Visual Mining of Powersets with Large Alphabets

by

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Abstract

We present the PowerSetViewer visualization system for lattice-based mining of powersets. Searching for items within the powerset of a universe occurs in many large dataset knowledge discovery contexts. Using a spatial layout based on a powerset provides a unified visual framework at three different levels: data mining on the filtered dataset, browsing the entire dataset, and comparing multiple datasets sharing the same alphabet. The features of our system allow users to find appropriate parameter settings for data mining algorithms through lightweight visual experimentation showing partial results. We use dynamic constrained frequent-set mining as a concrete case study to showcase the utility of the system. The key challenge for spatial layouts based on powerset structure is in handling large alphabets, since the size of the powerset grows exponentially with the size of the alphabet. We present scalable algorithms for enumerating and displaying datasets containing between 1.5 and 7 million itemsets, and alphabet sizes of over 40,000.
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Chapter 1

Introduction

Data mining and information visualization share the same goals: identifying trends, patterns, and outliers in a sea of information. Data mining approaches these tasks through statistics approaches, while information visualization does so visually. By combining these two approaches, we can achieve their goals more efficiently and effectively.

1.1 Motivation

A database is a collection of individual items or records that alone may convey limited information to the user and may appear to be unrelated to each other. The relationships between various items or records, however, may reveal much more useful information that is critical to decision making. Identifying trends, patterns, and other hidden relationships in large databases is the core task of knowledge discovery and data mining (KDD). Data mining is “the non-trivial extraction of implicit, previously unknown and potentially useful information from data in a database” [10]. In general, data mining techniques have been successfully used in commercial domains such as managing customer relation, analyzing market baskets, and detecting credit card fraud, as well as in scientific and engineering applications.
Chapter 1. Introduction

Most data mining tasks involve exploring how objects are related to each other within a universe of objects. Primary examples include the following:

- Finding association rules and frequent sets: Association rules identify co-occurring events, and finding frequent sets is the first step in discovering them [1]. For example, in a sales transaction dataset, a typical association rule would be that a certain percentage of customers who buy milk also buy bread. A frequent set is a set of items that are frequently bought together.

- Mining sequential patterns: In many domains, such as finance, data can be ordered based on certain dimensions, for example, time or location. Identifying all the sub-sequences that appear frequently given that ordering will help us predict what will happen next [2].

- Building decision trees: Decision trees are used in classification-related problems [4]. A decision tree is a tree representation of a decision procedure for assigning a class label to a given example, which distinguishes one group from another. There is a test at each internal node of the tree with a branch corresponding to each possible outcome. At each leaf node, there is a class label. A class label is assigned to an entity by traversing a path from the root to a leaf.

- Clustering: Clustering involves dividing data into groups of similar objects [18]. Information retrieval, web analysis, customer relationship management, marketing, medical diagnostics, computational biology, and many other data mining applications require data to be clustered,
such that items in a particular cluster share certain properties.

All of the above tasks require searching for "interesting" groupings of objects within a search space, which consists of partial or all possible groupings of objects. This process is almost the same as searching sets within a powerset space, which is a collection of all possible sets. Analysts, however, may be interested not only in the individual "interesting" set, but also in the inter-set information of the individual set in the context of other "interesting" sets, or in the context of the entire powerset space. Traditional text-based data mining applications perform quite well when the cardinality of the final result is small. However, when the number of items returned by the data mining engine exceeds a certain threshold, typically 20, traditional text-based applications will probably fail to provide analysts with the contextual information that is critical to most data mining tasks. This is because the results provided by text-based applications are organized in a way that does not easily yield useful inter-set information.

Information visualization uses interactive representations, typically visual, of abstract data to facilitate its exploration and understanding. This is a complex research area involving information design, computer graphics, human-computer interaction, and cognitive science [32]. The goal of information visualization is to employ the high-bandwidth channel of the human visual system in identifying trends, clusters, gaps, and outliers. Representations offered by a well-designed information visualization application have several advantages over traditional text-based representations.

First, more information is available to the user given the same screen
space. Information provided by traditional text-base applications is limited by the size of the text [14]. To show more information on the display, we need to decrease the size of the text. However, the text becomes illegible below a certain threshold. In contrast, information visualization applications usually use marks to represent records in the original dataset, where different visual or retinal properties are used to encode record fields. Therefore, a lengthy record in the original dataset is rendered as a mark on the display. If users are interested in the original information encoded by a particular mark, they can simply move the mouse over the mark to display the detailed information in either a pop-up dialogue or a dedicated information panel.

Second, an overview of the dataset is available to the user. By allowing more data in the original dataset to be visualized at the same time, users can get an overview of the dataset, which is vital to many analysis tasks. The human visual system can quickly identify trends, pattern, or outliers in the dataset. These hidden gems are unlikely to be easily acquired by looking at thousands of lines of characters.

Last, users are able to fully interact with the data. Users may select an area of interest and zoom in to investigate local or detailed information in that area. Users can also filter out "uninteresting" data points or highlight certain "hot" data points, in order to focus their attention on interesting items.

Furthermore, some data mining tasks require a number of parameters to be set [20]. It is very likely that the final result, which takes hours if not days to obtain, is not what the user needed, due to inaccurate or inappropriate parameter settings. Offering users the ability not only to explore the search
space but also to see and steer the computation would help significantly.

1.2 Thesis Statement

The ideal visual data mining system would offer a meaningful visualization based on a huge search space without losing any important information. It would also provide users with the ability to explore in the search space, which requires at least 10 frames per second to ensure good user interaction. Moreover, it is critical for the system to maintain a "fixed" layout of groupings, since retaining the relative positions of groupings enables users to easily compare different datasets sharing the same alphabet.

1.3 Contributions

We present the contributions of our system, ordered by their significance, in this section. They will be discussed in detail in Chapter 4.

- Powerset enumeration: We propose an enumeration of powerset for PowerSetViewer (PSV) that is ordered first by cardinality, then by lexicographical ordering. Creating a spatial layout that maps a related family of datasets into the same absolute space is a powerful visualization technique that enables users to compare different datasets sharing the same alphabet. We also develop an algorithm for calculating the index of a powerset in the powerset enumeration that is linear in the cardinality of the set and independent of its size.
Chapter 1. Introduction

- **Scaling to large alphabet**: We propose new data structures and develop an algorithm that enables PSV to accommodate large alphabets of over 40,000 items, with \(2^{40000}\) potential sets in the entire powerset space.

- **Rendering and picking in PSV**: Real-time interactivity requires frame rates of at least 10-20 frames per second, which is a challenge when rendering millions of objects distributed within the sparse powerset space. PSV can handle more than six million records using our new rendering and traversal algorithm optimized for sparse data. As will be explained in Section 6.2, the rendering time is near-constant after a threshold dataset size has been reached, and this constant time is very small: 60 milliseconds per scene, allowing over 15 frames per second even in the worst case.

