ at $b$, query $Q$ that has been transmitted at $b$ via some path $P \in \mathbb{P}_{a\rightarrow b}$, $Q$ and $P$ have been chosen by some strategy. The returned answer set at $b$ is $A = p_p(Q(D)) \subseteq Q(D)$. Use ACPs of $b$ to decide the safe peer list.
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$L = \{c|p_c(A) = A\}$. Annotate the answer set $A$ with $L$. Choose a path $P'$ s.t. $P' \in P_{b \rightarrow a}$ and $P' \subseteq L$. Route $A \times \{L\}$ down $P'$.

**O4A Whole – Dynamic Routing**: Assumption 6 holds. Given target peer $b$, database $D$ at $b$, query $Q$ that has been transmitted at $b$ via some path $P \in P_{a \rightarrow b}$, $Q$ and $P$ have been chosen by some strategy. The returned answer set at $b$ is $A = p_P(Q(D)) \subseteq Q(D)$. ∀ peer $c$ that received $A$: $c$ routes $A$ to peer $d$ if $p_d(A) = A$, until $A$ arrives at $a$.

**O4B Whole – Dynamic Routing**: Assumption 6 holds. Given target peer $b$, database $D$ at $b$, query $Q$ that has been transmitted at $b$ via some path $P \in P_{a \rightarrow b}$, $Q$ and $P$ have been chosen by some strategy. The returned answer set at $b$ is $A = p_P(Q(D)) \cup S$, where $S$ is the set of supporting elements. ∀ peer $c$ that received $A$: $c$ routes $A$ to peer $d$ if $p_d(A) = A$, until $A$ arrives at $a$.

**O5 Partition – Target**: Given target peer $b$, database $D$ at $b$, query $Q$ at $b$, $Q$ has been chosen by some strategy. $Q(D)$ is regarded as the answer set.

1. Partition $Q(D)$ as follows: let the partition $K = K_1, \ldots, K_n$, where
   $$\bigcup_{i=1}^{n} K_i = Q(D) \land K_i \cap K_j = \emptyset(i \neq j)$$
   ∀ $K_i$ ($i = 1..n$), use ACPs of $b$ to compute its annotation $L_i$, where $L_i = \{c|p_c(K_i) = K_i\}$

2. ∀ $K_i$ ($i = 1..n$): if $K_i \times \{L_i\}$ arrives at peer $c$, $c$ routes $K_i \times \{L_i\}$ to all its neighbors $d$, where $d \in L_i$.

**O6A Dynamic Routing**: Assumption 6 holds. Given target peer $b$, database $D$ at $b$, query $Q$ at $b$, $Q$ has been chosen by some strategy. The returned answer set at $b$ is $Q(D)$. Let $c$ be a peer who receives a subset $K \subseteq Q(D)$. ∀ $c$ ∀ its neighbor $d$: $c$ routes $p_d(K)$ to $d$. Notice: all parts sent by $c$ to its neighbors may not be disjointed.

**O6B Dynamic Routing**: Assumption 6 holds. Given target peer $b$, database $D$ at $b$, query $Q$ at $b$, $Q$ has been chosen by some strategy. The returned answer set at $b$ is $A = Q(D) \cup S$, where $S$ is the set of supporting elements. Let $c$ be a peer who receives a subset $K \subseteq A$. ∀ $c$ ∀ its neighbor $d$: $c$ routes $p_d(K)$ to $d$. Notice: all parts sent by $c$ to its neighbors may not be disjointed.
In $O_{4B}$ and $O_{6B}$, there is a new concept "supporting element". **Supporting elements** refer to the elements that should be projected out in the answer tuples but are needed for later usage, especially as filters of ACPs to determine the safe peers. In $O_{4B}$ and $O_{6B}$, without help of tuple annotations, it is necessary to keep supporting elements within the answer tuples during the answer routing process.

In $O_5$, the notation "$K_i \times \{L_i\}$" is mainly intended for logical correctness. It doesn't necessarily mean to attach each answer tuple $t$ in $K_i$ with $L_i$. An implementation for $O_5$, which factors away the common repeating $L_i$ for all the tuples in a set $K_i$, is entirely consistent with this notation. Likewise the explanation works for "$A \times \{L\}$" in $O_3$.

In order to make $O_i$ ($i=1..6$) work well, there are necessary obligations for peers in the PDMS:

- For $O_1$, $\forall$ peer $c$ (except the source peer $a$) who receives/has an answer set $Q(D)$: $c$ correctly routes $Q(D)$ to the previous peer in path $P$. The target peer $b$ correctly annotates the answer set $Q(D)$ with the path $P$.

- For $O_{2A}$ and $O_{2B}$, $\forall$ peer $c_1$ (except the source peer $a$) who receives/has an answer set: $c_1$ correctly routes the answer set to a peer $c_2 \in P$. The target peer $b$ correctly annotates the answer set with the path $P$.

- For $O_3$, $\forall$ peer $c_1$ (except the source peer $a$) who receives/has an answer set: $c_1$ correctly routes the answer set to a peer $c_2 \in L$. The target peer $b$ correctly annotates the answer set with the list $L$.

- For $O_{4A}$ and $O_{4B}$, $\forall$ peer $c_1$ (except the source peer $a$) who receives/has an answer set: $c_1$ uses all related ACPs to correctly find a safe peer $c_2$ for the answer set, and routes the answer set to $c_2$.

- For $O_5$, $\forall$ peer $c_1$ (except the source peer $a$) who receives/has a partition $K_i$: $c_1$ correctly routes $K_i \cup L_i$ to a peer $c_2 \in L_i$. The target peer $b$ correctly partitions $Q(D)$ and annotates each partition $K_i$ with an annotation $L_i$.

- For $O_{6A}$ and $O_{6B}$, $\forall$ peer $c$ (except the source peer $a$) who receives/has a partition $K$, $\forall$ peer $d$ who is adjacent to peer $c$: $c$ uses all related ACPs to correctly compute and route $p_d(K)$ to peer $d$. 

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The combination of any strategy and any option in this section forms a full query-answering algorithm in a PDMS. In the next chapter, we will analyze the information leakage and completeness properties of each \((S, O)\) pair.
Chapter 5

Information Leakage and Completeness for (S,O) Pairs

The properties of a query-answering algorithm in a PDMS are those of an (S,O) pair. Information leakage and completeness (of the answer) are among the most important properties for an (S,O) pair.

In Section 5.1, we present the definition of information leakage (IL), the sufficient and necessary condition for IL-free, then analyze the IL-free property for all (S,O) pairs; in Section 5.2, we present the definition, the sufficient and necessary condition for completeness, then analyze the completeness property for all (S,O) pairs.

5.1 Information Leakage (IL)

The general sense of information leakage has been given in Section 3.1.1: some protected data are accessed by unauthorized subjects. Information leakage for a PDMS query-answering algorithm will be formally defined and studied in this section.

5.1.1 Definitions

Avoiding information leakage is an important security issue in the PDMS query-answering process. The information leakage we are concerned with concentrates on the query-answering process. Informally speaking, during the query-answering process under control of an (S,O) pair, if peer c happens to receive tuple t but isn’t authorized access to t, information leakage arises. Because which peer to receive a tuple is determined by an (S,O) pair, we regard infor-
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Information leakage (or no information leakage) as a runtime property of an (S,O) pair. Now let us make a formal definition for information leakage.

Definition 5.1 (Information Leakage (IL)) Given source peer a, target peer b, database D at b, query Q, (S,O) has information leakage iff (i) $\exists$ path $P_{a\rightarrow b}$ from a to b, $P_{a\rightarrow b}$ is chosen by S: S will send $Q'$ to b through $P_{a\rightarrow b}$ (S defines the rewritten query $Q'$ from Q), (ii) $\exists$ a tuple $t \in Q'(D)$, (iii) $\exists$ path $P_{b\rightarrow x}$ from b to peer x, $P_{b\rightarrow x}$ is chosen by O: O will send $t$ down that path s.t. $t \in p_c(D)$. (S,O) is IL-free iff it has no information leakage, $\forall a, b, Q$.

IL-free is defined as the negation of Information Leakage in the above definition. For clarity, we reword the IL-free definition as follows:

Definition 5.2 (IL-Free) Given source peer a, target peer b, database D at b, query Q, (S,O) has no information leakage iff (i) $\forall$ path $P_{a\rightarrow b}$ from a to b, which is chosen by S: S will send $Q'$ to b through $P_{a\rightarrow b}$ (S defines the rewritten query $Q'$ from Q), (ii) $\forall$ tuple $t \in Q'(D)$, (iii) $\forall$ path $P_{b\rightarrow x}$ from b to peer x, $P_{b\rightarrow x}$ is chosen by O: O will send $t$ down that path $\wedge \exists c$ on that path s.t. $t \in p_c(D)$. (S,O) is IL-Free iff it has no information leakage, $\forall a, b, Q$.

The expression "$t \in p_c(D)$" in the above definition needs to be explained. As mentioned in Section 4.2, "$p_c(D)$" denotes the part of database D that can be accessed by peer c. Thus, "$t \in p_c(D)$" means "tuple $t$ is computed from D and can be accessed by peer c". From the viewpoint of schema, t and D have different schemas and they are not comparable. Nevertheless, from the viewpoint of information containment, t is contained in D. Since we are discussing IL-Free in terms of information containment, we accept the expression "$t \in p_c(D)$". Another similar expression is "$Q(D) \subseteq D$". Given specific schemas of $Q(D)$ and D, there is no reason to say $Q(D) \subseteq D$. But from the viewpoint of information containment, we accept "$Q(D) \subseteq D$" as a fact.

The above discussion is based on Assumption 3 & 4 of Section 4.3. We don't discuss the cases violating these assumptions. Furthermore, we assume no caching here. As a common approach to accelerate the query-answering process, caching is useful and worth noting. Nevertheless, as a supportive approach for query-answering, caching is not in the central place. A system works smoothly without caching. So at this moment we omit caching. We leave the security problems involved in caching as future work.
5.1.2 The Sufficient and Necessary Condition for IL-Free

IL-free is a security property for an \((S, O)\) pair. However, we cannot expect to use the IL-free definition to check if an \((S, O)\) pair is IL-free. First, because the IL-free definition is based on execution, you would need to run \((S, O)\) on all possible source peers, target peers, queries, query routing paths, etc. Secondly, the IL-free definition has a tuple-based granularity, which is far different from the description of a strategy or an option. So we need a general condition that can be directly applied to the description of any \((S, O)\) pair and check if it is IL-free.

The following ideas are illuminating for finding such a condition:

- By the definitions of strategy and option, the answer tuples are computed only at the target peer, and no more tuples are created in the answer routing process. The option \(O\) determines whether to send an existing tuple to a peer, but cannot create a new tuple and send it to a peer. Thus, if peer \(c_0\) has an answer set \(T\) and option \(O\) will route the set \(T'\) from peer \(c_0\) to its neighbor \(c\), it must have \(T' \subseteq T\).

- By the definition of IL-free, if the option \(O\) sends a tuple \(t\) to some peer \(c\), \(c\) must have access to \(t\). In other words, \(O\) will send to \(c\) only the tuples that \(c\) has access to.

Based on the above observation, we propose the sufficient & necessary condition (SNC) for an arbitrary \((S, O)\) pair to be IL-free.

SNC: For an \((S, O)\) pair, \(\forall\) source peer \(a\), \(\forall\) target peer \(b\), \(\forall\) query \(Q\) at \(a\), \(\forall\) peer \(c_0\), \(\forall\) neighbors \(c\) of \(c_0\): \(c_0\) has answer set \(T\) and routes set \(T' \subseteq T\) to \(c \rightarrow T' \subseteq p_c(T)\).

Proof:

1. SNC is Sufficient. We shall show if \((S, O)\) satisfies SNC, it also satisfies the IL-free definition. Assume \((S, O)\) satisfies SNC. Given source peer \(a\), target peer \(b\), database \(D\) at \(b\), query \(Q\) at \(a\), rewritten query \(Q'\) of \(Q\) at \(b\), peer \(c_0\), \(c_0\)'s neighbor \(c\), let the answer set at peer \(c_0\) be \(T\) and the set sent to peer \(c\) be \(T' \subseteq T\). By SNC, we know \(T' \subseteq p_c(T)\). Let an arbitrary tuple \(t \in T'\). Since \(T' \subseteq p_c(T)\), it follows \(t \in p_c(T)\). By the definition of Strategy and Option, we can infer \(T \subseteq Q'(D)\). Since we also have the fact \(Q'(D) \subseteq D\) in sense of information containment, it follows \(T \subseteq D\). Applying exactly the same restriction \(p_c(\cdot)\) to both sides of this term, we get \(p_c(T) \subseteq p_c(D)\). Since we
already have \( t \in p_c(T) \) and \( p_c(T) \subseteq p_c(D) \), it follows \( t \in p_c(D) \). The expression \( t \in p_c(D) \) holds for every peer \( c \), via which tuple \( t \) is routed. And it holds \( \forall a, b, D, Q, Q', t \in Q'(D) \). By the definition of IL-free, \((S, O)\) satisfies the IL-free definition.

2. SNC is Necessary. We shall show if \((S, O)\) satisfies the IL-free definition, it also satisfies SNC. Assume \((S, O)\) is IL-free. Given source peer \( a \), target peer \( b \), database \( D \) at \( b \), query \( Q \) at \( a \), rewritten query \( Q' \) of \( Q \) at \( b \), let \( t \in Q'(D) \) be an arbitrary answer tuple. By the definition of IL-free, \( t \) is routed by \( O \) down some paths. Let \( P_{ba} \) be one of these paths. Let \( c_0 \) and \( c \) be arbitrary adjacent peers on path \( P_{ba} \) and \( c_0 \) routes \( t \) to \( c \). By the definition of IL-free, we know \( t \in p_c(D) \). Without loss of generality, \( t \) is in set \( T \subseteq Q'(D) \) at \( c_0 \), and \( t \) is in set \( T' \subseteq T \) routed from \( c_0 \) to \( c \). Since we have (i) \( T \subseteq Q'(D) \) and (ii) the fact \( Q'(D) \subseteq D \) in sense of information containment, it follows \( T \subseteq D \). There is another fact: given \( T \subseteq D, p_c(T) \) is exactly \( T \cap p_c(D) \). Since we have this fact \( T \subseteq D, t \in T, t \in p_c(D), p_c(T) \) holds for any tuple \( t \in T' \). Thus, \( T' \subseteq p_c(T) \). This expression holds \( \forall a, b, Q, c_0, c \). By the statement of SNC, \((S, O)\) satisfies SNC.

### 5.1.3 IL-Free Analysis for all \((S, O)\) pairs

In the previous section, we get the sufficient and necessary condition SNC for IL-free. An \((S, O)\) pair is IL-free, if and only if \((S, O)\) satisfies SNC.

Table 5.1 is the IL-free Result Matrix for the \((S, O)\) pairs we have designed in Chapter 4. It summarizes which \((S, O)\) pairs guarantee to be IL-free, where "Y" denotes "guarantee IL-free" and "N" denotes "may cause information leakage".

<table>
<thead>
<tr>
<th></th>
<th>( O_1 )</th>
<th>( O_{2A} )</th>
<th>( O_{2B} )</th>
<th>( O_3 )</th>
<th>( O_{4A} )</th>
<th>( O_{4B} )</th>
<th>( O_5 )</th>
<th>( O_{6A} )</th>
<th>( O_{6B} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( S_1 )</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
</tr>
<tr>
<td>( S_2 )</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
</tr>
<tr>
<td>( S_3 )</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
</tr>
<tr>
<td>( S_4 )</td>
<td>N</td>
<td>Y</td>
<td>N</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
</tr>
</tbody>
</table>

Table 5.1: IL-free Result Matrix

Let us analyze the result in the matrix by using the sufficient and necessary condition SNC. We will discuss the matrix in a column-by-column order.

First, consider \((S_1, O_1)\) and \((S_3, O_1)\). By the descriptions of \( S_1, S_3, O_1 \), the answer set is \( p_P(Q(D)) \) at each routing peer, where path \( P \in P_{a \rightarrow b} \). Let \( c_0 \) and \( c \) be adjacent peers on the reversed path of \( P \). There exists a fact: for \( c \in P \) and
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tuple set \( X, p_P(X) = p_c(p_P(X)) \). Replacing \( X \) by \( Q(D) \) in the previous term, we get \( p_P(Q(D)) = p_c(p_P(Q(D))) \). Therefore, \( p_P(Q(D)) \subseteq p_c(p_P(Q(D))) \). Since (i) \( p_P(Q(D)) \subseteq p_c(p_P(Q(D))) \) and (ii) by \( O_1 \), peer \( c_0 \) has answer set \( p_P(Q(D)) \) and routes exactly \( p_P(Q(D)) \) to \( c \), we see that \((S_1, O_1)\) and \((S_3, O_1)\) satisfy SNC.

Let us consider \((S_2, O_1)\). By \( S_2 \) and \( O_1 \), the answer set is \( p_A(Q(D)) \) at each routing peer, where \( A \) is the set of all peers in the P2P system. Let a path \( P \in \mathcal{P}_{a\rightarrow b}, c_0 \) and \( c \) be adjacent peers on the reversed path of \( P \). There exists a fact: for \( c \in P \) and tuple set \( X, p_A(X) = p_c(p_A(X)) \). Replacing \( X \) by \( Q(D) \) in this term, we get \( p_A(Q(D)) = p_c(p_A(Q(D))) \). Therefore, \( p_A(Q(D)) \subseteq p_c(p_A(Q(D))) \). Since (i) \( p_A(Q(D)) \subseteq p_c(p_A(Q(D))) \) and (ii) by \( O_1 \), peer \( c_0 \) has answer set \( p_A(Q(D)) \) and routes exactly \( p_A(Q(D)) \) to \( c \), we see that \((S_2, O_1)\) satisfies SNC.

Let us consider \((S_4, O_1)\). By \( S_4 \) and \( O_1 \), the answer set is \( Q(D) \) at each routing peer. Let a path \( P \in \mathcal{P}_{a\rightarrow b}, c_0 \) and \( c \) be adjacent peers on the reversed path of \( P \). By \( O_1 \), \( c_0 \) has the answer set \( Q(D) \) and routes exactly \( Q(D) \) to \( c \). However, there is no guarantee \( Q(D) \subseteq p_c(Q(D)) \). That is to say, \((S_4, O_1)\) doesn't satisfy SNC.

Let us consider \((S_2, O_{2A}) (i = 1, 3, 4)\). By \( S_i \) \((i = 1, 3, 4)\) and \( O_{2A} \), the answer set is \( p_P(Q(D)) \) at each routing peer, where path \( P \in \mathcal{P}_{a\rightarrow b} \). Let \( c_0 \) and \( c \) be adjacent peers on the returning path \( P' \). By \( O_{2A} \), we know \( P' \subseteq P \). Thus, \( c \in P \). There exists a fact: for \( c \in P \) and tuple set \( X, p_P(X) = p_c(p_P(X)) \). Since we already have \( c \in P \), replace \( X \) by \( Q(D) \) in the previous term, then get \( p_P(Q(D)) = p_c(p_P(Q(D))) \). Therefore, \( p_P(Q(D)) \subseteq p_c(p_P(Q(D))) \). Since (i) \( p_P(Q(D)) \subseteq p_c(p_P(Q(D))) \) and (ii) by \( O_{2A} \), peer \( c_0 \) has answer set \( p_P(Q(D)) \) and routes exactly \( p_P(Q(D)) \) to \( c \), we see that \((S_i, O_{2A}) (i = 1, 3, 4)\) satisfies SNC.

Let us consider \((S_2, O_{2A})\). By \( S_2 \) and \( O_{2A} \), the answer set is \( p_A(Q(D)) \) at each routing peer, where \( A \) is the set of all peers in the P2P system. Let \( c_0 \) and \( c \) be adjacent peers on a returning path \( P' \). Since \( A \) is the set of all peers in the P2P system, it follows \( c \in A \). There exists a fact: for \( c \in A \) and tuple set \( X, p_A(X) = p_c(p_A(X)) \). Replacing \( X \) by \( Q(D) \) in this term, we get \( p_A(Q(D)) = p_c(p_A(Q(D))) \). Therefore, \( p_A(Q(D)) \subseteq p_c(p_A(Q(D))) \). Since (i) \( p_A(Q(D)) \subseteq p_c(p_A(Q(D))) \) and (ii) by \( S_2 \) and \( O_{2A} \), peer \( c_0 \) has answer set \( p_A(Q(D)) \) and routes exactly \( p_A(Q(D)) \) to \( c \), we see that \((S_2, O_{2A})\) satisfies SNC.

Let us consider \((S_i, O_{2B}) (i = 1, 3)\). Analyzing the case exactly as \((S_i, O_{2A})\)
(i = 1, 3, 4), we will get that \((S_i, O_{2B}) (i = 1, 3)\) satisfies SNC.

Let us consider \((S_2, O_{2B})\). Analyzing the case exactly as \((S_2, O_{2A})\), we will get that \((S_2, O_{2B})\) satisfies SNC.

Let us consider \((S_4, O_{2B})\). By \(S_4\) and \(O_{2B}\), the answer set is \(Q(D)\) at each routing peer. Let \(c_0\) and \(c\) be adjacent peers on a returning path \(P'\). By \(O_{2B}\), \(c_0\) has the answer set \(Q(D)\) and routes exactly \(Q(D)\) to \(c\). However, there is no guarantee \(Q(D) \subseteq p_c(Q(D))\). Thus, \((S_4, O_{2B})\) doesn’t satisfy SNC.

Let us consider \((S_i, 0_i)\) \((i = 1, 3, 4)\). By \(S_i (i = 1, 3, 4)\) and \(0_3\), the answer set is \(p_P(Q(D))\) at each routing peer, where path \(P \in P_{a-b}\). Let \(c_0\) and \(c\) be adjacent peers on a returning path \(P'\). By \(O_3\), we know \(P' \subseteq L\) and \(L = \{c_0(p_P(Q(D))) = p_P(Q(D))\}\). Since \(c \in P' \land P' \subseteq L \land L = \{c_0(p_P(Q(D))) = p_P(Q(D))\}\), it follows \(p_0(p_P(Q(D))) = p_P(Q(D))\). Therefore, \(p_P(Q(D)) \subseteq p_0(p_P(Q(D)))\). Since (i) \(p_P(Q(D)) \subseteq p_0(p_P(Q(D)))\) and (ii) by \(O_3\), peer \(c_0\) has answer set \(p_P(Q(D))\) and routes exactly \(p_P(Q(D))\) to \(c\), we see that \((S_i, O_3) (i = 1, 3, 4)\) satisfies SNC.

Let us consider \((S_2, O_3)\). The analysis is almost the same as \((S_i, O_3) (i = 1, 3, 4)\). The only difference is: the answer set is \(p_A(Q(D))\) at each routing peer, where \(A\) is the set of all peers in the P2P system. We will get that \((S_2, O_3)\) satisfies SNC.

Let us consider \((S_i, O_4A) (i = 1..4)\) and \((S_i, O_{4B}) (i = 1..4)\). By \(O_{4A}\) or \(O_{4B}\), the answer set is always some \(A\) at each routing peer. Let \(c_0\) and \(c\) be adjacent peers on a returning path. By \(O_{4A}\) or \(O_{4B}\), we know \(p_c(A) = A\). Therefore, \(A \subseteq p_c(A)\). Since (i) \(A \subseteq p_c(A)\), (ii) by \(O_{4A}\) or \(O_{4B}\), peer \(c_0\) has answer set \(A\) and routes exactly \(A\) to \(c\), we see that \((S_i, O_{4A}) (i = 1..4)\) and \((S_i, O_{4B}) (i = 1..4)\) satisfy SNC.

Let us consider \((S_i, O_5) (i = 1..4)\). By \(O_5\), the answer set is divided into several partitions \(K_i (i = 1..n)\). Let \(L_i\) be \(K_i\)'s annotation, \(c_0\) and \(c\) be adjacent peers on a path to route \(K_i\) back. Since by \(O_5\) we know that \(L_i = \{c_0(K_i) = K_i\} \land \) peer \(c \in L_i\), it follows \(p_c(K_i) = K_i\). Then \(K_i \subseteq p_c(K_i)\). Since (i) \(K_i \subseteq p_c(K_i)\), (ii) by \(O_5\), peer \(c_0\) has answer set \(K_i\) and routes exactly \(K_i\) to \(c\), we see that \((S_i, O_5) (i = 1..4)\) satisfies SNC.

Last, let us consider \((S_i, O_{6A}) (i = 1..4)\) and \((S_i, O_{6B}) (i = 1..4)\). Let \(c_0\) and \(c\) be adjacent peers on a returning path, \(K\) be the answer set that \(c_0\) has, \(K'\) be the set that \(c_0\) routes to \(c\). By \(O_{6A}\) or \(O_{6B}\), we know \(K' = p_c(K)\). Then \(K' \subseteq p_c(K)\). Thus, \((S_i, O_{6A}) (i = 1..4)\) and \((S_i, O_{6B}) (i = 1..4)\) satisfy SNC.
5.2 Completeness

The general sense of completeness has been given in Section 3.1.1. It will be formally defined and studied in this section.

5.2.1 Definitions

Given the source peer $a$, target peer $b$, and query $Q$ at $a$, the answer set $A$ arriving at peer $a$ may be different for different $(S, O)$ pairs. The set $A$ is expected to be maximized, or Complete. Because the returned answer set $A$ is largely decided by the query-answering algorithm, the completeness is expected to be a property of an $(S, O)$ pair.

To define completeness, we need to make the following assumptions:

- As the property of an $(S, O)$ pair, completeness is independent of the query $Q$ at source peer $a$. In other words, the completeness of the answer set is not query-sensitive. If an $(S, O)$ pair has the completeness property, it ensures the completeness of the returned answer set for every query $Q$.

- As the property of an $(S, O)$ pair, completeness is independent of the source peer $a$, the target peer $b$, and the database $D$ at $b$. Whatever $a$, $b$ or $D$ is, the completeness means that the corresponding maximum answer set $A$ should be retrieved from $b$ to $a$. The completeness of the answer set is independent of the source peer and target peer, given an $(S, O)$ pair.

Firstly, let us define the Ideal Completeness:

**Definition 5.3 (Completeness I (Ideal Completeness))** Given source peer $a$, target peer $b$, database $D$ at $b$, query $Q$ at $a$, $(S, O)$ is complete for $(a, b, Q)$ iff: $\forall$ tuple $t \in p_a(Q(D))$, $\exists$ path $P$ from $a$ to $b$ $\land$ $\exists$ path $P'$ from $b$ to $a$, $S$ sends $Q'$ to $b$ $\land$ $t \in Q'(D)$ $\land$ $O$ sends $t$ to $a$ via $P'$ $\land$ $t \in p_c(D)$, $\forall$ peer $c$ on $P'$. $(S, O)$ is complete if it is complete for $(a, b, Q)$, $\forall$ $a$, $b$, $Q$.

The Ideal Completeness definition implies "maximal completeness based on soundness". In other words, it is the completeness on the condition of no information leakage. Because the condition "$t \in p_c(D)$, $\forall$ peer $c$ on $P'$" in the above definition ensures no information leakage. However, the Ideal Completeness depends on the network topology and the target peer's ACPs for other peers.
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Here we have an example for this dependency. It is shown in Figure 5.1: a is the source peer; b is the target peer; D is the database at b; b has an ACP saying that a can access all b's data; b has another ACP saying that c can access none of b's data; Q is the query put forth by a. We see that \( p_a(Q(D)) \) equals \( Q(D) \). But for the restriction of the topology and ACPs, the answer set \( Q(D) \) will be blocked at c and nothing can be routed back to a. Any \((S,O)\) cannot satisfy Completeness I, no matter how smart \((S,O)\) is.

This is not what we want. If Completeness is to be a property to distinguish \((S,O)\) pairs, another assumption needs to be made: Completeness is not affected by the network topology and ACP distribution. Now we will define another type of Completeness, which accounts for the network topology and ACP distribution:

**Definition 5.4 (Completeness II)** Given source peer a, target peer b, database D at b, query Q at a, let the ideal answer set \( L = \{ t | \exists \text{ path } P \in P_{b \rightarrow a} (t \in p_P(D)) \} \); let the returned answer set \( L' = \{ t | \exists \text{ path } P \in P_{a \rightarrow b} \exists \text{ path } P' \in P_{b \rightarrow a} (Q' \text{ is the written query of } Q \text{ defined by } S \land S \text{ transmits } Q' \text{ to } b \land t \in Q'(D) \land O \text{ routes } t \text{ to } a \text{ via } P') \} \). \((S,O)\) is complete for \((a,b,Q)\) iff \( L = L' \), \( \forall \) database D at b. \((S,O)\) is complete iff \((S,O)\) is complete for \((a,b,Q)\), \( \forall a, b, Q \).

Note that in the above definition, we have an equivalent form for the ideal answer set \( L \): \( L = \{ t | \exists \text{ path } P \in P_{b \rightarrow a} (t \in p_P(Q(D))) \} \). This form of \( L \) is more concise than the original one, and will be used in our later discussion.

The Completeness II definition likewise implies "maximal completeness based on soundness". Because it requires not only \( L \subseteq L' \) but also \( L' \subseteq L \). What differs Completeness II from Completeness I is that the former is independent of the network topology and ACP distribution. Therefore, Completeness II can be regarded as a property of an \((S,O)\) pair.

By the Completeness II definition, The ideal answer set \( L \) is independent of any \((S,O)\) pair. Thus, a fact can be inferred from the definition of Completeness.
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II:

Given the PDMS topology, the query Q, the source peer a, the target peer b and its database D. Assume (S_i, O_i) and (S_j, O_j) both satisfy Completeness II. Let L_i be the returned answer set of (S_i, O_i), and L_j be the returned answer set of (S_j, O_j), where the returned answer set is defined as L' in the Completeness II definition. Then we have L_i = L_j.

The proof for this fact is trivial. Let L be the ideal answer set as defined in Completeness II. By the definition of Completeness II, we know L_i = L and L_j = L. Therefore, we have L_i = L_j.

Because Completeness II allows us to account for the conditions imposed by the topology, throughout this thesis we consider Completeness II when we consider completeness.

5.2.2 The Sufficient and Necessary Condition for Completeness

We cannot expect to use the definition of Completeness II (as defined in the previous section) to check if an (S,O) pair satisfies Completeness II. First, L' in the Completeness II definition has an execution manner, you have to run (S,O) on all possible source peers, target peers, queries, query routing paths, etc. Secondly, both L and L' have the tuple-based granularity, which is far away from the description of a specific strategy or a specific option. So there is a need for a condition that can be easily applied to the description of any (S,O) pair and check if it satisfies Completeness II. Since (i) the ideal answer set L is independent of any (S,O), (ii) L has an equivalent form as we pointed out after the Completeness II definition, we get the following sufficient and necessary condition for checking if an (S,O) pair satisfies Completeness II.

SNC: For an (S,O) pair, ∀ source peer a, ∀ target peer b and its database D, ∀ query Q at a: the returned answer set L' at a is

\[ \bigcup_{P \in P_a(b)} p_f(Q(D)) \]

Proof:
Before proving that SNC is a sufficient and necessary condition, we need some preparation work.

(i) The fact is: if there is a path \( P \in P_{b \rightarrow a} \), there must be a path \( P' \in P_{a \rightarrow b} \), where \( P' \) is the reversed sequence of \( P \). By this fact, if \( P \) and \( P' \) are treated as sets of peers, we have \( P = P' \). Therefore, for any \( Q(D) \) and \( P \), \( pp(Q(D)) = p_{P'}(Q(D)) \).

(ii) By the definitions of set and set union, we have

\[
\bigcup_{P \in P_{a \rightarrow b}} p_{P}(Q(D)) = \{ t | \exists \text{path } P \in P_{a \rightarrow b}(t \in p_{P}(Q(D))) \}.
\]

Since we have (i) and (ii), it follows that

\[
\bigcup_{P \in P_{a \rightarrow b}} p_{P}(Q(D)) = \{ t | \exists \text{path } P \in P_{b \rightarrow a}(t \in p_{P}(Q(D))) \}.
\]

Next, let us prove that SNC is a sufficient and necessary condition for Completeness II.