### 1.4 Outline of the Thesis

This chapter has presented our problem motivation, thesis statement, an overview of our approach, and our contributions. The remaining chapters of the thesis are organized as follows. Chapter 2 introduces related work. Chapter 3 provides a detailed overview of our approach and the features that are supported by PSV. Chapter 4 explains our approach in details and discusses implementation issues. Chapter 5 presents a concrete example to showcase the utility of PSV. Chapter 6 details the performance of PSV. Finally, Chapter 7 discusses future work as well as providing a conclusion that highlights the contributions of our research. This document is based in
part on a technical report coauthored by Tamara Munzner, Raymond T. Ng, Jordan Lee, Janek Klawe, Dragana Radulovic, and Carson K. Leung [22].
Chapter 2

Related Work

In this chapter, we introduce Information Visualization in Section 2.1. We then discuss related work based on three categories: database visualization systems in Section 2.2, mining results visualization systems in Section 2.3, and steerable visualization systems in Section 2.4. Finally, in Section 2.5 we introduce two other applications that are also based on the Accordion Drawing infrastructure.

2.1 Information Visualization

Information visualization bridges the two most powerful information processing systems: the human mind and the computer. It transforms data into a visual form and takes advantage of humans’ remarkable abilities in identifying trends, patterns, and outliers. Information visualization systems enable users to acquire the information they need through observation, search, navigation, and exploration of the original data. One of the challenges in information visualization is to meaningfully design spatial mapping of data that is not inherently spatial. A well-designed spatial layout will reveal useful hidden patterns that are probably not apparent in the plain representation of the original data. In addition to spatial position, information
visualization applications also take advantage of other visual channels to encode information, such as shape, size, orientation, colour, and texture [7]. However, only part of these visual encodings are helpful for a given task, which imposes another design challenge. A typical information visualization application will employ some or all of the following techniques to help users identify the information they need [25]:

- Overview: Providing an overview of the entire dataset allows users to understand its global structure.

- Zoom: Users are able to zoom in to have a detailed view of “interesting” items, which reveals some local information.

- Filter: Users can filter out “uninteresting” items.

- Detail-on-demand: Provides detailed information on selected items at the user’s request. This technique avoids potential clutter in the visualization without losing important information.

- Related: Users can view relationships among items.

Information visualization and data mining share the same ultimate goal: identifying hidden patterns in the datasets. Therefore, visualizing databases is an active research area in the field.
2.2 Database Visualization Systems

VisDB

The VisDB system [15], shown in Figure 2.1, is a visualization tool that allows users to explore large multidimensional databases in terms of a query result. It uses pixel-oriented techniques, with each record in the database represented by a single pixel or group of pixels. The VisDB system takes advantage of spatial encoding and colour to indicate the relevance of data.
items with respect to the query in order to give the user an overview of the query result. It also supports dynamic query refinement, where users can use sliders to change the parameters of the query based on the immediate visual feedback. However, VisDB only provides information about the relationship between individual items and the query. It does not offer information about relationships among items in the dataset, which is critical to most data-mining tasks. Moreover, the size of the dataset that can be accommodated in VisDB is limited by the number of pixels on screen. The current version of VisDB only allows interactive database exploration for datasets containing up to 50,000 data items [15].
2.2.1 Spotfire

Spotfire [3], as shown in Figure 2.2, is a database exploration system that employs several information visualization techniques, including dynamic queries, brushing and linking, and other interactive graphic techniques. This system focuses on visualizing the original dataset and uses a graphical interface to help users identify trends, patterns, and outliers. However, Spotfire does not provide visualization of any data-mining results. The Spotfire system also suffers from a lack of scalability and cannot handle databases that are organized using a hierarchical structure, where users are able to acquire information with different granularity.

2.2.2 Independence Diagrams

Independence diagrams [6], as shown in Figure 2.3, help users identify correlations between any two attributes in a particular database. Independence diagram systems divide each attribute into ranges. For each pair of attributes, the combination of these ranges forms a two-dimensional grid. Brightness is used to encode the number of data items within that cell. Since Independence Diagrams can show relationships between only two attributes at once, users may have to try several times before they can find the “interesting” pairs. Moreover, users are not able to find any correlations or pattern among independence diagrams. In contrast, PSV puts all of these “combinations” of dimensions into a single window, where users can identify individual interesting combinations (any two dimensions that are highly correlated or highly independent) as well as correlations or patterns among
Chapter 2. Related Work

Figure 2.3: An independence diagram with legend [6], showing a synthetic dataset. Brightness is used to encode degree of dependence. A darker region means that there are fewer items in it. The two attributes are independent, except for a range of X-attribute values, where the region is brighter.

2.2.3 Polaris

Polaris [30, 29], as shown in Figure 2.4, is an interactive visual exploration tool that facilitates exploratory analysis of multidimensional datasets with rich hierarchical information. Polaris builds a visual grid of small multiples [31] based on a user query. Polaris also provides a visual interface to help the user formulate complex queries against a multi-dimensional data cube. By taking advantage of the hierarchical structure of the data cube, Polaris allows the analyst to drill down or roll up data to get a complete overview of the entire dataset before focusing on detailed portions of it. How-
Figure 2.4: The Polaris system [30, 29]. Each chart displays profit and sales over time for a hypothetical coffee chain, organized by state.

ever, Polaris is limited to processing basic queries against the data cubes, and does not support exploring powerset space.

In summary, these four systems provide features for arranging and displaying data in various forms. However, they are not designed to display data mining results nor could they be easily modified to accommodate powerset enumeration. The PSV system allows the raw data to be visualized and explored as well as providing a unified visual framework for the user to examine data-mining results.
Figure 2.5: The PBC system [4]. Each sector shows a dimension of the original dataset, with individual data points ordered by the values of the attribute and colour coded based on the class label.

2.3 Mining Results Visualization System

2.3.1 Decision Trees

The PBC framework proposed by Ankerst et al. [4] and shown in Figure 2.5 is not a general visualization system. It focuses on involving the user in the process of building decision trees through a pixel-based multidimensional visualization technique and interaction capabilities. The system overcomes the limitation of most decision trees, that they are fixed to binary splits for numerical attributes. However, since visualization is used only as an indicator of how a split value affects the classification result, the user is not able to get any information about the individual records in the original database or the relationships among them.
2.3.2 Association Rules

The rule-visualization system developed by Han and Cercone [11] focuses on the discretization of numeric attributes and the discovery of the numerical association rules for large datasets. The system uses a two-dimensional plot to show the original datasets and parallel coordinates to show the mined association rules. However, the system takes only two attributes into consideration throughout the mining process. Once a data point is displayed, users are not able to get detailed information about individual records. In contrast, PSV allows the user to operate on all attributes of the records.

Hofmann et al. [13] use a variant of mosaic plots, called double-decker plots, to visualize association rules. Their focus is on helping users to understand association rules. PowerSetViewer, on the other hand, operates at the level of frequent sets. Furthermore, unlike the two previous frameworks, PSV supports midstream steering of the mining process. Again, the use of a spatial layout based on a powerset is unique.