1. SNC is Sufficient. We need to show if \((S, O)\) satisfies SNC, it also satisfies Completeness II. Assume \((S, O)\) satisfies SNC. Given source peer \(a\), target peer \(b\), database \(D\) at \(b\), query \(Q\) at \(a\), let \(L'\) be the answer set at \(a\) that \((S, O)\) returns. By SNC, we know

\[
L' = \bigcup_{P \in P_{a \rightarrow b}} p_{P}(Q(D)).
\]

Since we also have

\[
\bigcup_{P \in P_{a \rightarrow b}} p_{P}(Q(D)) = \{ t | \exists \text{path } P \in P_{b \rightarrow a}(t \in p_{P}(Q(D))) \},
\]

it follows \(L' = \{ t | \exists \text{path } P \in P_{b \rightarrow a}(t \in p_{P}(Q(D))) \}\). By the definition of Completeness II, the ideal answer set \(L = \{ t | \exists \text{path } P \in P_{b \rightarrow a}(t \in p_{P}(Q(D))) \}\). Since \(L' = \{ t | \exists \text{path } P \in P_{b \rightarrow a}(t \in p_{P}(Q(D))) \}\), and \(L = \{ t | \exists \text{path } P \in P_{b \rightarrow a}(t \in p_{P}(Q(D))) \}\), it follows \(L = L'\). The term \(L = L'\) holds \(\forall a, b, Q\). By the definition of Completeness II, we see that \((S, O)\) satisfies Completeness II.

2. SNC is Necessary. We need to show if \((S, O)\) satisfies Completeness II, it also satisfies SNC. Assume \((S, O)\) satisfies Completeness II. Given source peer \(a\), target peer \(b\), database \(D\) at \(b\), query \(Q\) at \(a\), let \(L\) be the ideal answer set, and \(L'\) be the answer set at \(a\) that \((S, O)\) returns. By the definition of
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Completeness II, \( L = \{ t \mid \exists \text{path} P \in P_{b \rightarrow a} (t \in p_P(Q(D))) \} \) and \( L = L' \). Thus, we have

\[
L' = \{ t \mid \exists \text{path} P \in P_{b \rightarrow a} (t \in p_P(Q(D))) \}.
\]

Since we also have

\[
\bigcup_{P \in P_{a \rightarrow b}} p_P(Q(D)) = \{ t \mid \exists \text{path} P \in P_{b \rightarrow a} (t \in p_P(Q(D))) \},
\]

it follows

\[
L' = \bigcup_{P \in P_{a \rightarrow b}} p_P(Q(D)).
\]

This equation for \( L' \) holds \( \forall a, b, D, Q \). By the description of SNC, we see that \((S,O)\) satisfies SNC. ■

5.2.3 Completeness Analysis for all (S,O) pairs

In the previous section, we get the sufficient and necessary condition SNC for Completeness II. An \((S,O)\) pair satisfies Completeness II, if and only if \((S,O)\) satisfies SNC.

Table 5.2 is the Completeness II Result Matrix for all \((S,O)\) pairs we designed in Chapter 4. It summarizes which \((S,O)\) pairs have the completeness II property, where "Y" refers to "Completeness II holds" and "N" refers to "Completeness II doesn't hold". If an \((S,O)\) pair isn’t IL-free, we skip it and fill in "-".

<table>
<thead>
<tr>
<th></th>
<th>( O_1 )</th>
<th>( O_{2A} )</th>
<th>( O_{2B} )</th>
<th>( O_3 )</th>
<th>( O_{4A} )</th>
<th>( O_{4B} )</th>
<th>( O_5 )</th>
<th>( O_{6A} )</th>
<th>( O_{6B} )</th>
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<td>Y</td>
<td>Y</td>
<td>N</td>
<td>N</td>
<td>Y</td>
<td>N</td>
<td>N</td>
</tr>
<tr>
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<td>N</td>
<td>N</td>
<td>N</td>
<td>N</td>
<td>N</td>
<td>N</td>
<td>N</td>
<td>N</td>
</tr>
<tr>
<td>( S_3 )</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>N</td>
<td>N</td>
<td>Y</td>
<td>N</td>
<td>N</td>
</tr>
<tr>
<td>( S_4 )</td>
<td>-</td>
<td>Y</td>
<td>-</td>
<td>Y</td>
<td>N</td>
<td>N</td>
<td>Y</td>
<td>N</td>
<td>N</td>
</tr>
</tbody>
</table>

Table 5.2: Completeness II Result Matrix

Let us analyze the result in the matrix by using the sufficient and necessary condition SNC. We will discuss the matrix in a column-by-column order, except \( S_2 \).

First of all, let us consider \((S_2,O_1)\) \((i = 1..6)\). By the descriptions of \( S_2 \) and \( O_1 \) \((i = 1..6)\), the answer set computed at the target peer \( b \) is \( p_A(Q(D)) \), where \( A \) is the set of all peers in the P2P system. Since answer tuples are only computed at \( b \) and no more tuples are created in the answer routing process, it follows that the returned answer set at \( a \) is \( L' \subseteq p_A(Q(D)) \). Since \( A \) is the set
of all peers in the PDMS, normally we have

$$p_A(Q(D)) \subseteq \bigcup_{P \in P_{a \rightarrow b}} p_P(Q(D)).$$

Since $L' \subseteq p_A(Q(D))$ and

$$p_A(Q(D)) \subseteq \bigcup_{P \in P_{a \rightarrow b}} p_P(Q(D)),$$

it follows

$$L' \subseteq \bigcup_{P \in P_{a \rightarrow b}} p_P(Q(D)).$$

Therefore, $(S_i, O_i)$ (i = 1..6) doesn’t satisfy SNC.

Let us consider $(S_1, O_1)$ and $(S_3, O_1)$. By the descriptions of $S_1$, $S_3$ and $O_1$, $\forall$ path $P \in P_{a \rightarrow b}$: the answer set at $b$ is $p_P(Q(D))$. Then by $O_1$, $\forall$ path $P \in P_{a \rightarrow b}$: the answer set $p_P(Q(D))$ is routed at $a$ via the reversed path of $P$. Thus, the returned answer set $L'$ at $a$ is

$$\bigcup_{P \in P_{a \rightarrow b}} p_P(Q(D)).$$

Therefore, $(S_i, O_1)$ and $(S_3, O_1)$ satisfy SNC.

Let us consider $(S_i, O_{2A})$ (i = 1, 3, 4). By the descriptions of $S_i$ (i = 1, 3, 4) and $O_{2A}$, $\forall$ path $P \in P_{a \rightarrow b}$: the answer set at $b$ is $p_P(Q(D))$. Then by $O_{2A}$, $\forall$ path $P \in P_{a \rightarrow b}$: the answer set $p_P(Q(D))$ is routed at $a$ via some path $P'$, where $P' \in P_{b \rightarrow a}$ and $P' \subseteq P$. Thus, the returned answer set $L'$ at $a$ is

$$\bigcup_{P \in P_{a \rightarrow b}} p_P(Q(D)).$$

Therefore, $(S_i, O_{2A})$ (i = 1, 3, 4) satisfy SNC.

Let us consider $(S_i, O_{2B})$ (i = 1, 3). Analyzing the case exactly as $(S_i, O_{2A})$ (i = 1, 3, 4), we will get that $(S_i, O_{2B})$ (i = 1, 3) satisfies SNC.

Let us consider $(S_i, O_3)$ (i = 1, 3, 4). By the descriptions of $S_i$ (i = 1, 3, 4) and $O_3$, $\forall$ path $P \in P_{a \rightarrow b}$: the answer set at $b$ is $p_P(Q(D))$, annotated with a safe peer list $L$. Then by $O_3$, $\forall$ path $P \in P_{a \rightarrow b}$: the answer set $p_P(Q(D))$ is routed at $a$ via some path $P'$, where $P' \in P_{b \rightarrow a}$ and $P' \subseteq P$. (Hint: In the worst case, $P'$ could be the reversed path of $P$, because $P \subseteq L$.) Thus, the returned
answer set \( L' \) at \( a \) is
\[
\bigcup_{P \in \mathcal{P}_{a \rightarrow b}} p_P(Q(D)).
\]
Therefore, \((S_i, O_3) \) (\( i = 1, 3, 4 \)) satisfy SNC.

Let us consider \((S_i, O_{4A}) \) (\( i = 1, 3, 4 \)). By the descriptions of \( S_i \) (\( i = 1, 3, 4 \)) and \( O_{4A}, \forall \text{ path } P \in \mathcal{P}_{a \rightarrow b}: \) the answer set at \( b \) is \( p_P(Q(D)) \). By \( O_{4A}, \forall \text{ path } P \in \mathcal{P}_{a \rightarrow b}: \) the answer set \( p_P(Q(D)) \) is routed to peer \( d \) if \( p_d(p_P(Q(D))) = p_P(Q(D)) \). However, without the help of tuple annotations and supporting elements, the answer set \( p_P(Q(D)) \) might be blocked during the routing process. Thus, the returned answer set at \( a \) might be
\[
L' \subseteq \bigcup_{P \in \mathcal{P}_{a \rightarrow b}} p_P(Q(D)).
\]
Therefore, \((S_i, O_{4A}) \) (\( i = 1, 3, 4 \)) doesn’t satisfy SNC.

Let us consider \((S_i, O_{4B}) \) (\( i = 1, 3, 4 \)). The analysis is similar with that of \((S_i, O_{4A}) \) (\( i = 1, 3, 4 \)). The only difference is as follows. By \( O_{4B}, \forall \text{ path } P \in \mathcal{P}_{a \rightarrow b}: \) the answer set \( p_P(Q(D)) \cup S \) might be blocked at some peer \( c \), where \( S \) per se cannot be safely accessed by \( c \). Therefore, \((S_i, O_{4B}) \) (\( i = 1, 3, 4 \)) doesn’t satisfy SNC.

Let us consider \((S_i, O_5) \) (\( i = 1, 3 \)). By the descriptions of \( S_i \) (\( i = 1, 3 \)) and \( O_5, \forall \text{ path } P \in \mathcal{P}_{a \rightarrow b}: \) the answer set at \( b \) is \( p_P(Q(D)) \). Then by \( O_5, \forall \text{ path } P \in \mathcal{P}_{a \rightarrow b}: \) the answer set \( p_P(Q(D)) \) is partitioned and routed back at \( a \) via some paths. (Hint: In the worst case, \( p_P(Q(D)) \) cannot be partitioned and is routed back to \( a \) via the reversed path of \( P \).) Thus, the returned answer set \( L' \) at \( a \) is
\[
\bigcup_{P \in \mathcal{P}_{a \rightarrow b}} p_P(Q(D)).
\]
Therefore, \((S_i, O_5) \) (\( i = 1, 3 \)) satisfy SNC.

Let us consider \((S_4, O_5) \). By the descriptions of \( S_4 \) and \( O_5, \forall \text{ path } P \in \mathcal{P}_{a \rightarrow b}: \) the answer set at \( b \) is \( Q(D) \). By \( O_5, Q(D) \) is partitioned and routed. Notice that only the subset \( p_P(Q(D)) \) is possible to be routed back to \( a \), where \( P \in \mathcal{P}_{a \rightarrow b} \). Thus, the returned answer set \( L' \) at \( a \) is
\[
\bigcup_{P \in \mathcal{P}_{a \rightarrow b}} p_P(Q(D)).
\]
Therefore, \((S_4, O_5) \) satisfies SNC.
Let us consider \((S_i, O_{6A})\) \((i = 1, 3)\). By the descriptions of \(S_i\) \((i = 1, 3)\) and \(O_{6A}\), \(\forall\) path \(P \in P_{a \rightarrow b}\): the answer set at \(b\) is \(p_P(Q(D))\). By \(O_{6A}\), \(\forall\) path \(P \in P_{a \rightarrow b}\): peer \(c\), who has the subset \(K \subseteq p_P(Q(D))\), routes \(p_d(K)\) to peer \(d\). However, without the help of tuple annotations and supporting elements, some answer tuples in \(p_P(Q(D))\) might be blocked/lost during the routing process. Thus, the returned answer set at \(a\) might be

\[
L' \subseteq \bigcup_{P \in P_{a \rightarrow b}} p_P(Q(D)).
\]

Therefore, \((S_i, O_{6A})\) \((i = 1, 3)\) doesn’t satisfy SNC.

Let us consider \((S_4, O_{6A})\). By the descriptions of \(S_4\) and \(O_{6A}\), \(\forall\) path \(P \in P_{a \rightarrow b}\): the answer set at \(b\) is \(Q(D)\). However, by \(O_{6A}\), the problem of no tuple annotations and no supporting elements still exists. Some answer tuples might be blocked during the routing process. Therefore, \((S_4, O_{6A})\) doesn’t satisfy SNC.

Let us consider \((S_i, O_{6B})\) \((i = 1, 3, 4)\). It is similar to the case of \((S_i, O_{6A})\) \((i = 1, 3, 4)\). Even with help of supporting elements, \(O_{6B}\) might block/lost some answer tuples during the routing process, if the supporting elements per se cannot be safely accessed by a routing peer. Therefore, \((S_i, O_{6B})\) \((i = 1, 3, 4)\) doesn’t satisfy SNC.
Chapter 6

Cost Analysis for (S, O) pairs

Thus far, we presented the designed strategies and options in Chapter 4, and the IL-free and Completeness property analysis for all (S, O) pairs in Chapter 5. But the cost related to each (S, O) pair has not been studied.

In this chapter, we build the cost model for an (S, O) pair (Section 6.1), conduct the cost analysis for all (S, O) pairs (Section 6.2), and compare the analysis to hypothesize which (S, O) pairs perform the best under which conditions (Section 6.3).

6.1 The Cost Model

A cost model estimates the cost of the query-answering process in a PDMS, in control of an (S, O) pair. The following are the assumptions for the cost model:

- We only consider the cost for given one source peer and one target peer. The cost estimation can be extended to a general case with one source peer and multiple target peers.

- We assume that databases residing on all peers have the same schema. As mentioned in Section 3.4, the access control issue is orthogonal to the issue of schema heterogeneity. Tackling query-answering among different peer schemas is the main task of previous research work in PDMSs (Section 2.1), which is beyond the scope of the thesis.

- In the cost model, we do not count in the cost of Answer Generating, which is the cost for the target peer to compute answer tuples for a query upon its local database. The reason of not including the cost lies in that (1) this cost is mandatory for every (S, O) pair, and the costs
are similar and nondistinctive, (2) answer generating is a local task, whose time cost is fairly low comparing to those of the networking transaction.

Under the above assumptions, there are several major tasks in the query answering process of a PDMS:

- Query Transmitting: transmit a query $Q$ from the source peer $a$ to the target peer $b$.
- Query Rewriting: rewrite a query $Q$ using ACPs when it is transmitted from the source peer $a$ to the target peer $b$.
- ACP Evaluation: use ACPs to determine if a peer has access to certain answer tuples.
- Answer Routing: ship answer tuples back to the source peer $a$.
- ACP Distributing: distribute ACPs from the target peer $b$ to other appropriate peers.
- Annotating: associate every partition of the answer tuples with a specific annotation.
- Annotation Shipping: ship annotations together with the "pure" answer tuples back to the source peer $a$.

Now let us identify the primitive operations and the corresponding cost unit for each task. In order to find reasonable primitive operations and cost unit for each major task, the following approximation assumptions need to be made.

Assumption 1: The numbers of constraints in different ACPs do not differ too much.

Assumption 2: Using each constraint for a query rewriting will cost approximately constant time.

Assumption 3: Using each constraint as a filter to determine whether a peer has access to an answer tuple will cost approximately constant time.

Assumption 4: In a PDMS, the time to transmit a message between any two adjacent peers is approximately constant. Thus, it takes approximately equal time for a small size message to be transmitted between any two
Chapter 6. Cost Analysis for (S,O) pairs

adjacent peers. Of course, networking costs do differ, but they are small enough that the differences are dominated by the other factors.

Assumption 5: The sizes of different answer tuples do not differ too much.