2.3.3 Clustering

The visualization method developed by Koren and Harel [18] is designed for clustering analysis and validation. It integrates a dendrogram, which contains hierarchical information, and low-dimensional embedding. The leaf nodes of the dendrogram are well ordered so that similar nodes are adjacent to each other. The data points in the low-dimensional embedding are drawn exactly below the corresponding leaf node in the dendrogram so that the user is able to mentally connect the two parts, as shown in Figure 2.6. This
system is a specific visualization tool for exploring clusters and provides no information at the level of individual records. Moreover, the size of the dendrogram is limited by the number of screen pixels, which limits the utility of the system.

![Dendrogram Image](image)

Figure 2.6: The two-way visualization system for clustered data [18].

The visual metaphors of visualization systems based on data-mining results are quite different from the PSV system, which uses a spatial layout based on the powerset of an alphabet. These other systems use dots, lines, or rectangles to represent data points in the original datasets. These on-screen elements may overlap with each other when the number of data points exceeds a certain threshold. However, all of these systems are limited by their failure to offer elegant solutions to occlusion when laying out large datasets. Moreover, they do not provide users with the ability to explore the original datasets.
2.4 Steerable Visualization Systems

2.4.1 SCIRun

SCIRun [24] is a scientific programming environment that allows user to refine parameter settings at any phase of computation, based on the visual representation of the partial result. It offers users the ability to find the cause-and-effect relationships within the simulation. However, SCIRun is designed to provide volumetric representations of the data, such as medical imaging and scientific simulation, and uses a very different visual representation than that used by PSV.

2.4.2 MDSteer

MDSteer [33] is an interactive visualization tool designed to apply Multi-dimensional Scaling (MDS) to very large datasets. The user can steer the computation of the algorithm to areas of interests by creating a rectangular box on the screen. Figure 2.7 shows a partial layout after 20 seconds of interactive steering, which successfully reveals the large-scale structure.

2.4.3 Discussion

These two applications are not designed to steer data-mining engines. In contrast, PSV can be connected to a data-mining engine and allows the user to explore both the original dataset and the mining result.
2.5 Accordion Drawing

Accordion drawing is an information-visualization technique that features rubber-sheet navigation and guaranteed visibility. Rubber-sheet navigation allows the user to select and stretch out any rectangular area to show more detail in that area. This action automatically squishes the rest of the scene. All stretching and squishing happens with smoothly animated transitions, so that the user can visually track the motions with ease. Parts of the scene can become highly compressed, showing very high-level aggregate views in those regions. However, no part of the scene will ever slide out of

Figure 2.7: The MDSteer system [33], showing a partial layout of a 50,000-point S-shaped benchmark dataset. Users can steer the computation by creating boxes.
the field of view; the borders of the malleable sheet are “nailed down”. A second critical property of accordion drawing is the guaranteed visibility of visual landmarks in the scene, even if those features might be much smaller than a single pixel. Without this guarantee, a user browsing a large dataset cannot know if an area of the screen is blank because it is truly empty, or if it is blank because marks in that region happen to be smaller than the available screen resolution can show.

Accordion drawing was originally proposed for browsing phylogenetic trees [21, 5], as shown in Figure 2.8, and was then adapted for the task of visually comparing multiple aligned gene sequences [28], as shown in Figure 2.9. The powerset-based spatial layout used by PSV was another extension to the generic accordion-drawing framework[27]. This previous work focused on dense and static data, while PSV addresses sparse and dynamic data.

Figure 2.8: The TreeJuxtaposer system [21], showing a phylogenetic tree with hierarchical structure. Some subtrees are highlighted due to user interaction.
Figure 2.9: The SequenceJuxtaposer system [28], showing a set of related gene sequences. These sequences are vertically aligned for easy comparison.
Chapter 3

PSV Overview

In this chapter, we give a detailed overview of our approach. Sections 3.1.1 through 3.1.4 explain the features that are supported by our system. Section 3.2 explains the client-server architecture of PSV. Finally, Section 3.3 introduces PSVproto, an initial prototype, and its limitations.

3.1 Features

PSV provides a visual framework for examining individual powersets in the context of the entire powerset space, and also an interface where users can find appropriate parameter settings for data-mining algorithms through lightweight visual experimentation that shows partial results. This lightweight visual experimentation also shows how various parameter settings would create a filter for the mined data with respect to the entire dataset. Moreover, when the mining algorithms are steerable, dynamic display of intermediate or partial results helps the user decide how to change the parameters settings of computation in midstream. In our unified framework, we can support setting the filter parameters to let all items pass through, so that the entire input dataset is shown to the user. Another benefit of using the powerset for spatial layout is that users can meaningfully compare
images that represent two different datasets sharing the same alphabet. For example, the distribution of purchases between two chain stores in different geographic regions could be compared this way. Our system provides the following features to assist users with frequent-set mining.

3.1.1 Visual Metaphor

PSV uses the visual metaphor of accordion drawing [27] introduced in Section 2.5. Although the absolute on-screen location of an itemset changes, its relative ordering with respect to its neighbours is always preserved in both the horizontal and vertical directions. Accordion drawing also allows interactive exploration of datasets that contain many more itemsets than the fixed number of pixels available in a finite display.

3.1.2 Layout

PSV introduces a novel layout that maps a related family of datasets, those sharing the same alphabet of available items, into the same absolute space of all possibilities. That space is created by enumerating the entire powerset of a finite alphabet as a very long one-dimensional list, where every possible set has an index in that list. The linear list is wrapped scanline-style to create a two-dimensional rectangular grid of fixed width, with a small number of columns and a very large number of rows. We draw a small box representing a set if it is passed to the visualizer by the miner, located at the position in the grid corresponding to its index in this wrapped enumeration list. Without guaranteed visibility, these boxes would be much smaller than pixels in the display for alphabets of any significant size because of the exponential
Chapter 3. PSV Overview

nature of the powerset. This guarantee is one fundamental reason why PSV can handle large alphabets.

In areas where there is not enough room to draw one box for each set, multiple sets are represented by a single aggregate box. The colour of this box is a visual encoding of the number of sets that it represents using saturation: objects representing few sets are pale, and those representing many are dark and fully saturated. Colour is also used in the background to distinguish between areas where sets of different cardinality are drawn: those background regions alternate between four unobtrusive, unsaturated colours. The minimum size of boxes is controllable, from a minimum of one pixel to a maximum of large blocks that are legible even on high-resolution displays.

In this layout, seeing visual patterns in the same relative spatial region in the visualization of two different datasets means that they have similarities in their distribution in this absolute powerset space. Side by side visual comparison of two different datasets sharing the same alphabet is thus a fruitful endeavor.

3.1.3 Interaction

Interactions that can be accomplished quickly and easily allow more fluid exploration than those that require significant effort and time to carry out. The PSV design philosophy is that simple operations should only require minimal interaction overhead. Rubber-sheet navigation, where the user sweeps out a box anywhere in the display and then drags the corner of the box to stretch or shrink it, is just one example. Mouseover highlighting occurs whenever the cursor is moved, so that the box currently under the cursor
is highlighted and the names of the items in that highlighted itemset are shown in a status line below the display. Mouseover highlighting is a very fast operation that can be carried out many times each second because it does not require redrawing the entire scene. Highlighting the superset of an itemset can be done through the shortcut of a single click on the itemset’s box.

The layout and rubber-sheet navigation described above provide a spatial substrate users can explore on by colouring sets according to constraints. We do not support changes in the relative spatial position of itemsets, because it would then be impossible to usefully compare visual patterns at different times during the interaction. The underlying mechanism for colouring is to assign sets to a group that has an assignable colour. A group is a collection of sets that satisfy certain constraints. Users can create an arbitrary number of coloured groups as a mechanism for tracking the history of both visualizer and miner constraints, by saving each interesting constraint choice as a separate group. The priority of groups is controllable by the user; when a particular set belongs to multiple enabled groups, the highest priority group colour is shown.

3.1.4 Monitoring

As will be discussed in Chapter 5, the visualizer shows several important status variables, which helps the user to adjust parameter settings. These include the following:

- *Total*: The total number of itemsets in the raw dataset
Figure 3.1: PSV has a client-server architecture, with a visualizer that can show either the filtered results from the miner or the raw data directly.

- **Processed**: The number of itemsets processed so far by the miner
- **Shown**: The number of itemsets passed on to the visualizer to display
- **Rows**: The number of visualizer rows needed so far
- **Maxrow**: The biggest visualizer row needed so far

Comparing these numbers helps users make choices: for instance, *total* vs. *processed* is the progress of the miner, and *processed* vs. *shown* shows the amount of filtering done by the miner. The *rows* and *maxrow* pair shows the average distribution density of itemsets. The higher the *rows-to-maxrow* ratio, the denser the distribution, since the higher ratio means there are fewer empty rows. Comparing *shown* with *processed* gives the user feedback on whether the miner constraints should be changed to make the filter tighter or looser.
3.2 Client-Server Architecture

PSV has a client-server architecture, as shown in Figure 3.1. The server is a steerable data-mining engine, the miner, that is connected through sockets with a client visualization module, the visualizer, that handles graphical display. The visualizer client includes interface components for controlling both itself and the miner server. The client and server communicate using a simple text protocol: the client sends control messages to the server. The miner sends partial results to the visualizer as they are completed, allowing the user to monitor progress.

3.3 PSVproto

PSVproto, an initial prototype of PSV, had been implemented when the research for this thesis began. The server-side mining engine was first developed by Carson Leung and was then modified by Dragana Radulovic so that the engine could communicate with the visualizer through plain text protocol. The client-side of PSVproto was developed by Jordan Lee. Figure 3.4 shows the original PSVproto interface. The top section is the rendering window, which supports Accordion Drawing navigation. The lower control panel allows users to communicate with the data-mining engine. In addition to the main control panel and rendering window, PSVproto also provides users with the following panels:

- Grouping panel: As shown in Figure 3.2, users can select a group of items satisfying the supplied constraints and highlight them for further
Chapter 3. PSV Overview

Figure 3.2: The grouping panel of PSVproto. [19]

Figure 3.3: The visualization panel of PSVproto. [19]
exploration.

- Visualization panel: As shown in Figure 3.3, users can turn on the background colour so that sets with different cardinalities can be easily identified.

![Figure 3.4: The interface of the PSV prototype. [19]](image)

Those features supported by PSVproto offers users a powerful tool to explore datasets. However, PSVproto still suffers from the following limitations:
Chapter 3. PSV Overview

- **Enumeration**: The prototype uses a brute-force algorithm to calculate the index of a set in the entire powerset enumeration. Given a set $s$, the algorithm traverses the powerset space from the very beginning of the enumeration until it encounters $s$. On average, computing the index of a set takes 40 milliseconds with this approach. Since the operation is performed every time a set comes into PSVproto, it is not ideal for processing very large datasets.

- **Scalability**: The PSV prototype cannot display a dataset with an alphabet size larger than 30 items [19]. Since the PSV prototype uses the plain `Integer` type variable as the index of a set in the powerset enumeration, the size of the alphabet is in turn limited by the maximum value of the `Integer`, which is $2^{31}$.

- **Rendering**: Since the PSV prototype cannot handle a dataset with an alphabet size larger than 30 items, rendering is not efficient. The PSV prototype employs a quad-tree data structure. A quad-tree is very similar to a binary tree, but any node in a quad-tree can contain up to four children. The quad-tree maintains a hierarchical structure of the rendering window, where each leaf node corresponds to a set returned by the server. Since we subdivide the screen as we are traversing from the root to a leaf node, a large portion of the screen space will not be used, since the distribution of the sets is extremely sparse. Therefore, quad-tree is not an ideal data structure for rendering any mid-size or large-size datasets. Moreover, it takes PSVproto half a second to render a scene that contains only a few thousand items.
The aforementioned limitations of PSVproto makes it unsuitable for processing most real-world datasets, whose alphabet sizes exceed its limit of 30 items. In the next chapter, we will explain how PSV is designed to overcome these limitations.
Chapter 4

Approach

As discussed in Chapter 3, our approach can be divided into three parts. The first part is to map each set to a box on the display, where the relative positions of the sets should be maintained. The second part is to build and maintain related data structures to support fast rendering and navigation. The last part is to render the sets on screen. In this chapter, we discuss these three parts in detail in sections 4.1 to section 4.3 respectively. In section 4.4, we explain how PSV is designed to handle datasets with large alphabets.

4.1 Mapping

Mapping is the process of finding the position of a set in the enumeration of powersets and using an on-screen box to represent it, so that the relative position of the set with respect to other sets is maintained.

4.1.1 Challenges

A meaningful ordering of the powerset is critical to the data-mining task, because useful hidden patterns will be made available if a meaningful ordering of the powerset is chosen. Moreover, each set that comes into PSV will go through the mapping process. Therefore, an appropriate yet efficient
algorithm is required to map each set to a position on the screen.

4.1.2 Our Approach

There are many ways to enumerate powersets, but when visually represented most do not yield a helpful mental model. The enumeration we use is ordered first by cardinality, then by lexicographic ordering. All singleton sets are shown before the two-sets, two-sets before the three-sets, and so on. The steerable data-mining engine that motivated this application uses an underlying lattice structure, so first sorting by cardinality is a good match. Within a given cardinality, we choose a lexicographic ordering for alphabet items, again to match the powerset traversal order of many lattice-based mining algorithms. For example, an alphabet of \( \{a, b, \ldots, z\} \) yields the enumeration \( \{a\}, \{b\}, \ldots, \{z\}, \{ab\}, \{ac\}, \ldots, \{yz\}, \{abc\}, \ldots \) We assume that the underlying alphabet has a canonical lexicographic ordering; for example, \( a = 1, b = 2, \ldots, z = 26 \). Another design guideline was to choose a single spatial layout and allow users to find patterns by changing the colours of data elements. If we used spatial proximity to show membership of some chosen element, for example by grouping sets containing the element \( b \), the layout would change drastically and visual patterns from different times could not be meaningfully compared. Rubber-sheet navigation can change the absolute position of boxes in space while preserving the relative ordering of marks in all directions. All computations involving sets assume that their internal item ordering is also lexicographically sorted.