Assumption 6: The sizes of different ACPs do not differ too much.

Assumption 7: The sizes of different annotations do not differ too much.

Assumption 8: An annotation is in the form of a set of peer ID's. Inserting/deleting an peer ID into/from an annotation costs approximately constant time.

Assumption 9: The sizes of a query and its rewritten forms do not differ too much.

Assumption 10: An annotation is directly associated and shipped with a set of tuples. It requires no supportive structure.

Each of the following cost is the time cost for a major task in the query answering process of a PDMS.

The Query Transmitting Cost refers to the cost of transmitting a query Q from the source peer a to the target peer b. According to Assumption 4 and 9, it can be inferred that the cost of shipping a query down one network link is approximately an constant time. “Shipping a query down one network link” is then the primitive operation. We identify the cost unit as “query-hop”, which is the charge associated with the primitive operation. Thus the Query Transmitting Cost can be measured in terms of query-hops.

The Query Rewriting Cost refers to the cost of rewriting a query Q using ACPs when it is transmitted from the source peer a to the target peer b in the framework of an (S,O) pair. According to Assumption 1 and 2, it can be inferred that rewriting query Q using ACP A1 will cost approximately equal time to that of rewriting query Q using ACP A2, no matter what Q is, or what A1 and A2 are. So the primitive operation for query rewriting can be regarded as “rewriting a query using one ACP”. We identify the cost unit as “qrewrite-acp”, which is the charge associated with the previous primitive operation. Thus the Query Rewriting Cost can be measured in terms of qrewrite-acps. E.g. rewriting 1 query using 100 ACPs costs 100 qrewrite-acps, which has the same cost of rewriting 2 queries using 50 ACPs each.
Chapter 6. Cost Analysis for \((S, O)\) pairs

The ACP Evaluation refers to using ACPs to determine if a peer is authorized to access certain answer tuples. It happens in two different places: (1) when certain answer tuples are to be routed from peer \(c_1\) to peer \(c_2\), related ACPs are used at \(c_1\) to determine if \(c_2\) is authorized to access these answer tuples, (2) ACPs are used as filters at a peer, usually the target peer, to decide the set of peers that is authorized to access each answer tuple. According to Assumption 1 and 3, it can be inferred that evaluating an ACP over a tuple costs approximately constant time, no matter how the answer tuple looks like. So the primitive operation for ACP evaluation is “evaluating an ACP over an answer tuple to decide the related safe peers”. The cost unit is identified as “acp-eval”, which is the charge associated with the primitive operation. It’s measured on a per tuple basis. e.g. if we evaluated 1 ACP over 1000 tuples versus 10 ACPs over 100 tuples each, both cases incur the same cost: 1000 acp-evals. Thus the ACP Evaluation Cost can be measured in terms of acp-evals.

The Answer Routing Cost refers to the total cost of shipping answer tuples back to the source peer. According to Assumption 4 and 5, it can be inferred that the cost of shipping one answer tuple down one network link is approximately an constant time. “Shipping one answer tuple down one network link” is then the primitive operation. We identify the cost unit as “tuple-hop”, which is the charge associated with the previous primitive operation. Thus the Answer Routing Cost can be measured in terms of tuple-hops. E.g. if 100 tuples are sent down a path of 10 links, the cost is 1000 tuple-hops, which is also the same charge if 1 tuple is sent down a path of length 1000. Note that we are considering the amount of work in the network. Actually it is faster to send 100 tuples down a path of 10 links than to send 1 tuple down a path of 1000 links. The former does the primitive operations in a concurrent way. In our cost model, we simply sum up all primitive operations as if they are done sequentially. Likewise, the assumption applies to the Query Transmitting Cost and the ACP Distributing Cost.

For certain \((S, O)\) pairs, ACPs need to be distributed from the target peer to other peers. The ACP Distributing Cost refers to such kind of distributing cost. According to Assumption 4 and 6, it can be inferred that the cost of shipping one ACP down one network link could be treated as an approximately constant time. Thus “shipping one ACP down one network link” is the primitive operation for ACP Distributing Cost. We identify the cost unit as “acp-hop”, which is the charge associated with the previous primitive operation. So the ACP Distributing Cost can be measured in terms of acp-hops. E.g. if 100
ACPs are sent down a path of 10 links, the cost we charge is 1000 acp-hops, which is the same cost if 1 ACPs are sent down a path of length 1000.

The Annotating Cost is the cost of associating every partition of the answer tuples with a specific annotation. As mentioned in Assumption 8, an annotation is in the form of a set of peer ID's. Then the task of annotating refers to the operations of inserting/deleting peer ID's into/from annotations. The primitive operation then can be treated as "insert/delete a peer ID into/from an annotation". Such an primitive operation is the atomic step for any annotating algorithm. It works for both tuple-based and partition-based algorithms, i.e. an algorithm annotating one tuple at a time or an algorithm annotating a set of tuples at a time. According to Assumption 8, the cost unit is identified as "annot-update", which is the charge associated with the aforementioned primitive operation. So the Annotating Cost can be measured in terms of annot-updates. E.g. if we insert 4 peer ID's into an annotation, then delete 2 peer ID's from another annotation, the cost we'd charge is 6 annot-updates. Generally speaking, in a specific annotating algorithm, the task of annotating is often interleaved with the following tasks:

- answer generating, i.e. computing answer tuples for a query
- ACP evaluation, i.e. using ACPs as filters to decide the peers that have access to each answer tuple in the answer set

We ignore the cost of answer generating, as mentioned at the beginning of this section. For ACP evaluation, it is included in the ACP Evaluation Cost.

In some query-answering algorithms, the annotations are routed together with the answer tuples. This will increase the workload for the whole network. This cost is called the Annotation Shipping Cost. According to Assumption 4, 7 and 10, it can be inferred that the cost of shipping one annotation down one network link can be treated as an approximately constant time. Then "shipping one annotation down one network link" is the primitive operation. The cost unit is identified as "annot-hop", which is the charge associated with the primitive operation. Thus the Annotation Shipping Cost can be measured in terms of annot-hops. E.g. if 10 annotations are sent down a path of 4 links, the cost charged is 40 annot-hops, which has the same cost if 2 annotations are sent down a path of length 20.

Now we have identified the cost unit for each major task in the cost model. Although these cost units are different from each other, we can certainly find
the relationship for some of them. For instance, "tuple-hop", "acp-hop" and "annot-hop" are quite similar. The only difference is the size of "cell" to be shipped. Coefficients can be assigned to illuminate the relationship:

- 1 tuple-hop = $c_1 \cdot \text{acp-hop}$
- 1 acp-hop = $c_2 \cdot \text{annot-hop}$

where $c_1$ and $c_2$ are application-specific coefficients. With these relationships, it is possible to sum up the costs of Answer Routing, ACP Distributing and Annotation Shipping, which helps us to calculate the best/fastest ($S,O$) pairs.

### 6.2 Cost Analysis Result

The cost model in Section 6.1 can be used to assess an ($S,O$) pair. In this section, we analyze and compare the costs for every ($S,O$) pair we already designed. Each cost presented in this section is for ONE query, ONE source peer, and ONE target peer. Because IL-free and Completeness are necessary properties for an ($S,O$) pair, only ($S,O$) pairs that are both IL-free and complete are analyzed in this section.

In the results of this section, we sum up the cost of a major task for each ($S,O$) pair, as if the primitive operations in this task are done sequentially. But in a real PMDS, we can pipeline the primitive operations, then a task takes less time.

For clarity, we define the following terminology, which is used in later discussion. Given the PDMS topology, all ACPs, the source peer $a$, the target peer $b$:

- The number of all paths from $a$ to $b$ is $|\mathcal{P}_{a-b}|$;
- Let $N_0$ be the number of all peers in the PDMS;
- Let path $P_i \in \mathcal{P}_{a-b}$ ($i = 1, \ldots, |\mathcal{P}_{a-b}|$), $N_i$ be the number of peers (except $b$) in $P_i$, or the length of $P_i$;
- When considering only one routing path in $\mathcal{P}_{a-b}$ (e.g. in $S_2$), we will use the simplified symbols: $P$ denotes the path, $N$ denotes the number of peers (except $b$) in $P$ or the length of $P$;
- If $c_j$ is a peer, let $X_j$ be the number of the target peer $b$'s ACPs for $c_j$, $d_j$ be the shortest path from the target peer $b$ to $c_j$.
• If \( P_i \) is a path, let \( X_{P_i} \) be the number of the target peer \( b \)'s ACPs, each of which is for at least one peer in \( P_i \);

• Let \( Y \) be the total number of the target peer \( b \)'s ACPs;

• If query \( Q' \) is transmitted at the target peer \( b \) via path \( P_i \in \mathcal{P}_{a\rightarrow b} \), let \( T_i \) be the number of returned answer tuples for \( Q' \) at \( b \).

### 6.2.1 Query Transmitting Cost

For Query Transmitting Cost, "Shipping a query down one network link" is the primitive operation, and the cost unit is identified as "query-hop", which is the charge associated with the primitive operation.

Table 6.1 is the matrix summarizing the Query Transmitting Cost for every \((S, O)\) pair. We do not assess the \((S, O)\) pairs, who are either not IL-free or incomplete.

<table>
<thead>
<tr>
<th>((S_i, O_i))</th>
<th>(\sum_{i=1}^{\mid \mathcal{P}_{a\rightarrow b} \mid} N_i)</th>
</tr>
</thead>
<tbody>
<tr>
<td>((S_1, O_1))</td>
<td>(\sum_{i=1}^{\mid \mathcal{P}_{a\rightarrow b} \mid} N_i)</td>
</tr>
<tr>
<td>((S_2, O_1))</td>
<td>(\sum_{i=1}^{\mid \mathcal{P}_{a\rightarrow b} \mid} N_i)</td>
</tr>
<tr>
<td>((S_3, O_1))</td>
<td>(\sum_{i=1}^{\mid \mathcal{P}_{a\rightarrow b} \mid} N_i)</td>
</tr>
</tbody>
</table>

Table 6.1: Query Transmitting Cost (unit: query-hop)

Getting the result in the matrix is not hard: by \( S_i \) or \( S_3 \) or \( S_4 \), the query \( Q \) is transmitted along every path \( P_i \in \mathcal{P}_{a\rightarrow b} \) \((i = 1, \ldots, \mid \mathcal{P}_{a\rightarrow b} \mid)\).

### 6.2.2 Query Rewriting Cost

For Query Rewriting Cost, "rewriting a query using one ACP" is the primitive operation, and the cost unit is identified as "qrewrite-acp", which is the charge associated with the primitive operation.

Table 6.2 is the matrix summarizing the Query Rewriting Cost for every \((S, O)\) pair. We do not assess the \((S, O)\) pairs, who are either not IL-free or incomplete.

As a fact, Query Rewriting Cost is related only to strategies, not to options.

By \( S_1 \), the query \( Q \) is transmitted along every path \( P_i \in \mathcal{P}_{a\rightarrow b} \) \((i = 1, \ldots, \mid \mathcal{P}_{a\rightarrow b} \mid)\); \( Q \) is rewritten at every peer \( c_j \) \((j = 1, \ldots, N_i)\) on path \( P_i \), using \( X_j \) ACPs. Thus, the query rewriting cost for \((S_1, O_1)\) is \(\sum_{i=1}^{\mid \mathcal{P}_{a\rightarrow b} \mid} \sum_{j=1}^{N_i} X_j \) qrewrite-acps.
Chapter 6. Cost Analysis for (S, O) pairs

\[
\begin{array}{|c|c|c|}
\hline
(S_1, O_i) & \sum_{i=1}^{p_{a-b}} \sum_{j=1}^{n_i} X_j \\
(S_2, O_i) & - \\
(S_3, O_i) & \sum_{i=1}^{p_{a-b}} \sum_{j=1}^{n_i} X_j \\
(S_4, O_i) & 0 \\
\hline
\end{array}
\]

Table 6.2: Query Rewriting Cost (unit: qrewrite-acp)

The case of S_3 is similar to that of S_1. The only difference is that S_3 rewrites the query Q when it is transmitted at the target peer b. Thus, the query rewriting cost for (S_3, O_i) is also \(\sum_{i=1}^{p_{a-b}} \sum_{j=1}^{n_i} X_j\) qrewrite-acps.

By S_4, the query Q is never rewritten. Thus, the query rewriting cost for (S_4, O_i) is 0 qrewrite-acp.

### 6.2.3 ACP Evaluation Cost

For ACP Evaluation Cost, “evaluating an ACP over an answer tuple to decide the related safe peers” is the primitive operation, and the cost unit is identified as “acp-eval”, which is the charge associated with the primitive operation.

Table 6.3 is the matrix summarizing the ACP Evaluation Cost for every (S, O) pair. We do not assess the (S, O) pairs, who are either not IL-free or incomplete. We will go through the matrix entries column by column.

\[
\begin{array}{|c|c|c|c|c|}
\hline
O_1 & O_{2A} & O_{2B} & O_3 & O_{4A} & O_{4B} \\
\hline
S_1 & 0 & 0 & 0 & \sum_{i=1}^{p_{a-b}} (T_i \cdot (Y - X_{P_i})) & - & - \\
S_2 & - & - & - & - & - & - \\
S_3 & 0 & 0 & 0 & \sum_{i=1}^{p_{a-b}} (T_i \cdot (Y - X_{P_i})) & - & - \\
S_4 & - & \sum_{i=1}^{p_{a-b}} (T_i \cdot Y) & - & \sum_{i=1}^{p_{a-b}} (T_i \cdot (Y - X_{P_i})) & - & - \\
\hline
O_5 & O_{5A} & O_{5B} \\
\hline
S_1 & \sum_{i=1}^{p_{a-b}} (T_i \cdot Y) & - & - \\
S_2 & - & - & - \\
S_3 & \sum_{i=1}^{p_{a-b}} (T_i \cdot Y) & - & - \\
S_4 & \sum_{i=1}^{p_{a-b}} (T_i \cdot Y) & - & - \\
\hline
\end{array}
\]

Table 6.3: ACP Evaluation Cost (unit: acp-eval)

Let us consider (S_1, O_1) \((i = 1, 3)\). By O_1, for any path \(P \in P_{a-b}\), the answer set at b is routed via the reversed path of P. Thus, there is no ACP evaluation cost for (S_1, O_1) \((i = 1..3)\).

Let us consider (S_1, O_{2A}) \((i = 1, 3)\). By S_1 \((i = 1, 3)\) and O_{2A}, we know that for any path \(P \in P_{a-b}\), the query at b can be directly evaluated and the answer
set is routed via some path $P'$, where $P' \in \mathcal{P}_{b \rightarrow a} \cap \mathcal{P}' \subseteq \mathcal{P}$. Thus, there is no ACP evaluation cost for $(S_i, O_{2A})$ ($i = 1, 3$).

Let us consider $(S_4, O_{2A})$. By $S_4$, for any path $P \in \mathcal{P}_{a \rightarrow b}$, $Q(D)$ computed from $Q$ is not exactly $p_P(Q(D))$, which is the answer set $O_{2A}$ will route back. Thus, $O_{2A}$ needs to evaluate every ACP over every tuple in $Q(D)$ to decide the returned answer set. Since we know (i) for every path $P \in \mathcal{P}_{a \rightarrow b}$, the number of tuples in $Q(D)$ is $T_i$ and (ii) the total number of the target peer's ACPs is $Y$, it follows the ACP evaluation cost is $\sum_{i=1}^{\|\mathcal{P}_{a \rightarrow b}\|} (T_i \cdot Y)$.

Let us consider $(S_i, O_{2B})$ ($i = 1, 3$). By $O_{2B}$, for any path $P \in \mathcal{P}_{a \rightarrow b}$, the answer set at $b$ is directly computed by the query $Q$ at $b$ and routed via some path $P'$, where $P' \in \mathcal{P}_{b \rightarrow a} \cap \mathcal{P}' \subseteq \mathcal{P}$. Thus, there is no ACP evaluation cost for $(S_i, O_{2B})$ ($i = 1, 3$).