The mapping from a set to a box that is drawn in a display window has two main steps:
• convert from an \( m \)-set \( \{s_1, \ldots, s_m\} \) to its index \( e \) in the enumeration of the powerset

• convert from the enumeration index \( e \) to a \((row, column)\) position in the grid of boxes

We present an efficient \( O(m) \) algorithm for the first stage of computing an enumeration index \( e \) given an arbitrary set. The second stage is straightforward: \( row \) is \( e \) divided by the width of the grid, and \( column \) is \( e \) modulo the width. We start with an example of computing the enumeration index \( e = 1206 \) of the \( 3 \)-set \( \{d,h,k\} \) given an alphabet of size 26.

Given a particular \( m \)-set, the computation of the index in the enumeration of the powerset is done in two steps. The first step is to compute the total number of \( k \)-sets, for all \( k < m \). These are all the sets with a strictly smaller cardinality. For the \( \{d,h,k\} \) example, the first step is to compute the total number of 1-sets and 2-sets, which is given by
\[
\binom{26}{1} + \binom{26}{2} = 26 + 325 = 315.
\]
The general formula, where \( A \) is the size of the alphabet, is
\[
\sum_{i=1}^{m-1} \binom{A}{i}.
\]

The second step is to compute the number of sets between the first \( m \)-set in the enumeration and the particular \( m \)-set of interest. For the \( \{d,h,k\} \) example, the second step computes three terms:

• the number of 3-sets beginning with the 1-prefixes \( \{a\}, \{b\}, \text{ or } \{c\} \):
\[
\binom{26-1}{2} + \binom{26-2}{2} + \binom{26-3}{2} = 300 + 276 + 253 = 829.
\]
Picking \( a \) as a 1-prefix leaves 2 other choices that yield a 3-set containing \( a \); there are 25 other items left in the alphabet from which to choose 2. Similarly,
when $b$ is then picked as the 1-prefix, there are only 24 choices left; since the $m$-set is internally ordered lexicographically, neither $a$ nor $b$ is still available as a choice.

- the number of 3-sets beginning with 2-prefixes \{d, e\}, \{d, f\}, or \{d, g\}, which is given by $\binom{26}{1}^5 + \binom{26}{1}^6 + \binom{26}{1}^7 = 21 + 20 + 19 = 60$; and

- the number of 3-sets between the 3-prefixes \{d, h, i\} and \{d, h, j\}, which is $\binom{26}{0}^2 + \binom{26}{0}^3 = 1 + 1 = 2$.

This example suggests a formula of

$$\sum_{i=1}^{m} \sum_{j=p_{i-1}+1}^{p_i-1} \binom{A-j}{m-i}$$

where $p_i$ is the lexicographic index of the $i$th element of the $m$-set and $p_0$ is 0. In the worst case, the number of terms required to compute this sum is linear in the size of the alphabet. However, we can collapse the inner sum to be just two terms by noticing that

$$\sum_{i=0}^{j} \binom{n-i}{k} = \binom{n+1}{k+1} - \binom{n-j}{k+1}.$$

We derive this lemma using the identity $\binom{n}{k} = \binom{n-1}{k} + \binom{n-1}{k-1}$. The general formula is thus given by

$$\sum_{i=1}^{m} \left[ \binom{A-p_{i-1}}{m-i+1} - \binom{A-p_{i+1}}{m-i+1} \right] \quad (4.1)$$

Combining these two steps, we can compute the enumeration index as

$$\sum_{i=1}^{m-1} \binom{A}{i} + \sum_{i=1}^{m} \left[ \binom{A-p_{i-1}}{m-i+1} - \binom{A-p_{i+1}}{m-i+1} \right] \quad (4.2)$$
The complexity of computing the index of a set can be reduced to $O(m)$, where $m$ is the cardinality of the set, by using a lookup table instead of explicitly calculating \( \binom{n}{k} \). We compute such a table of size $n \times k$ using dynamic programming in a preprocessing step. As we will discuss in Section 4.4.2, the maximum set size $k$ needed for these computations is often much less than the alphabet size $n$, but we do not want to hardwire any specific limit on maximum set size. Our time-space tradeoff is to use the lookup table for the common case of small $k$, 25 in our current implementation, and explicitly compute the binomial coefficient for the rare case of a large $k$.

### 4.1.3 Knuth’s Algorithm

As discussed in Section 4.1.1, an efficient enumeration algorithm yielding a meaningful visualization is essential to PSV. In this section, we present an alternative enumeration algorithm proposed by Donald E. Knuth to explore the possibilities of employing different enumeration methods in PSV [16]. We will compare Knuth’s approach with ours in terms of both complexity and usefulness.

Knuth’s algorithm uses the following formula to calculate the index of an arbitrary $m$-set in the powerset enumeration:

$$
\sum_{i=1}^{m-1} \binom{A}{i} + \sum_{i=1}^{m} \binom{p_{i} - 1}{i}
$$

where $A$ is the size of the alphabet and $p_{i}$ is the lexicographic index of the $i$th element of the $m$-set [16]. This algorithm has the same complexity as

$^{1}$Background material for this approach is discussed in Volume 4 of *The Art of Computer Programming* [17].
Figure 4.1: Two visualizations with different enumeration functions. Top visualization uses our approach while bottom one uses Knuth's algorithm. These two enumeration methods give very similar distributions.
ours but the resulting enumeration does not strictly follow the lexicographic order. For example, given an alphabet of \{a, b, c, d, e\}, the set \{b, c, d\} comes before \{a, b, e\}. However, this enumeration has a nice property: any \(m\)-set that contains \(a_i\) comes after all \(m\)-sets that are generated using \(\{a_1, a_2, \ldots, a_{i-1}\}\), where \(a_i\) is the \(i\)th element in the alphabet. This process is especially useful when the alphabet size keeps increasing over time, since the newly generated powersets will be appended at the end of the powerset enumeration, leaving the layout of the exiting sets untouched. As shown in Figure 4.1, Knuth's approach and ours give two very similar visualizations of the enrollment dataset, which will be introduced in Section 5.1.

### 4.2 SplitLine Hierarchy

Once the index in the enumeration of an itemset has been calculated, we need to create boundaries, which we discuss next.

#### 4.2.1 Challenges

All itemsets will be laid out in a 2-D grid, where each box that represents an itemset is bounded by four movable lines, which we call SplitLines. Rubber-sheet navigation is accomplished by moving the SplitLines. The full powerset space is extremely large. For example, for a database that has an alphabet size of 50 items, the total number of powersets is \(1.12 \times 10^{15}\), which, considering the memory requirements, makes it impossible to create all SplitLines beforehand. Moreover, for alphabets of any significant size, the screen space allocated to each of the boxes would be much smaller than a
pixel in the display because of the cardinality of the powerset. To guarantee visibility, we need to maintain some aggregation information for use by the rendering engine at the rendering stage.

### 4.2.2 Our Approach

As shown in Figure 4.2 Left, SplitLines are boundaries of boxes that are to be rendered on the display. All boxes in the same row share the same upper and lower SplitLines. Two adjacent rows also share a SplitLine that lies between the two rows. The column case is analogous. Users are able to change the size of part of the screen by dragging SplitLines that are boundaries of that region. As shown in Figure 4.2 Right, after the second vertical SplitLine is dragged to the left, the region to the left of it is squished, while the size of the region on the right side of the third vertical SplitLine remains the same.

![Figure 4.2](image)

**Figure 4.2:** *Left:* boxes are bounded by SplitLines. Screen space is evenly distributed before dragging. *Right:* the region occupied by the red box grows bigger by dragging the second vertical SplitLine left and the second horizontal SplitLine up.

A set of SplitLines provides both a linear ordering and a hierarchical
subdivision of space, as shown in Figure 4.3. Linearly, SplitLine B falls spatially between A and C. Hierarchically, it splits the region to the left of its parent SplitLine D in two, and its range is from the minimum SplitLine to the maximum of its parent SplitLine D. The diagram here shows only the vertical SplitLines; the horizontal situation is analogous. Each SplitLine has a split value, which ranges from 0 to 1. This value indicates the relative position of the SplitLine with respect to the boundary.

Rendering the boxes in the correct position on the display requires calculating the absolute positions of SplitLines. PRISAD [27] is a generic rendering infrastructure for information visualization applications on top of which PSV is built. It makes use of a hierarchical structure to organize the SplitLines to support efficient calculation of their absolute positions on the fly. When calculating the absolute value of a SplitLine, PRISAD simply traverses the SplitLine hierarchy from the root to the node that represents that SplitLine. The complexity of this operation is bounded by the depth of the tree, which is efficient enough to support real-time interaction.

Construction and maintenance are the two major tasks related to the SplitLine hierarchy. PRISAD is responsible for maintaining the correct hierarchical information once the SplitLine hierarchy has been successfully constructed. For example, after navigation by a user, PRISAD will update the split values when necessary to reflect the user’s interaction. Detailed information on how to maintain the SplitLine hierarchy can be found in James Slack’s Master’s thesis [26]. The rest of this section focuses on constructing the SplitLine hierarchy.

Since the powerset space is potentially enormous, it is not feasible to
Figure 4.3: An example of a SplitLine Hierarchy.

We instantiate every SplitLine, if view of the memory usage. Moreover, since sets are returned by the mining engine on the fly, we do not know which SplitLine needs to be instantiated until a set arrives in PSV. Therefore, PSV requires a dynamic hierarchical data structure that efficiently supports adding new SplitLines. We accomplish this task by extending the well-known red-black tree data structure [9] so that each red-black tree node is associated with a SplitLine. We maintain a red-black tree for both the horizontal and vertical dimensions. These two trees are fundamentally the same, except that the number of nodes in the horizontal tree is much smaller than that in the vertical one. We will use the horizontal tree as an example to demonstrate how we create and maintain the SplitLine hierarchy.

Construction of the SplitLine hierarchy can be further divided into two subproblems: (a) when to instantiate a SplitLine and (b) how to update necessary data structures to maintain the correct hierarchical structure. The following example gives an overview of the mapping process on a database with an alphabet size of eight items. As shown in Table 4.1, as sets are sent to the visualizer, their enumeration index is computed and used to find the row and column in the grid where boxes are drawn.

We instantiate a SplitLine when and only when (a) it has not been
Figure 4.4: Mapping from sets to boxes with alphabet size 8. 

*Bottom left:* After two sets have been loaded, lines 1 and 31 have been instantiated.

*Top left:* A single empty row visually separates the two sets, which are the first and last itemsets in the enumeration.

*Bottom right:* As more sets are added, the red-black tree storing the SplitLines rebalances, changing the root.

*Top Right:* The grid fills in with boxes, with visual separation between non-contiguous itemsets in the enumeration.
Table 4.1: As sets are sent to the visualizer, their enumeration index is computed and used to find the row and column in the grid where boxes are drawn.

<table>
<thead>
<tr>
<th>No.</th>
<th>Set</th>
<th>Index</th>
<th>Row</th>
<th>Col</th>
<th>Lines</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>{a}</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>{a, b, c, d, e, f, g, h}</td>
<td>254</td>
<td>31</td>
<td>6</td>
<td>31</td>
</tr>
<tr>
<td>3</td>
<td>{b}</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>-</td>
</tr>
<tr>
<td>4</td>
<td>{a, b, c, e}</td>
<td>93</td>
<td>11</td>
<td>5</td>
<td>11, 12</td>
</tr>
<tr>
<td>5</td>
<td>{a, b, d, h}</td>
<td>100</td>
<td>12</td>
<td>4</td>
<td>13</td>
</tr>
</tbody>
</table>

instantiated and (b) it serves as a boundary of at least one box. As shown in Figure 4.4 top left, after the first two sets have been loaded, a single empty row visually separates the two sets, which are the first and last itemsets in the enumeration. The instantiation of the empty row is important in that it servers as a visual cue to the user that the first two sets are not immediately adjacent to each other. A corresponding SplitLine hierarchy is shown in Figure 4.4 bottom left. Figure 4.4 top right shows the visualization after all the sets have been loaded. As more sets are added, the red-black tree stores the SplitLines, rebalances, and changes the root. The horizontal SplitLines hierarchy would require \(2^5 = 32\) nodes if it were statically allocated, but only 5 are needed when using dynamic allocation.

We need to insert a node in the corresponding red-black tree once we have decided to create a SplitLine. Before we insert the node into the red-black tree, we must calculate the default relative split position of each line, which is used to set or reset its initial absolute position so that the lines look uniformly distributed. If the number of SplitLines were a power of 2, then we could simply set each one to the split position of 0.5. When the binary tree is not perfectly balanced, then the correct value for a SplitLine
is the ratio between the regions of its left and right children:

\[ SV = \frac{L}{L + R}. \]  

(4.4)

Inserting a node \( z \) into a standard red-black tree with \( n \) leaves has a cost of \( O(\log n) \). Node insertion is a two-phase process: first, traversing a path downward from the root node to the correct insertion point at some leaf node; second, rebalancing the tree through a series of rotations. In our algorithm, the traversal and rotation functions must also maintain split positions for the SplitLines attached to the nodes. This additional functionality does not increase the complexity of the operations.

**Phase 1:** At each node in the red-black tree, we store the number of its left descendants \( L \) and right descendants \( R \). When inserting a node into the tree we increment the counters on the appropriate path. The sorting criterion for nodes is based on a key computed from the canonical enumeration of a powerset, as described in Section 4.1.2. We also calculate the default relative split positions for all nodes traversed.

If the change in the split position for a line is the result of navigation, we preserve the visible configuration of lines, and update the default split position for use the next time the line positions are reset. Otherwise, when no user navigation has occurred, we want to make room for the newly inserted line, uniformly distributing the available space between the set of SplitLines. In this case, we do update both the split position and the absolute position using the new default.