Let us consider $(S_i, O_3)$ ($i = 1, 3, 4$). By $O_3$, for every $P \in \mathcal{P}_{a \rightarrow b}$, we know (1) a query $Q$ is transmitted at the target peer $b$, and the number of answer tuples is $T_i$, (2) for each answer tuple $t$, every ACP of $b$ needs to be evaluated over $t$, except the $X_{P_i}$ ACPs for the peers in $P_i$ (They have been evaluated over $t$). Thus, the ACP evaluating cost for $(S_i, O_3)$ ($i = 1, 3, 4$) is $\sum_{i=1}^{\|\mathcal{P}_{a \rightarrow b}\|} (T_i \cdot (Y - X_{P_i}))$.

Let us consider $(S_i, O_5)$ ($i = 1, 3, 4$). By $O_5$, we know that for every incoming path, for every tuple $t$ in the answer set, each ACP of the target peer needs to be evaluated over $t$. Thus, the ACP evaluation cost is $\sum_{i=1}^{\|\mathcal{P}_{a \rightarrow b}\|} (T_i \cdot Y)$, where $T_i$ is the number of answer tuples at the target peer and $Y$ is the total number of the target peer's ACPs. However, this is the theoretical cost. In practice, the implementation of $O_5$ may annotate (partition) the answer set before the answer tuples are computed, and the ACP evaluation cost for $(S_i, O_5)$ ($i = 1, 3, 4$) will decrease dramatically.

### 6.2.4 Answer Routing Cost

For Answer Routing Cost, "shipping one answer tuple down one network link" is the primitive operation, and the cost unit is identified as "tuple-hop", which is the charge associated with the primitive operation.

Table 6.4 is the matrix summarizing the Answer Routing Cost for every $(S, O)$ pair. We do not assess the $(S, O)$ pairs, who are either not IL-free or incomplete. We will go through the matrix entries column by column.

Let us consider $(S_i, O_1)$ ($i = 1, 3$). By $O_1$ and $S_i$ ($i = 1, 3$), for any path $P_i \in \mathcal{P}_{a \rightarrow b}$, the answer set is returned via the reversed path of $P_i$. Since the number of tuples in the answer set is $T_i$ and the length of $P_i$ is $N_i$, it follows
Chapter 6. Cost Analysis for (S, O) pairs

<table>
<thead>
<tr>
<th>O₁</th>
<th>O₂A</th>
<th>O₂B</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \sum_{i=1}^{m} (T_i \cdot N_i) )</td>
<td>( \sum_{i=1}^{m} (T_i \cdot n_i), n_i \leq N_i )</td>
<td>( \sum_{i=1}^{m} (T_i \cdot n_i), n_i \leq N_i )</td>
</tr>
<tr>
<td>S₁</td>
<td>S₂</td>
<td>S₃</td>
</tr>
<tr>
<td>( \sum_{i=1}^{m} (T_i \cdot N_i) )</td>
<td>( \sum_{i=1}^{m} (T_i \cdot n_i), n_i \leq N_i )</td>
<td>( \sum_{i=1}^{m} (T_i \cdot n_i), n_i \leq N_i )</td>
</tr>
<tr>
<td>S₄</td>
<td>-</td>
<td>-</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>O₃</th>
<th>O₄ ( \cdot ) A ( \cdot ) B</th>
<th>O₅</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \sum_{i=1}^{m} (T_i \cdot n_i) )</td>
<td>( \approx \sum_{i=1}^{m} {k[1-(ck)^n]/(1-ck) \cdot T_i} )</td>
<td>( \approx \sum_{i=1}^{m} {k[1-(ck)^n]/(1-ck) \cdot T_i} )</td>
</tr>
<tr>
<td>S₁</td>
<td>( \sum_{i=1}^{m} (T_i \cdot m_i) )</td>
<td>( \sum_{i=1}^{m} (T_i \cdot m_i) )</td>
</tr>
<tr>
<td>S₂</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>S₃</td>
<td>( \sum_{i=1}^{m} (T_i \cdot m_i) )</td>
<td>( \sum_{i=1}^{m} (T_i \cdot m_i) )</td>
</tr>
<tr>
<td>S₄</td>
<td>-</td>
<td>-</td>
</tr>
</tbody>
</table>

Table 6.4: Answer Routing Cost (unit: tuple-hop)

that the answer routing cost for \((S_i, O_1)\) \((i = 1, 3)\) is \( \sum_{i=1}^{m} (T_i \cdot N_i) \).

Let us consider \((S_i, O_{2A})\) \((i = 1, 3, 4)\) and \((S_i, O_{2B})\) \((i = 1, 3)\). By \(O_{2A}, O_{2B}\) and \(S_i\), we know for any path \(P_i \in \mathbb{P}_{a-b}\), the answer set is returned via \(P'_i \subseteq P_i\). Since the number of tuples in the answer set is \(T_i\) and the length of \(P_i\) is \(N_i\), it follows that the answer routing cost for \((S_i, O_{2A})\) \((i = 1, 3, 4)\) and \((S_i, O_{2B})\) \((i = 1, 3)\) should be \( \sum_{i=1}^{m} (T_i \cdot n_i), n_i \leq N_i \).

Let us consider \((S_i, O_3)\) \((i = 1, 3, 4)\). By \(S_i\) and \(O_3\), for every path \(P_i \in \mathbb{P}_{a-b}\) (length of \(P_i\) is \(N_i\)), the answer set is annotated with annotation \(L_i\) at the target peer and returned via path \(P'_i \subseteq L_i\). Let \(m_i\) be the length of path \(P'_i\). Since the number of tuples in the answer set is \(T_i\), it follows that the answer routing cost for \((S_i, O_3)\) \((i = 1, 3, 4)\) is \( \sum_{i=1}^{m} (T_i \cdot m_i) \). Normally, \(m_i \leq N_i\).

Before turning to \((S_i, O_5)\) \((i = 1, 3, 4)\), Let us study \((S_i, O_{4A})\) and \((S_i, O_{4B})\) \((i = 1, 3, 4)\). Although \((S_i, O_{4A})\) and \((S_i, O_{4B})\) \((i = 1, 3, 4)\) cause either information leakage or incompleteness, the analysis for \((S_i, O_{4A})\) and \((S_i, O_{4B})\) \((i = 1, 3, 4)\) helps to find the cost of \((S_i, O_5)\) \((i = 1, 3, 4)\). By \(O_{4A}\) and \(O_{4B}\), for any path \(P_i \in \mathbb{P}_{a-b}\), for every peer \(c_1\) that received the answer set \(A_i\); \(A_i\) is routed from \(c_1\) to \(c_2\) if \(p_{c_2}(A_i) = A_i\). Let \(k\) be the average fanout of a peer (average number of neighbors of a peer), \(c\) be a coefficient between 0 and 1 (the average reduction factor of a peer’s “safe” neighbor number over all its neighbor number), \(n\) is the average length of an answer routing path. It is not hard to
see the number of peers receiving $A_i$ is the sum of a geometric sequence: $k, ck^2, c^2k^3, \ldots, c^n k^{n+1}$. The sum is $k[1-(ck)^n]/(1-ck)$. Since the number of tuples in the answer set $A_i$ is $T_i$, it follows the answer routing cost is approximately $\sum_{i=1}^{\|P_a\|-1} \{k[1-(ck)^n]/(1-ck) \cdot T_i\}$.

Let us consider $(S_i, O_5)$ ($i = 1, \ldots, 4$). By $O_5$, the answer set is partitioned and routed back to the source peer. In a global view, the answer routing cost in this case, in terms of “tuple-hops”, has no difference from the case of routing the answer set as a whole in $(S_i, O_{4A})$ and $(S_i, O_{4B})$ ($i = 1, 3, 4$). Thus, we'd like to adopt the approximate costs for $(S_i, O_{4A})$ and $(S_i, O_{4B})$ ($i = 1, 3, 4$), i.e., $\approx \sum_{i=1}^{\|P_a\|-1} \{k[1-(ck)^n]/(1-ck) \cdot T_i\}$.

### 6.2.5 ACP Distributing Cost

For ACP Distributing Cost, “shipping one ACP down one network link” is the primitive operation, and the cost unit is identified as “acp-hop”, which is the charge associated with the primitive operation.

Table 6.5 is the matrix summarizing the ACP Distributing Cost for every $(S, O)$ pair. We do not assess the $(S, O)$ pairs, who are either not IL-free or incomplete.

<table>
<thead>
<tr>
<th></th>
<th>$O_1$</th>
<th>$O_{2A}$</th>
<th>$O_{2B}$</th>
<th>$O_3$</th>
<th>$O_{4A,4B}$</th>
<th>$O_5$</th>
<th>$O_{6A,6B}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$S_1$</td>
<td>$\sum_{i=1}^{N_a} (X_i \cdot d_i)$</td>
<td>$\sum_{i=1}^{N_b} (X_i \cdot d_i)$</td>
<td>$\sum_{i=1}^{N_a} (X_i \cdot d_i)$</td>
<td>$\sum_{i=1}^{N_b} (X_i \cdot d_i)$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
</tr>
<tr>
<td>$S_2$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
</tr>
<tr>
<td>$S_3$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
</tr>
<tr>
<td>$S_4$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
<td>$-4 \cdot X_5$</td>
</tr>
</tbody>
</table>

Table 6.5: ACP Distributing Cost (unit: acp-hop)

An ACP of the target peer $b$ for peer $c$ is distributed only to $c$ if it is needed, not to any other peer. Only such ACP distribution cost is considered. On the other side, if peer $c$'s neighbor $c_2$ has the requirement to possess ACPs for $c$, $c$ can share ACPs with $c_2$ with little cost. We don’t count in this part of cost.

The fact is: any $(S, O)$ pair requiring ACP distribution will have the same ACP distributing cost, i.e., distributing ACPs from the target peer to the relevant peers. More specifically, for $(S, O)$ requiring ACP distribution, the ACP
Chapter 6. Cost Analysis for \((S, O)\) pairs

distributing cost is \( \sum_{i=1}^{N_0} (X_i \cdot d_i) \), where \( N_0 \) is the number of all peers in the P2P system, \( X_i \) is the number of ACPs of the target peer \( b \) for peer \( c \), \( d_i \) is the distance from \( b \) to \( c \). By the descriptions of strategies and options, we know that only \( S_1 \) requires ACP distribution. Thus, the corresponding matrix entries for \( S_1 \) are \( \sum_{i=1}^{N_0} (X_i \cdot d_i) \).

### 6.2.6 Annotating Cost

For Annotating Cost, “insert/delete a peer ID into/from an annotation” is the primitive operation, and the cost unit is identified as “annot-update”, which is the charge associated with the primitive operation.

Table 6.6 is the matrix summarizing the Annotating Cost for every \((S, O)\) pair. We do not assess the \((S, O)\) pairs, who are either not IL-free or incomplete. We will go through the matrix entries column by column.

<table>
<thead>
<tr>
<th></th>
<th>( O_1 )</th>
<th>( O_{2A} )</th>
<th>( O_{2B} )</th>
<th>( O_3 )</th>
<th>( O_{4A,4B} )</th>
<th>( O_5 )</th>
<th>( O_{6A,6B} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( S_1 )</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>( \sum_{i=1}^{P_a} l_i )</td>
<td>-</td>
<td>( \sum_{j=1}^{P_a} \sum_{i=1}^{k_i} l_j )</td>
<td>-</td>
</tr>
<tr>
<td>( S_2 )</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>( S_3 )</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>( \sum_{i=1}^{P_a} l_i )</td>
<td>-</td>
<td>( \sum_{j=1}^{P_a} \sum_{i=1}^{k_i} l_j )</td>
<td>-</td>
</tr>
<tr>
<td>( S_4 )</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>( \sum_{i=1}^{P_a} l_i )</td>
<td>-</td>
<td>( \sum_{j=1}^{P_a} \sum_{i=1}^{k_i} l_j )</td>
<td>-</td>
</tr>
</tbody>
</table>

Table 6.6: Annotating Cost (unit: annot-update)

Let us consider \((S_i, O_1)\) \((i = 1, 3)\), \((S_i, O_{2A})\) \((i = 1, 3, 4)\), \((S_i, O_{2B})\) \((i = 1, 3)\). By the descriptions of \( O_1 \), \( O_{2A} \) and \( O_{2B} \), they don’t require to annotate answer tuples. Thus, the annotating cost for them is 0.

Let us consider \((S_i, O_3)\) \((i = 1, 3, 4)\). By \( O_3 \), for each path \( P_i \in P_{a \rightarrow b} \), the returned answer set is annotated with the list \( L_i \). Let \( l_i \) be the number of peer ID’s in \( L_i \). Thus, the annotating cost for \((S_i, O_3)\) \((i = 1, 3, 4)\) is the sum of \( l_i \), i.e., \( \sum_{i=1}^{P_a} l_i \).

Let us consider \((S_i, O_5)\) \((i = 1, 3, 4)\). By \( O_5 \), for each path \( P_i \in P_{a \rightarrow b} \), the returned answer set is partitioned and annotated. For a query incoming path \( P_i \in P_{a \rightarrow b} \), let \( k_i \) be the number of partitions of the answer set, \( l_i \) be the number of peer ID’s in the \( j \)-th partition. Thus, the annotating cost for \((S_i, O_5)\) \((i = 1, 3, 4)\) is \( \sum_{j=1}^{P_{a-b}} \sum_{i=1}^{k_i} l_j \).
6.2.7 Annotation Shipping Cost

For Annotation Shipping Cost, "shipping one annotation down one network link" is the primitive operation, and the cost unit is identified as "annot-hop", which is the charge associated with the primitive operation.

Table 6.7 is the matrix summarizing the Annotation Shipping Cost for every \((S, O)\) pair. We do not assess the \((S, O)\) pairs, who are either not IL-free or incomplete. We will go through the matrix entries column by column.

<table>
<thead>
<tr>
<th>(O_1)</th>
<th>(O_{2A})</th>
<th>(O_{2B})</th>
<th>(O_3)</th>
<th>(O_{4A,AB})</th>
</tr>
</thead>
<tbody>
<tr>
<td>(S_1)</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>(\sum_{i=1}^{</td>
</tr>
<tr>
<td>(S_2)</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>(S_3)</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>(\sum_{i=1}^{</td>
</tr>
<tr>
<td>(S_4)</td>
<td>-</td>
<td>0</td>
<td>-</td>
<td>(\sum_{i=1}^{</td>
</tr>
</tbody>
</table>

Table 6.7: Annotation Shipping Cost (unit: annot-hop)

Let us consider \((S_i, O_1)\) \((i = 1, 3)\), \((S_i, O_{2A})\) \((i = 1, 3, 4)\) and \((S_i, O_{2B})\) \((i = 1, 3)\). By the description of \(O_1\), \(O_{2A}\) and \(O_{2B}\), none of them requires answer annotating, thus no annotation shipping cost.

Let us consider \((S_i, O_3)\) \((i = 1, 3, 4)\). By \(S_i\) and \(O_3\), we know for every path \(P_i \in P_{a=\text{in}}\) (length of \(P_i\) is \(N_i\)), the answer set is annotated with an annotation \(L_i\) at the target peer and returned via path \(P_i' \subseteq L_i\). Let \(m_i\) be the length of path \(P_i'\). Thus, the annotation shipping cost for \((S_i, O_3)\) \((i = 1, 3, 4)\) is \(\sum_{i=1}^{|P_a|} m_i\). Normally, we expect \(m_i \approx N_i\).

Let us consider \((S_i, O_5)\) \((i = 1, 3, 4)\). There is no way to accurately quantify the annotation shipping cost in this case. However, we can do the approximation. By \(O_5\), for any path \(P_i \in P_{a=\text{in}}\), for every peer \(c_1\) that received the answer set \(A_i\) and its annotation \(L_i\): \(A_i \times \{L_i\}\) is routed from \(c_1\) to \(c_2\) if \(p_{c_2}(A_i) = A_i\). Let \(k_i\) be the average fanout of a peer (average number of neighbors of a peer), \(c_i\) be a coefficient between 0 and 1 (the average reduction factor of a peer’s “safe” neighbor number over all its neighbor number), \(n_i\) is the average length of an answer routing path. It is not hard to see the number of peers receiving \(A_i \times \{L_i\}\) is the sum of a geometric sequence: \(k_i^2, c_i k_i^2, \),
Chapter 6. Cost Analysis for (S,0) pairs

\[ c_i^2 k_i^3 \cdots c_i^n k_i^{n+1} \]  The sum is \( k_i [1 - (c_i k_i)^{n_i}] / (1 - c_i k_i) \). Let the number of partitions (annotations) be \( p_i \). Thus, the annotation shipping cost is approximately \( \sum_{i=1}^{p_i} \{ k_i [1 - (c_i k_i)^{n_i}] / (1 - c_i k_i) \cdot p_i \} \).

### 6.3 Hypothesis for Best (S,O) pairs

Now let us make the hypothesis on which (S,O) pairs are the best in (1) being IL-free and complete as proved in Chapter 5, (2) fastest one as estimated by the results in Section 6.2.

First, \((S_4, O_1)\) and \((S_4, O_{2B})\) are excluded because they are not IL-free. Besides, \((S_2, O_j) (j = 1, 6)\), \((S_1, O_{4A}) (i = 1, 4)\), \((S_1, O_{4B}) (i = 1, 4)\), \((S_i, O_{6A}) (i = 1, 4)\), \((S_i, O_{6B}) (i = 1, 4)\) are excluded because they are not complete.

Next let us pick out the best (S,O) pairs according to each major cost:

- **Query Transmitting Cost** is non-discriminative, because this cost for each (S,O) pair is exactly the same.
- **For Query Rewriting Cost**, the best (S,O) pairs are \((S_4, O_i) (i = 2A, 3, 5)\).
- **For ACP Evaluating Cost**, the best (S,O) pairs are \((S_1, O_j) (j = 1, 2A, 2B)\), \((S_3, O_j) (j = 1, 2A, 2B)\).
- **For Answer Routing Cost**, the best (S,O) pairs are \((S_i, O_{2A}) (i = 1, 3, 4)\) and \((S_i, O_{2B}) (i = 1, 3)\). \((S_i, O_3) (i = 1, 3)\) cost at the same level of those best (S,O) pairs.
- **For ACP Distributing Cost**, the best (S,O) pairs are \((S_3, O_j) (j = 1, 2A, 2B, 3, 5)\) and \((S_4, O_j) (j = 2A, 3, 5)\).
- **For Annotating Cost**, the best (S,O) pairs are \((S_i, O_1) (i = 1, 3), (S_i, O_{2A}) (i = 1, 3)\) and \((S_i, O_{2B}) (i = 1, 3)\).
- **For Annotation Shipping Cost**, the best (S,O) pairs are \((S_i, O_1) (i = 1, 3), (S_i, O_{2A}) (i = 1, 3, 4)\) and \((S_i, O_{2B}) (i = 1, 3)\).

In the above list, \((S_3, O_{2A})\) and \((S_3, O_{2B})\) are always among the best, except for the Query Rewriting Cost. As we know, query rewriting is done at peers locally, and is normally faster than the network transportation, such as query transmitting and answer routing. Thus, if the local computing speed of peers in a PDMS is much faster than the network transportation speed, \((S_3, O_{2A})\) and
(S₃, O₂B) perform better than any other (S, O) pair. Notice that when S₃ is used, given source peer a, target peer b, database D at b, query Q that has been transmitted at b via some path \( P \in P_{a \rightarrow b} \), we have \( p_P(Q(D)) = Q(D) \). That means, (S₃, O₂A) and (S₃, O₂B) behave exactly the same. Therefore, if the local computing speed of peers in a PDMS is much faster than the network transportation speed, (S₃, O₂A) is the best (S, O) pair.

Another notable point is: if the local computing speed of peers in a PDMS is much faster than the network transportation speed, (S₃, O₂A) may not always be the best/fastest (S, O) pair. If the local computing speed of peers in a PDMS is much faster than the network transportation speed, Answer Routing Cost is the major cost and really matters. From the above bullets, we know that (Sᵢ, O₃) (i = 1, 3) perform fairly well at answer routing, though they are not among the best (S, O) pairs according to most other costs. Given a good PDMS topology and ACP distribution, (Sᵢ, O₃) (i = 1, 3) could be the best (S, O) pairs, even faster than (S₃, O₂A).
Chapter 7

Algorithm Details

We have implemented the strategies and options that can be combined to form an (S, O) pair being both IL-free and complete. They are S1, S3, S4, O1, O2A, O2B, O3, and O5. In this chapter, we present the crucial algorithms in these strategies and options.

7.1 Algorithm for Query-Rewriting in light of ACPs

By the descriptions of S1 and S3 in Section 4.4, during the query transmitting process controlled by these two strategies, a query is rewritten into a new query at some peer to adhere to ACPs defined by the target peer. Therefore, the algorithm for query-rewriting in light of ACPs plays the central role in S1 and S3. We present this algorithm in Section 7.1.1, and illustrate it by an example in Section 7.1.2.

7.1.1 Algorithm Description

Given a query Q and an ACP R, the intuition of the query rewriting algorithm is to rewrite Q into a new query Q' such that Q' satisfies any structure/value constraint in either Q or R. In another word, for any database, the answer for Q' is contained by both the answer for Q and the answer for R, where Q, Q', R are treated as tree pattern queries. According to the query containment concept in Section 2.2, we have Q' ⊆ Q and Q' ⊆ R. In our algorithm, the containment mapping approach is used to ensure these query containment relationships.

First, let us go through some terminology that will be used in the algorithm. Let Q be a query, R be an ACP. Both Q and R can be expressed as tree patterns. For a tree pattern, there exists an output node that means only instances corresponding to this output node are returned as the answer set. The output element in query Q is called return element, and the output element in ACP
Chapter 7. Algorithm Details

$R$ is called visible element. There are two types of edges in a tree pattern, i.e., $pc$ (parent-child) edge and $ad$ (ancestor-descendant) edge. Secondly, we assume no more than two nodes in $R$, or the extension form of $R$, have the same tag name. That is the ACP fragment our algorithm currently handles.

The algorithm for Query-Rewriting in light of ACP is shown in Figure 7.1.

Let us explain more on few steps of the algorithm. In step 3 of the algorithm, it requires that the schema $scm$ is available, at least for all the ancestors and descendants of visible nodes in $TP.R$. In step 6, it ensures that the nodes in $TP.R.ext$, which are attached with new constraints in step 5 (b), must be in the range of mapping $M$. Because the nodes in $TP.Q.ext$ with the original constraints are in the domain of $M$ (in fact, every node in $TP.Q.ext$ is in the domain of $M$), thus their mapped nodes in $TP.R.ext$ to accept these constraints are in the range of $M$. So these nodes will not be pruned in step 6 according to the second condition.

As mentioned earlier, the algorithm ensures $Q \supseteq Q'$ and $R \supseteq Q'$. $Q \supseteq Q'$ because there exists a containment mapping from the tree pattern of $Q$ to the tree pattern of $Q'$ ($TP.R.ext$), as described in step 5. $R \supseteq Q'$ because there is a obvious containment mapping from the tree pattern of $R$ to the tree pattern of $Q'$ ($TP.R.ext$) since all we've done is adding elements to $TP.R.ext$.

7.1.2 Example

Let us use an example to illustrate the algorithm in the previous section. In our example, the output nodes in tree patterns are capitalized.

The database schema $scm$ and the results after each step of the algorithm are shown in later figures.

After step 1, the corresponding tree patterns of given query $Q$ and ACP $R$ are built. We directly show the tree patterns here, skipping the string expressions of $Q$ and $R$.

After step 2, $TP.R$ is marked, where marked nodes are tagged with a "$\ast\$".

After step 3, $TP.R$ is expanded to $TP.R.ext$. (Please refer to the schema $scm$.)

After step 4, $TP.Q$ is expanded to $TP.Q.ext$. (Actually nothing changes, just $TP.Q$ has been replicated as $TP.Q.ext$.)

Step 5(a) finds the obvious mapping. Because every node in $TP.Q.ext$ can be mapped and every edge is preserved. Specially, the "ad" edge "$c => b$" in $TP.Q.ext$ is mapped to a path "$c => g => f => b$" in $TP.R.ext$. The
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**Algorithm QueryRewriteACP**

**Input:** query \( Q \), ACP \( R \), database schema \( s cm \)

**Output:** the rewritten query \( Q' \), or NULL if \( Q \) cannot be rewritten in light of \( R \)

1. Let \( TP_R \) be the tree pattern of \( R \)
   - Let \( TP_Q \) be the tree pattern of \( Q \)
   - Build \( TP_R \) and \( TP_Q \)
2. Mark each element in \( TP_R \)
3. Expand \( TP_R \) to \( TP_R.\text{ext} \). \( TP_R.\text{ext} \) includes:
   1. all of \( TP_R \)
   2. all ancestors to visible nodes exposed
   3. all descendants of visible nodes exposed
4. Expand \( TP_Q \) to \( TP_Q.\text{ext} \). \( TP_Q.\text{ext} \) includes: all of \( TP_Q \)
5. Do the containment mapping related work:
   (a) Attempt to find a containment mapping \( M \), from \( TP_Q.\text{ext} \) to \( TP_R.\text{ext} \):
      Given that nodes of \( TP_R.\text{ext} \) have distinct tags, finding \( M \) is as follows:
      - Given node \( x \) in \( TP_Q.\text{ext} \): define \( h(x) = \) node \( y \) in \( TP_R.\text{ext} \) where \( x.\text{tag} = y.\text{tag} \).
      - Then test if (1) this mapping \( M \) preserves edges/paths, i.e., a “pc” edge is mapped to a “pc” edge, while an “ad” edge is mapped to a path with arbitrary number of nodes; (2) the return element \( x \) in \( TP_Q.\text{ext} \) is mapped to a node \( y \) that is a descendant of the visible element (including itself) in \( TP_R.\text{ext} \). If the test succeeds, the containment mapping \( M \) exists.
      - If the containment mapping \( M \) doesn’t exist, return NULL
   (b) Identify the constraints from \( TP_Q.\text{ext} \) and attach them to \( TP_R.\text{ext} \), after converting the variable names.
6. Prune each element \( e \in TP_R.\text{ext} \) s.t.
   1. \( e \) is not marked (see step 2)
   2. \( e \) is not in the range of \( M \) (i.e., it is not mapped to)
   3. \( TP_R.\text{ext} \) remains a tree
7. Set the return element in \( TP_R.\text{ext} \) as the mapped node of the return element in \( TP_Q.\text{ext} \)
8. Translate \( TP_R.\text{ext} \) to a query \( Q' \), and return \( Q' \)

Figure 7.1: Query-Rewriting in light of ACP Algorithm
mapping succeeds. And we can see that element $d$ in $TP.R.ext$, which is the mapped element of the return element $D$ in $TP.Q.ext$, is a child of the visible element $B$ in $TP.R.ext$.

Step 5(b) identifies the constraint "$c > 8"$ from $TP.Q.ext$ and attach it to $TP.R.ext$.

After step 6, $TP.R.ext$ is pruned. The difference is that node $g,f,e,m,n$ have been deleted because they are neither marked nor mapped to by $TP.Q.ext$. Furthermore, to keep $TP.R.ext$ a tree, the "ad" edge between $c$ and $B$ is compensated.

After step 7, the return element in $TP.R.ext$ is set as $D$.

After step 8, $TP.R.ext$ is translated into an XQuery $Q'$.
after step 2:

\[
\begin{array}{c|c}
TP_Q & TP_R \\
\hline
a & a^* \\
\hline
c (c>8) & c^* i^* \\
\hline
b & B^* \\
\hline
D & d^* \\
\end{array}
\]

after step 3:

\[
\begin{array}{c|c|c}
TP_Q & TP_R & TP_{R, ext} \\
\hline
a & a^* & a^* \\
\hline
c (c>8) & c^* i^* & c^* i^* \\
\hline
b & B^* & g \\
\hline
D & d^* & f \\
\end{array}
\]

after step 4:

\[
\begin{array}{c|c|c|c}
TP_Q & TP_Q_{ext} & TP_R & TP_{R, ext} \\
\hline
a & a & a^* & a^* \\
\hline
c (c>8) & c (c>8) & c^* i^* & c^* i^* \\
\hline
b & b & B^* & g \\
\hline
D & D & d^* & f \\
\end{array}
\]


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after step 5:

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<th>TP_R =</th>
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<td>a*</td>
</tr>
<tr>
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<td>c (c&gt;8)</td>
<td>c* i*</td>
<td>c*(c&gt;8) i*</td>
</tr>
<tr>
<td>b</td>
<td>b</td>
<td>B*</td>
<td>g</td>
</tr>
<tr>
<td>D</td>
<td>D</td>
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<td>f</td>
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after step 6:

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</tr>
<tr>
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<td>c (c&gt;8)</td>
<td>c* i*</td>
<td>c*(c&gt;8) i*</td>
</tr>
<tr>
<td>b</td>
<td>b</td>
<td>B*</td>
<td>B*</td>
</tr>
<tr>
<td>D</td>
<td>D</td>
<td>d*</td>
<td>d*</td>
</tr>
</tbody>
</table>

after step 7:

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<th>TP_Q_ext</th>
<th>TP_R =</th>
<th>TP_R_ext</th>
</tr>
</thead>
<tbody>
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<td>a</td>
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<td>a*</td>
</tr>
<tr>
<td>c (c&gt;8)</td>
<td>c (c&gt;8)</td>
<td>c* i*</td>
<td>c*(c&gt;8) i*</td>
</tr>
<tr>
<td>b</td>
<td>b</td>
<td>B*</td>
<td>B*</td>
</tr>
<tr>
<td>D</td>
<td>D</td>
<td>d*</td>
<td>D*</td>
</tr>
</tbody>
</table>
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7.2 Algorithms for $O_3$

By the description of option $O_3$ in Section 4.4, a safe peer list $L$ for the returned answer set needs to be computed. After that, the answer set is routed back via peers in $L$.

In this section, we go into the details of the safe-peer-list finding algorithm and the answer routing algorithm adopted in $O_3$.

7.2.1 Safe-Peer-List Finding Algorithm

Assume only positive ACPs are considered. The intuition of finding the safe peer list is: find the peers, each of which satisfy the intersection of the ACP sets defined by the target peer for all peers in the query incoming path. Here is an example.

\[
\begin{align*}
Q' : \\
\text{FOR } & \text{n1 IN doc("example.xml")/a,} \\
& \text{n2 IN n1/c,} \\
& \text{n3 IN n2/b,} \\
& \text{n4 IN n3/d,} \\
& \text{n5 IN n1/i} \\
& \text{WHERE xs:integer(n2)>8} \\
& \text{RETURN (n4)}
\end{align*}
\]

In Figure 7.2, $a$ is the source peer, $b$ is the target peer. $b$ defines ACPs for every other peer. There are three ACPs $R_1$, $R_2$ and $R_3$. $R_1$ is defined by $b$ for $a$ and $c_1$; $R_2$ is defined by $b$ for $a$, $c_2$ and $c_3$; $R_3$ is defined by $b$ for $a$ and $c_2$.
Suppose the query $Q$ is transmitted along the path $a \rightarrow c_1 \rightarrow c_2 \rightarrow b$. Let the rewritten query at $b$ be $Q'$. The initial safe peer list $L$ is $\{a, c_1, c_2\}$. The target peer $b$ knows that the ACP set (defined by itself) for $a$ is $S_a = \{R_1, R_2, R_3\}$, the ACP set (defined by itself) for $c_1$ is $S_{c_1} = \{R_1, R_2\}$, the ACP set (defined by itself) for $c_2$ is $S_{c_2} = \{R_2, R_3\}$, the ACP set (defined by itself) for $c_3$ is $S_{c_3} = \{R_2\}$. $b$ notices that the intersection of the ACP sets for all peers in the query incoming path is $I = S_a \cap S_{c_1} \cap S_{c_2} = \{R_2\}$ and $I \subseteq S_{c_3}$. That means, the data, which can be accessed by $a$, $c_1$ and $c_2$, can also be accessed by $c_3$. Thus, $c_3$ can be added into the safe peer list: $L = \{a, c_1, c_2, c_3\}$. Then the answer set for $Q'$ can be routed via any peer in $L$. The answer can be routed via the path $b \rightarrow c_3 \rightarrow a$, which is shorter than the path $b \rightarrow c_2 \rightarrow c_1 \rightarrow a$.