**Phase 2:** During a rotation on a node \( x \), there are four cases to
consider: $x$ could be either a left or right child, and there could be a left or right rotation. Figure 4.5 Right shows the right-left case: when doing a left rotation on a node $E$, which is a right child of its parent $D$, we only need to update the relative split positions of $E$ and its right child $F$, because for each node in the subtrees $\alpha$, $\beta$, $\gamma$, and $B$, its descendants and ancestors are preserved. Maintaining the $L$ and $R$ counts is straightforward, as described above. However, we cannot simply update the relative split positions of $E$ and $F$ using Equation 4.4 when the relative split positions have been changed by user navigation. Instead, we compute the new relative split positions based on the old ones using Equations 4.5 and 4.6. The absolute positions of $E$ and $F$ remain the same after the rotation, preserving the correct SplitLine hierarchy. The remaining three cases are analogous to this one. The bookkeeping operations are local and can be done in constant time.

\[
SV_F' = (1 - SV_E) \times SV_F + SV_E \tag{4.5}
\]

\[
SV_E' = \frac{SV_E}{SV_F'} \tag{4.6}
\]

### 4.3 Rendering and Picking

After all the necessary SplitLines have been instantiated, the boundaries of a particular box can be computed by traversing the SplitLine hierarchy. We can then start to draw these boxes on the display.
Figure 4.5: Maintaining SplitLine values through red-black tree node rotation. Here we show the case of a left rotation on node $E$, which is a right child of its parent. Nodes are labelled with relative split positions if those values change as a result of the rotation. The resulting absolute positions of $E$ and $F$ are the same as those before the rotation, which preserves the visual configuration of SplitLines.

4.3.1 Challenges

The challenges in rendering relate to underdrawing and overdrawing. Overdrawing occurs when several items fall into the same block on the screen. A naive rendering algorithm will simply redraw that block over and over again, which will dramatically increase rendering time. Underdrawing is at the other end of the spectrum. Certain boxes that should be rendered on the display are missing. To avoid underdrawing while minimizing overwriting, we developed an $O(\log(n) \cdot b_v \cdot c)$ rendering algorithm for PSV, where $n$ is the total number of items on the screen, $b_v$ is the number of blocks in the vertical dimension, and $c$ is the number of columns.
4.3.2 Our Approach

Rendering

Rendering in PSV strictly follows the rendering pipeline described in PRISAD [27]. The rendering process consists of three steps: partitioning, seeding, and drawing. Partitioning is a discretization process that maps the infinite-precision drawing of rectangular boxes to the desired block level. In other words, we divide the world space into small regions of equal size, where the number of regions is determined by the number of pixels available on the display and the size of the on-screen blocks. If a particular region contains only one set, we simply draw a box on the screen to represent the set. When a region contains more than one set, which is the most common case, we need to use other visual channels to encode aggregate information in addition to drawing a box on the display. In our current implementation, the brightness of a box is proportional to the number of sets in the region. Since SplitLines also serve as the boundary of boxes, the discretization process in PSV is done by dividing them into small regions. When the discretization process is finished, we enqueue all the boxes that need to be rendered. Finally, we traverse the rendering queue to render the boxes one at a time.

We maintain a red-black tree, NodeTree, for each column. The item set that is mapped to a column will be attached to a node in the corresponding red-black tree, where the index of the node is the row number of that item set.

The NodeTree provides both a linear ordering and a hierarchical organization of the item sets (as shown in Figure 4.6), which is similar to
the SplitLine hierarchy. Linearly, Node 5 falls spatially between 4 and 7. Hierarchically, it splits the region to the left of its parent Node 4 in two. Moreover, Node 5 covers the region from the upper boundary of itself to the lower boundary of node 7. For a node \( n \), we cache the following variables, which are used to facilitate traversal:

- **leftChild**: a reference to the left child of \( n \);
- **rightChild**: a reference to the right child of \( n \);
- **parent**: a reference to the parent node of \( n \);
- **descendant**: an integer that records how many descendants \( n \) has;
- **minLine**: a reference to one of the SplitLines in the vertical SplitLine, which is the upper boundary of \( n \);
- **maxLine**: a reference to one of the SplitLines in the vertical SplitLine, which is the lower boundary of \( n \);
• **aggregate**: a Boolean value that indicates whether \( n \) represents more than one box;

• **aggregateNumber**: an integer that records how many boxes \( n \) represents; and

• **fixed**: a Boolean value that indicates whether \( n \) should be drawn in a fixed size or in its actual size.

In addition, we compute the following variables on the fly, using standard tree-traversal algorithms:

• **nodeRange**: the region that is split by node \( n \). As shown in Figure 4.6, the nodeRange of node 5 runs from the upper boundary of node 4 to the lower boundary of node 7; and

• **nodeCoverage**: the region that is covered by node \( n \). As shown in Figure 4.6, nodeCoverage of node 5 runs from the upper boundary of node 5 to the lower boundary of node 7.

We perform a recursive binary subdivision on the NodeTree hierarchy. Recursion is dependent on either the world-space criterion that the Node has no children, or the image-space criterion that the Node's range currently subtends less than one block.

Figure 4.7 illustrates the three cases that determine whether the recursion should terminate or continue. In case 1, for Nodes 4 and 0, the node coverage is larger than one block size and has child nodes, so we descend to both children. Node 5 shows case 2, since its coverage spans less than one block. We stop the recursion and draw a box to represent Node 5 and
Figure 4.7: The three cases used to determine how to descend the NodeTree hierarchy.

its descendant (Node 7). Finally, Node 2 is a leaf node in the NodeTree hierarchy, and recursion stops.

Algorithm 1 shows the pseudocode of the enqueuing function, enqueueRecurse(Node node). Line 1 to line 6 ensure that node does not overlap with any boxes that are already in the rendering queue. If node overlaps with a box b in the rendering queue, b will be updated to an “aggregate” box and rendered accordingly. Line 8 to line 16 flag node.fixed variable if its actual size is smaller than one block. Line 18 evaluates if node is a leaf node and line 20 decides whether node’s coverage is less than one block. The number of recursions is bounded by the number of boxes in the vertical direction, $b_v$. Each of the recursions requires traversing the SplitLine data structure with a complexity of $O(\log(n))$, where $n$ is the total number of item sets. Therefore, the overall complexity of the enqueuing function is $O(\log(n) \times b_v)$.
Algorithm 1 Enqueuing Function: enqueueRecurse(Node node)

1: if node.minLine - node.nodeRange.minLine < unitBlockLength then
2:    node.nodeRange.minNode.aggregate = true
3:    node.nodeRange.minNode.aggregateNumber++
4: else if node.nodeRange.max - node.minLine < unitBlockLength then
5:    node.nodeRange.maxNode.aggregate = true
6:    node.nodeRange.maxNode.aggregateNumber++
7: else
8:    if node.maxLine.getPosition() - node.minLine.getPosition() ≥ unitBlockLength then
9:        node.fixed = false
10:       node.aggregate = false
11:       enqueue node;
12:    else
13:        node.fixed = true
14:        node.aggregate = false
15:       enqueue node;
16:    end if
17: end if
18: if node is a leaf node then
19:    return
20: else if node.nodeCoverage < unitBlockLength then
21:    return
22: else if node.leftChild ≠ null then
23:    renderRecurse(node.leftChild)
24: else if node.rightChild ≠ null then
25:    renderRecurse(node.rightChild)
26: end if
In the second phase of the rendering pipeline, we traverse the render­
ing queue and render as many boxes as we can in a given time slot. This
 technique is called **progressive rendering**. Progressive rendering is a tech­
nique that renders the entire scene in a prioritized fashion. It always renders
the most important part of the scene first and then fills in the details. If the
time that is allocated for rendering this scene is used up, progressive render­
ing just stops rendering the current scene and immediately starts drawing
the next scene, which makes the system very responsive. In PSV, we start
the rendering process from the columns that are within the user's navigation
box, because user navigation in this area implies that it is of great interest
to the user.