The Safe-Peer-List Finding Algorithm described by the above example is shown in Figure 7.3. For clarity, the algorithm uses two hash tables $H_1$ and $H_2$. $H_1$ is the hash table keeping all (peer ID, (ACP ID, target peer ID)) pairs, where (ACP ID, target peer ID) is the set of (ACP ID, target peer ID). $H_2$ is the hash table keeping all ((ACP ID, target peer ID), {peer ID}) pairs, where {peer ID}) is the set of peers for whom this ACP is defined by the target peer.

### 7.2.2 Answer Routing Algorithm

After the safe peer list $L$ is found, $O_3$ routes the answer set back to the source peer via peers in $L$. There exists an opportunity for $O_3$ to find a better/shorter answer routing path than the reversed path of the query incoming path. In this section, we describe the answer routing algorithm designed for $O_3$.

Because no peer in the PDMS has the complete knowledge about the PDMS topology, there is no algorithm to find the optimal answer routing path. But given the safe peer list $L$, a peer, who is routing the answer set, is able to find a "local" shortcut. Here we use an example to illustrate the idea. Please refer to Figure 7.4.

In the PDMS, $S$ is the source peer, and $T$ is the target peer. The routed answer set is accompanied with two supported structures: a stack $ST$ with the current routing peer on the stack top, a safe peer list $L$ created by the Safe-Peer-List Finding Algorithm in the previous section. When the answer set is routed from $T$, the initial status of $ST$ is a stack containing all peers in the query incoming path. In our example, the query incoming path is $S \rightarrow ... \rightarrow C \rightarrow X \rightarrow Y \rightarrow Z \rightarrow A \rightarrow ... \rightarrow T$, so the initial $ST$ is $\{S, ..., C, X, Y, Z, A, ..., T\}$.
Algorithm FindSafePeers
Input: the set $S$ of all peer IDs along the query incoming path, the database $DB_R$ of tuples $(ACP.ID, targetPeerID, peerID)$
Output: the safe peer list $L$

Let $H_1$ be the hashtable for $(peerID, [(ACP.ID, targetPeerID)])$ pairs
Let $H_2$ be the hashtable for $((ACP.ID, targetPeerID), (peerID))$ pairs

1. Traverse $DB_R$ to build $H_1$ and $H_2$
2. Initialize $L = S$
3. Let $I$ be the intersection of the ACP set $\forall \ peer \in S$
   Initialize $I$ as the key set of $H_2$
   FOR each $p \in S$
   (a) From $H_1$, get the set $S_1 = \{(ACP.ID, targetPeerID)\}$
   (b) Update $I = I \cap S_1$
   }
4. FOR each $p \in$ the key set of $H_1$
   Let $S_2$ be the set $\{(ACP.ID, targetPeerID)\}$ for $p$
   (a) Get $S_2$ from $H_1$
   (b) IF $S_2 \supset I$
   (c) Update $L = L \cup \{p\}$
   }

Return $L$

Figure 7.3: Safe-Peer-List Finding Algorithm
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Figure 7.4: Example for O₃ Answer Routing Algorithm
At the moment, the answer set is at A. The corresponding stack ST and safe peer list L is shown in Figure 7.4.

Assume there is an easy way for each peer to know its neighbor’s adjacent peers, e.g., a peer sends a message to ask its neighbors for such information. (In our implementation, we use a similar way to achieve it.) For instance, in Figure 7.4, A knows the adjacent peers of Z are \{A, Y\}. Then A can utilize some peer in L to skip a few peers in stack ST. (The naive answer routing method is to route the answer set via peers in ST one by one.) In our example, A checks the safe peer list L, finds that B is in L and one of B’s neighbor is C, which exists in stack ST. Then the answer set is routed from A to C via B. All the entries above C in stack ST is popped. By this tactic, two hops are saved. (Instead of being routed via A → Z → Y → X → C, the answer set is routed via A → B → C.) Repeat the tactic at each passing peer, until the answer set arrives at S. The O₃ Answer Routing Algorithm is formalized in Figure 7.5. In this algorithm, if such peer B can not be found, the answer set is routed to the top element (peer) of the stack ST. This ensures that the answer set will be routed back to the source peer.

Algorithm AnswerRoutingO₃
Input: stack ST, safe peer list L

1. pop a peer ID A from ST
2. IF A is the source peer{
   RETURN
}
3. find peer ID B s.t.
   (1) B is A’s neighbor
   (2) B ∈ L
   (3) B’s neighbor C ∈ ST
4. IF such B exists {
   (a) Pop all entries above C from ST
   (b) Route the answer set to C via A → B → C
}
   ELSE {
   (a) Get the top entry N of ST
   (b) Route the answer set to N
}

Figure 7.5: O₃ Answer Routing Algorithm
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7.3 Algorithms for Option 5

According to Chapter 4, option O5 partitions the answer set and associates each partition $K_i$ with an annotation $L_i$, where $L_i$ is the safe peer list for $K_i$. $K_i$ is routed via peers in $L_i$. In this section, we present the partitioning semantics and methodologies (Section 7.3.1), the data-level partitioning algorithm (Section 7.3.2) and the schema-level partitioning algorithm (Section 7.3.3).

7.3.1 Partitioning Semantics and Methodologies

Given query $Q$, the database $D$ at the target peer $b$, all ACPs of $b$ for other peers. An annotating and partitioning algorithm of $O_5$ divides the answer set $Q(D)$ into several non-intersecting partitions, and annotates each partition with a set of safe peers, which are authorized by ACPs to access tuples in the partition.

The partitioning semantics is explained by Figure 7.6.

![Figure 7.6: Answer Partitioning Semantics](image)

In the PDMS, there are three peers $a$, $b$, $c$, besides the target peer. The rectangle denotes the whole answer set $Q(D)$. The three circles separately
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denote the set of answer tuples that can be accessed by a, b, c, according to the ACPs defined by the target peer. As we see, the answer set $Q(D)$ is divided into eight non-intersecting partitions, separately attached with annotations $\{a\}$, $\{b\}$, $\{c\}$, $\{a, b\}$, $\{a, c\}$, $\{b, c\}$, $\{a, b, c\}$, $\emptyset$. Each partition is maximized and its annotation set is maximized. More specifically, after partitioning, every answer tuple $t \in Q(D)$ is put into a partition that has an annotation $S$, such that $S$ is the maximum set of safe peers for $t$. This is the semantics for partitioning and annotating.

There are two possible methods of conducting the annotating and partitioning:

**Method 1.** Interleave ACP checking with evaluation of $Q(D)$. In another words, whenever computing an answer tuple according to $Q$ and an ACP, modify this tuple's annotation. After all tuples have been computed and annotated, partition them according to their annotations.

**Method 2.** First evaluate $Q(D)$ and get the answer set. Then find an algorithm for checking all ACPs on all the answer tuples and annotating them. Finally partition tuples according to their annotations.

Method 2 relies on the supporting elements, which might have been projected out but are required to be kept in the answer tuples of $Q(D)$. However, Method 1 doesn't have such a restriction. So we choose to use Method 1 in our partitioning algorithm.

There are two types of ACPs: data-level and schema-level ACPs. Data-level ACPs do not affect the schema of answer tuples, which all adhere to the same schema; while schema-level ACPs will project on some elements and thus affect the schema of answer tuples. We will work on the data-level partitioning algorithm in Section 7.3.2 and the schema-level partitioning algorithm in Section 7.3.3.

**7.3.2 Data-level Partitioning Algorithm**

Assume all ACPs defined by the target peer are data-level ACPs. Then ACPs do not affect the schema of answer tuples. Therefore, it is easy to check if an answer tuple exists in an answer set. From this conclusion, the intuition of our data-level partitioning algorithm is as follows. Initialize the answer set as an empty set. For each computed answer tuple, check whether it exists in the
current answer set. If so, we expand its annotation to include peers associated with the current ACP; else we add the tuple to the answer set, annotating with peers associated with the current ACP. After the process, the annotation of each answer tuple is maximized. Then according to their annotations, the tuples can be grouped to form proper partitions, which have the same property as Figure 7.6. The Data-level Partitioning Algorithm is shown in Figure 7.7.

In Algorithm DataLevelPartition, step 1 and step 2 are responsible for computing and annotating answer tuples, step 3 call Procedure Grouping to form partitions. Procedure Grouping traverses the annotated answer tuples once and groups them into several partitions. Any tuple \( t \) is put into a partition with the same annotation of \( t \).

### 7.3.3 Schema-level Partitioning Algorithm

The partitioning algorithm in the previous section can only handle data-level ACPs. Now let us extend the algorithm to tackle both data-level and schema-level ACPs.

In order to partition answer tuples in different schemas, we must have a clear idea on what an answer tuple schema and an answer tuple are. An answer tuple schema is the schema of an answer tuple. It is a set of attributes. An answer tuple is a set of attribute values. More specifically, in a relational query, each answer tuple is a set of table attribute values; in an XQuery, each answer tuple is a set of user-defined variable values, if not considering result restructuring.

There is a useful relationship between two answer tuples in different schemas. We define it as a new operator, **Tuple Containment**:

**Definition 7.1 (Tuple Containment)** Let \( T_1 \) be an answer tuple and \( S_1 \) be \( T_1 \)'s schema. Given an attribute value \( v \in T_1 \), \( v.\text{attr}S_1 \) is \( v \)'s corresponding attribute \( \in S_1 \). Let \( T_2 \) be an answer tuple and \( S_2 \) be \( T_2 \)'s schema. Given an attribute value \( v \in T_2 \), \( v.\text{attr}S_2 \) is \( v \)'s corresponding attribute \( \in S_2 \). \( T_1 \) is Tuple-Contained by \( T_2 \) if and only if \( \forall v \in T_1 : \exists v \in T_2 \) s.t. \( v.\text{attr}S_1 = v.\text{attr}S_2 \). It is written as \( T_1 \subseteq T_2 \). If \( T_1 \subseteq T_2 \) and \( S_1 \subseteq S_2 \), we say \( T_1 \) is strictly Tuple-Contained by \( T_2 \), written as \( T_1 < T_2 \).

Here is an example for the Tuple Containment. The schema for answer tuple \( t \) is \((A_1, A_3)\) and \( t = (a'_1, a'_3) \); the schema for answer tuple \( t' \) is \((A_1, A_2, A_3)\) and \( t' = (a'_1, a'_2, a'_3) \). According to the tuple containment definition, we have \( t < t' \).
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Algorithm **DataLevelPartition**

Input: query \( Q \), target peer \( b \), database \( D \) at peer \( b \), all ACPs \( A_i \) (\( i = 1..k \)) of peer \( b \) for other peers.

Output: partitions of \( Q(D) \), where every answer tuple \( t \) is put into a partition that has an annotation \( A \) s.t. \( A \) is the maximal set of safe peers for \( t \).

1. Initialize the answer set \( S = \emptyset \).
2. FOR each ACP \( R \) {
   (a) Let \( S_1 \) be the peer set associated to \( R \)
       Use \( R \) to rewrite query \( Q \), and compute the answer set \( I \)
   (b) FOR each answer tuple \( t \in I \) {
        IF \( (t \in S) \) {
           i. Let \( S_0 \) be \( t \)'s current annotation
           Update \( S_0 = S_0 \cup S_1 \)
        }
        ELSE { \( /t \notin S \)
           i. Assign \( S_1 \) as \( t \)'s annotation.
           ii. Update \( S = S \cup \{t\} \).
        } //ELSE
    } //FOR
} //FOR
3. Call the procedure **Grouping** to return partitions of \( Q(D) \)

Procedure **Grouping**

Input: a set \( S \) of answer tuples with annotations

Output: partitions of these answer tuples. Each partition has an annotation, which is a set of peer IDs. Each answer tuple \( t \) is put into the only partition with the same annotation of \( t \).

1. Let \( S_1 \) be the set of tuple partitions
   Let \( S_2 \) be the set of tuple annotations
   Initialize \( S_1 = \emptyset \), \( S_2 = \emptyset \)
2. FOR each tuple \( t \in S \) {
   (a) Let \( A \) be \( t \)'s annotation
       IF \( (A \in S_2) \) {
          i. Add \( t \) to partition \( P \) where \( P \in S_1 \land P \) has annotation \( A \).
       }
       ELSE { \( /A \notin S_2 \)
          i. Add \( A \) to \( S_2 \).
          ii. Create a new partition \( P' \) with annotation \( A \) in \( S_1 \).
          iii. Add \( t \) to \( P' \).
       }
   } //FOR
3. Return \( S_1 \)

Figure 7.7: Data-level Partitioning Algorithm
Intuitively, answer tuple $t_1$ is tuple-contained by $t_2$ if and only if all information in $t_1$ is covered by $t_2$. It infers a useful conclusion: if $t_1 \prec t_2$ and $t_2$ can be accessed by peer $p$, then $t_1$ can also be accessed by $p$. With this conclusion, we design a new partitioning algorithm that extends the partitioning algorithm in the previous section to handle both data-level and schema-level ACPs. It is shown in Figure 7.8. The procedure `Grouping` called in step 3 is exactly the same as in the previous section.

An supporting data structure is required for every answer tuple in Algorithm `SchemaLevelPartition`. This data structure is called `Affected Tuple Set`. The idea is: given tuples $t_1$ and $t_2$, if $t_2 \prec t_1$, $t_2$ is put in $t_1$’s Affected Tuple Set. Therefore, a tuple $t$’s Affected Tuple Set can accurately identify which tuples’ annotations need to be modified when $t$’s annotation is modified. For example, if $t_2 \prec t_1$, then $t_2$ is in $t_1$’s Affected Tuple Set. When peer $p$ is added to $t_1$’s annotation, $p$ should also be added to $t_2$’s annotation.

For an answer tuple $t$, the intuition of the algorithm is: (1) Check whether $t$ is in the current answer set. If so, expand $t$’s annotation to include peer IDs associated with this ACP; accordingly expand the annotations of tuples identified in $t$’s Affected Tuple Set. (2) Else $t$ isn’t in the current answer set. Assign peer IDs associated with this ACP as annotation of $t$. Furthermore, check whether there exists an answer tuple $t'$ in the current answer set such that $t \prec t'$. According to our previous conclusion, the annotation of $t$ will be expanded to include peer IDs in the annotation of $t'$. (1) and (2) ensure the annotation for each answer tuple is maximized. Thus, the algorithm returns the correct partitions.
Algorithm **SchemaLevelPartition**

Input: query $Q$, target peer $b$, database $D$ at peer $b$, all ACPs $A_i$ ($i = 1..k$) of peer $b$ for other peers.

Output: partitions of $Q(D)$, where every answer tuple $t$ is put into a partition with an annotation $A$, such that $A$ is the maximal set of safe peers for $t$.

1. Initialize the answer set $S = \emptyset$.
2. FOR each ACP $R$
   
   (a) Let $S_1$ be the peer set associated to $R$.
   
   (b) Use $R$ to rewrite query $Q$, and compute the answer set $T$.
   
   (c) FOR each tuple $t \in T$
      
      i. IF $t \in S$
         
         A. Let $S_0$ be the existing annotation of $t$. Update $S_0 = S_0 \cup S_1$.
         
         B. Let $ATS$ be the Affected Tuple Set of $t$. For every tuple $t_i$ identified in $ATS$, update $t_i$'s annotation $S_{t_i} = S_{t_i} \cup S_1$.
      
      } //IF /$t \notin S$
   
   ELSE
      
      A. Assign $t$'s annotation $S_0 = S_1$.
      
      B. FOR every answer tuple $t'$, where $t' \in S$ and $t < t'$
         
         • Let $S'$ be the annotation of $t'$. Update $S_0 = S_0 \cup S'$.
         
         • Let $ATS_{t'}$ be the Affected Tuple Set of $t'$. Update $ATS_{t'} = ATS_{t'} \cup \{t\}$.
      
      } //FOR
   
   C. Add $t$ (with $S_0$) to $S$.
   
   D. Let $ATS$ be the Affected Tuple Set of $t$. Compute $ATS$. For every tuple $t_i$ identified in $ATS$, update $t_i$'s annotation $S_{t_i} = S_{t_i} \cup S_0$.
      
      } //ELSE
   
3. Call procedure **Grouping** to return partitions of $Q(D)$.

Figure 7.8: Schema-level Partitioning Algorithm
Chapter 8

Experimental Study

In Chapter 3, we introduced the information leakage and completeness problems of the query answering process in a PDMS with access control requirements. Then in Chapter 4, our solution for the problem was presented: we designed some strategies and options to handle access control. Furthermore, we built a cost model to theoretically analyze the cost for each \((S, O)\) pair that ensures IL-free and completeness in Chapter 6, where a hypothesis for best/fastest \((S, O)\) pairs are proposed by us.

In this chapter, we use experiments to verify our hypothesis for best \((S, O)\) pairs, and study the algorithm scalability. Specifically, we describe the experiment implementation in Section 8.1, compare the running time of \((S, O)\) pairs in Section 8.2, and study the scalability in different facets in Section 8.3.

8.1 Experimental Settings and Implementation

To setup the P2P networking environment, FreePastry [3] is used in our experiment. FreePastry is an open-source P2P overlay network implementation. It provides an efficient algorithm for message routing, whose complexity is \(O(\log N)\), where \(N\) is the number of nodes in the network. Moreover, user-specified applications can be easily integrated with existing FreePastry source codes. In our experiment, FreePastry version 1.4.4 is used.

As to the emulation test bed, Emulab [2] is adopted in our experiment. Emulab holds a collection of hundreds of PCs for allocation. For an experiment at Emulab, the user can freely specify the topology of a network, the type of PCs in the network, latency, bandwidth, and so on. During the experiment life cycle, the user has full control on the allocated PCs. Thus, user applications can be loaded on any PC in the experiment. In our experiment, 47 PCs in Emulab are required and allocated: 31 of them work as peers in a PDMS, and the remaining 16 as the delay nodes that controls the networking traffic shaping. Unless specified otherwise, in later experiments, the network bandwidth is 50
MB, the latency is 100 ms. The bandwidth is big enough to avoid the bottleneck, comparing with the size of query/answer messages (at most few KB each). Every PC allocated has 3.0 GHz 64-bit Xeon processor and 2 GB RAM, with Testbed version of RedHat Linux 9.0 as the operating system. Our PDMS application built on FreePastry and the database are loaded on each PC.

To the best of our knowledge, Qizx [4] is the fastest open-source Java XML query engine. So it is used in our experiment for peers to query their local XML databases. Qizx supports the standard XQuery language, and also provides Java APIs to invoke the XQuery engine. In our experiment, Qizx version 1.0 is used.

In order to make the XML databases on peers general enough, we choose XMark [1] data generator to randomly create XML data. XMark project provides a benchmark suite for users. The XMark data generator can produce random XML documents modeling an auction website. Important structure features in a typical XML document is included in an XMark-created XML document. In our experiment, we create several XML databases, whose sizes range from 10 Mb to 40 Mb.

We manually build the schema for Xmark-created XML databases and a library of 20 ACPs. We design a topology generator to randomly create the PDMS topology we need. All the strategies and options, which can be combined while keeping IL-free and Completeness properties, are implemented. The peer application, which specifies its strategy and the option, is loaded on each PC (peer) allocated by Emulab.

Our implementation is written in Java 1.5 to make it cross-platform.

### 8.2 \((S, O)\) Pair Comparison and Analysis

In this section, we experiment to compare the running time of the query-answering process controlled by \((S, O)\) pairs that are both IL-free and complete. The running time here and in the next section is for ONE source peer, ONE target peer and ONE query, which adheres to the setting of the theoretical cost analysis for an \((S, O)\) pair (Chapter 6). The first reason lies in that using the same setting, the experiment result can directly verify our theoretical cost analysis and hypothesis. The second reason is that the result for one query, one source peer and one target peer can be extended to a general case with one query, one source peer and multiple target peers, which doesn't violate our
existing conclusion.

The compared \((S,O)\) pairs include \((S_1,O_j)\) \((j = 1,2A,3,5)\), \((S_3,O_j)\) \((j = 1,2A,3,5)\), \((S_4,O_5)\). Our experiment setting is: 50Mb bandwidth, 100ms latency, 10 peers, average 2 neighbors per peer, 10M database, 1 acp defined for each peer. The PDMS topology is fixed but randomly created. For each running time value, we execute the experiment for three times and get the average value. The result is shown in Figure 8.1.

Figure 8.1(a) is the running time of the query-answering process for all \((S,O)\) pairs. We can see that \((S_i,O_3)\) \((i = 1,3,4)\) is much slower than other \((S,O)\) pairs. To clearly see which \((S,O)\) pair is the fastest, we extract the first three groups of bars and put them into 8.1(b). In this figure, we see that (1) for \(O_j\) \((j = 1,2A,3)\), \((S_3,O_j)\) is slightly faster than \((S_1,O_j)\); (2) \((S_i,O_{2A})\) \((i = 1,3)\) are faster than others. Thus, \((S_3,O_{2A})\) is the fastest among all \((S,O)\) pairs, which adheres to the hypothesis we made in Section 6.3: if the local computing speed of peers in a PDMS is much faster than the network transportation speed, \((S_3,O_{2A})\) is the best \((S,O)\) pair.

Now let us retain the setting of the previous experiment, except decreasing the network latency to 10 ms, and repeat the experiment. This time the network transportation speed is so fast that the assumption “the local computing speed of peers in a PDMS is much faster than the network transportation speed” no longer holds. So the hypothesis “\((S_3,O_{2A})\) is the best \((S,O)\) pair” may not be true. The experiment result is shown in Figure 8.2. We see that \((S_i,O_5)\) \((i = 1,3,4)\) is still much slower than other \((S,O)\) pairs. But there is no \((S,O)\) pair that is apparently faster than others.

However, as we mentioned in Section 6.3, even given the condition “the local computing speed of peers in a PDMS is much faster than the network transportation speed”, \((S_3,O_{2A})\) may not always be the best/fastest \((S,O)\) pair; if given a proper PDMS topology and ACP distribution, \((S_i,O_3)\) \((i = 1,3)\) could be the best, even faster than \((S_3,O_{2A})\). To verify the hypothesis, we conduct another experiment. The experiment setting remains the same as the first one: 50Mb bandwidth, 100ms latency, 10 peers, average 2 neighbors per peer, 10M database, 1 acp defined for each peer. But this time, the PDMS topology and ACP distribution are carefully designed to benefit \(O_3\) finding a short answer-routing path. More specifically, the topology and ACP distribution enables \(O_3\) to find a shortcut for the reversed path of the longest query incoming path, with the help of safe peers outside the query incoming path. (Otherwise \(O_3\) has to route the answer back to the source peer via the reversed query incoming path.)
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(a) the Running Time of the Query-Answering Process for All \((S, O)\) Pairs Being Compared

(b) the Running Time of the Query-Answering Process for All \((S, O)\) Pairs Being Compared, Excluding \((S_i, O_k)\) \((i = 1, 3, 4)\)

Figure 8.1: Running Time Comparison of \((S, O)\) Pairs, in case of Large Network Latency
Chapter 8. Experimental Study

Algorithm Comparison 1b.1

(a) the Running Time of the Query-Answering Process for All \((S, O)\) Pairs Being Compared

Algorithm Comparison 1b.2

(b) the Running Time of the Query-Answering Process for All \((S, O)\) Pairs Being Compared, Excluding \((S_i, O_b)\) \((i = 1, 3, 4)\)

Figure 8.2: Running Time Comparison of \((S, O)\) Pairs, in case of Small Network Latency
On the other side, the topology in this experiment doesn't benefit $O_2$ finding a shortcut for the reversed path of the longest query incoming path, i.e., if a path is treated as a set of peers, there doesn't exist an answer routing path, which is a subset of the longest query incoming path. The experiment result is shown in Figure 8.3. We can clearly see that $(S_i, O_2)$ ($i = 1, 3$) are the fastest, even faster than $(S_3, O_{2A})$.

Because $(S_i, O_3)$ ($i = 1, 3, 4$) is always much slower than other $(S, O)$ pairs and even intolerable, in the experiments on scalability we will not consider $(S_i, O_3)$ ($i = 1, 3, 4$).

8.3 Scalability Results and Analysis

In this section, we experiment on the $(S, O)$ pair scalability in different facets.

(1) Scalability on Database Size

In this experiment, we test the running time trend of the query-answering process for $(S, O)$ pairs with the change of database size on the target peer.

The experiment setting is: 50Mb bandwidth, 100ms latency, 10 peers, average 3 neighbors per peer, 1 acps per peer. In the experiment, the PDMS topology is fixed but randomly created. For each running time value, we execute the experiment for three times and get the average value. The experiment result is shown in Figure 8.4.

We can see that the running time for any $(S, O)$ pair is proportional to the database size of the target peer. The result is reasonable: normally, the database query time and the returned answer set size are linear functions of the target database size, which in turn determines the query-answering time is a linear function of the target database size.

What is the effect if we increase the network latency? As a comparison, let us retain the setting of the previous experiment, except increasing the network latency to 1000 ms, and do the experiment again for $(S_1, O_1)$. The result is shown in Figure 8.5. We can see that the running time is still approximately a linear function of the target database size, but the slope is much more flat. This result is not hard to explain: with the increase of network latency, the affect of the target database size is diluted. The total running time now is mainly decided by the network transportation, which is irrelevant to the target database size. As an ultimate case, if the local computing time is by far smaller
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Figure 8.3: Running Time Comparison of (S, O) Pairs. Under this experiment setting, the PDMS topology and ACP distribution benefit O₃ finding a short answer-routing path, but doesn’t benefit O₂A.
than the network latency, the curve for our experiment result is expected to be a horizontal line.

(2) Scalability on Number of ACPs per Peer

ACP s are defined by the target peer for other peers. In this experiment, we study the running time trend of \((S, O)\) pairs with the change of the number of ACPs defined by the target peer for each peer.

The experiment setting is: 50Mb bandwidth, 2ms latency, 10 peers, 2 neighbors per peer, 10M database. The PDMS topology is fixed but randomly created. For each running time value, we execute the experiment for three times and get the average value. The experiment result is shown in Figure 8.6. By this curve, the running time seems to be a polynomial function of the number of ACPs per peer. But it is hard for us to explain where this result comes from. So we conduct the second experiment to discover the hidden fact.

In the second experiment, we test the running time trend of \((S_1, O_1)\) with the changes of both the number of ACPs per peer and the network latency. The experiment setting is: 50Mb bandwidth, 10 peers, 2 neighbors per peer, 1M database. The result is shown in Figure 8.7. From the result curves, we see that the running time is a polynomial function of the number of ACPs per peer, and
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Figure 8.5: the Running Time of the Query-Answering Process V.S. the Database Size of the Target Peer for \((S_1, O_1)\). The network latency is 1000 ms.

The network latency is a linear function of the network latency (because the distance between each two curves approximately remains a constant, and the distance between the curve of 0 ms latency and the curve of 100 ms latency equals the distance between the curve of 100 ms latency and the curve of 200 ms latency). Hinted by the experiment result, we reach a theoretical explanation: total running time \(T = \) message transmitting time + local query evaluation time = \(2 \ast n \ast l + E \ast r^n\), where \(n\) is the longest path from source to target, \(l\) is the network latency, \(E\) is the local evaluation time for a query, \(r\) is the number of ACPs per peer. The expression \(r^n\) is the number of rewritten queries at the target peer, which is decided by \(S_1\). From the above equation, it is clear that the total running time \(T\) is a polynomial function of \(r\) and linear function of \(l\), which explains the results in Figure 8.6 and Figure 8.7.

(3) Scalability on Length of the Longest Path

The running time of the query-answering process for an \((S, O)\) pair might be largely affected by the length of the longest path for a message having a round trip between the source peer and the target peer. For \((S_1, O_2 A)\) and \((S_1, O_3)\), such a longest path is hard to decide because the answer-routing path is decided by both the topology and ACP distribution. To make our experiment clear, we
Figure 8.6: the Running Time of the Query-Answering Process V.S. the Number of ACPs per Peer for Each Compared \((S, O)\) Pair

Figure 8.7: the Running Time of the Query-Answering Process V.S. the Number of ACPs per Peer for \((S_1, O_1)\), with the Network Latency of 0 ms, 100 ms and 200 ms Separately
choose to study \((S_1, O_1)\), for whom such a longest path is simply twice the length of the longest path from the source peer to the target peer.

In this experiment, we test the running time trend of the query-answering process for \((S_1, O_1)\) with the change of length of the longest path from the source peer to the target peer. The experiment setting is: 50Mb bandwidth, 100ms latency, 1M database, 2 neighbors per peer, 1 acp per peer. Given the same setting, we do the experiment on two PDMS of different sizes: one PDMS with 20 peers and the other PDMS with 30 peers. The experiment result is shown in Figure 8.8. By the result, we see the running time is proportional to length of the longest path from the source peer to the target peer, but nearly has no relation to the number of peers in the PDMS (because the two lines overlap). This result can be also explained by the aforementioned formula: total running time \(T = \text{message transmitting time} + \text{local query evaluation time} = 2 \cdot n \cdot l + E \cdot r^n\), where \(n\) is the longest path from source to target, \(l\) is the network latency, \(E\) is the local evaluation time for a query, \(r\) is the number of ACPs per peer. In our experiment setting, \(r = 1\). Thus, \(T = 2 \cdot n \cdot l + E\). It indicates that \(T\) is proportional to \(n\).

![Figure 8.8: the Running Time of the Query-Answering Process V.S. the Length of the Longest Path from Source Peer to Target Peer for \((S_1, O_1)\). The experiment is done for both a PDMS with 20 peers and a PDMS with 30 peers.](image)
Chapter 9

Conclusions and Future Work

In this thesis, we have studied the access control issue in the XML peer data management system. To the best of our knowledge, our work is the first attempt to systematically analyze the access control problems in the PDMS. Our main contributions include:

- A formal syntax for the Access Control Policy (ACP) is proposed. The ACP syntax is fine-grained and expressive enough for specifying the access control privilege on the XML database of a peer in the PDMS. (Chapter 3)

- We design several (query transmitting) Strategies and (answer routing) Options, whose combinations form the query-answering algorithms and can handle the access control requirements in a PMDS. (Chapter 4)

- Some novel algorithms used in the strategies and options, such as (i) query rewriting algorithm in light of ACPs (ii) safe peer list finding algorithm (iii) annotating and partitioning algorithm, are designed. (Chapter 7)

- We formalize the definitions for Information Leakage Free and Completeness, which are important properties of an (Strategy, Option) pair. Furthermore, we propose the sufficient and necessary conditions for them, and analyze every (Strategy, Option) pair designed. (Chapter 5)

- We propose a cost model, which consists of the major tasks and the corresponding primitive operations and cost units. All (Strategy, Option) pairs are assessed by this cost model. (Chapter 6)

- Experiments are conducted on the designed (Strategy, Option) pairs, comparing their execution speed and testing the scalability in terms of the tar-
get peer database size, ACP amount per peer, length of the longest path from the source peer to the target peer. (Chapter 8)

There are some directions that we would like to pursue in our future work:

- In our work we assume that all peers use the same schema, which avoids adding in the complications of schema heterogeneity. In a realistic PDMS, the schema heterogeneity will force ACPs to be rewritten if they are distributed among the PDMS. And the schema heterogeneity may also affect the query-rewriting in light of ACPs algorithm.

- Caching is not discussed in the thesis. However, as a common approach to accelerate the query-answering process, caching is worth noting. If caching is used in a PDMS, we need to be more careful to avoid information leakage. The IL-free and Completeness definitions in the thesis need to be modified. And other strategies and options can be designed to utilize caching.

- Thus far, our algorithm for query-rewriting in light of ACPs can only handle one fragment of tree patterns, whose corresponding XPath is with ‘/’, ‘/’; ‘[ ]’. And it also requires that nodes of $TP.R.ext$ have distinct tags. We would like to remove the restrictions and make the algorithm to handle more general cases.
Bibliography


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