**Picking**

Picking is the process of identifying which object was rendered at a particular
\((x, y)\) pixel location. Picking also requires traversing both the NodeTree
and SplitLine hierarchies. Picking is done in two steps. The first step is to
traverse the horizontal SplitTree to find the correct column. In the second
step, we retrieve the NodeTree from the correct column and do a traversal,
which is similar to the binary search, to find the correct node, if one exists.
Algorithm 2 shows the pseudocode of the picking function. The input of
this function is the root node of the selected column's NodeTree.

Sometimes, the actual size of a box could be too tiny to be easily picked
by the user. A well-selected *fuzzConstant* is used to ensure that every box
that is visible on screen is pickable by allowing an offset of a few pixels.
The complexity of this function is \(O(\log(n))\), where \(n\) is the total number
Algorithm 2 pickNode(Node node) function.

1: if node is null then
2:     return null
3: else
4:     if mousePosY < node.minLine.getPosition() - fuzzConstant then
5:         pickNode(node.leftChild)
6:     else if mousePosY > node.maxLine.getPosition() + fuzzConstant then
7:         pickNode(node.rightChild)
8:     else
9:         return node
10: end if
11: end if

of boxes on screen.

4.4 Scalability

4.4.1 Challenges

The powerset grows huge as the alphabet size increases: a universe of only 24 items outstrips the number of pixels on the screen, and universes of over 32 or 64 items are difficult to even store in standard data formats. Our PSV system advances the state of the art by providing scalability in the size of the alphabet.

4.4.2 Our Approach

In the following sections, we will show that through scaling, PSV can handle datasets not only with large alphabets, but also with maximum set size.
Handling Large Alphabets

When the alphabet size $A$ is large, the powerset size $P$ is a huge number: $2^A$. Dynamic allocation of the SplitLine hierarchy, as discussed above, is necessary but not sufficient. The indices in the power enumeration do not fit into an integer or a long integer when the alphabet size is greater than 31 or 63, whereas we support alphabets of over 40,000 items. The naïve approach would be to simply switch data structures from integer to \texttt{bignum} everywhere that indices are used in the SplitLine hierarchy. However, computations using bignums are far more expensive than those using integers or longs, and storing them imposes a heavy memory footprint, so we would like to minimize their use. In contrast, the visualizer must store all $N$ sets actually shown in main memory, so our algorithms are optimized for the case where $N << P$. In the current implementation, $N$ is limited to the range of 1.5 to 7 million sets, a number far smaller than the 2 trillion limit of integer data storage. Operations that use the number of shown sets $N$ can be done much more efficiently, as opposed to those that use the alphabet size $A$ or the powerset size $P$.

Our spatial layout does fundamentally depend on the powerset size $P$, so we cannot completely eliminate bignums. The key insight is that we only need to use these high-precision values when adding SplitLines from the hierarchy as sets are added to the scene. Specifically, we use bignums in two computations: finding the enumeration index as described by Equation 4.2, and then when dividing that index by the fixed width of the grid to get a bignum row index. The row index does need to be stored: as illustrated
in Figure 4.4, a full-precision SplitLine row index may be necessary when resolving the spatial relationship between the box in question and boxes that are added or deleted later. By storing this row index as a bignum, we support lazy evaluation and avoid unnecessary computation. Although the computation of the enumeration index requires bignums, we do not need to incur the memory overhead of storing it, so we throw it away after its use in computing the row index.

Our rendering and navigation routines remain fast because we do not need to use bignums when traversing the SplitLine hierarchy. Although the bignum row indices must be stored at each node of the hierarchy, we can traverse the tree without them by maintaining pointers or object references in the node data structure linking it to its children and parent.

**Extending the Maximum Set Size**

Often dataset semantics dictate that the maximum set size is much smaller than the alphabet size. For example, it is essentially impossible to buy every item in a grocery store in one shopping trip or to take the thousands of courses offered at a university during the same term. Figure 5.3 shows that a university enrollment dataset with alphabet 4616 has a maximum set size of 13, and the market basket data in Figure 5.6 has a maximum set size of 115 out of the 1700 items in the alphabet. In contrast, although the particular software engineering dataset shown in Figure 6.1 has a maximum set size of 48 files checked in together during a bug fix out of 42,028 files in the alphabet, the domain semantics could allow a maximum set commensurate with the entire alphabet. For instance, if the copyright notice on top of
each file needs changing, every file in the repository would be touched. An important property of our algorithm is that there is no hardwired prior limit on the maximum set size; we can accommodate a maximum set size up to the cardinality of the alphabet itself.
Chapter 5

Case Study

PSV is a general information visualization system for data mining that provides a unified visual framework at three different levels: data mining on the filtered dataset, the entire dataset, and comparison between multiple datasets or data mining runs sharing the same alphabet. In this chapter, we present a case study that showcases the utility of PSV.

5.1 Datasets

Two real datasets are used in this chapter to demonstrate the power of PSV: a student course enrollment dataset, enrollment, and a retail transaction dataset, market. In this section, we briefly introduce to these datasets.

- **Enrollment**: an itemset is a set of courses taken by a student during a particular term, which includes the student number, course numbers, and grades. The student numbers in the original dataset have been sanitized using random integers for privacy purposes. The 95,776 itemsets cover the six terms of the academic years 2001, 2002, and 2003. The alphabet size, 4616, is the number of courses offered.
• **Market**: a record in this dataset is a set of items that are bought together by a particular customer during a single visit to a store. This dataset was downloaded from UCI Machine Learning Repository \(^1\) and had been sanitized. This dataset contains 300,000 transactions and has 1657 items.

### 5.2 Enrollment Dataset

#### 5.2.1 Frequent-Set Mining

We chose dynamic, constrained frequent-set mining as a concrete case study. Frequent-set mining is the process of identifying groupings of co-appearing objects in a dataset, whose frequencies exceed a user-specified threshold. The appeal of constrained frequent-set mining is well known \([23, 8, 20]\). One key problem that has not been addressed in previous work is how to support users in choosing and changing constraint thresholds and parameters. This unsolved problem makes dynamic constrained frequent-set mining a perfect case study for showcasing the power of our visualization system.

At the beginning of the task, the analyst specifies a set of constraints and a frequency threshold. Sets that both satisfy the constraints and pass the frequency threshold will be returned to PSV. Finally, PSV will render the sets returned by the mining engine on the display to give analysts immediate visual feedback of the mining result.

PSV is able to communicate with the mining engine using a simple text protocol, which includes `constraint settings`, `pause`, and `play`. Users

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\(^1\) [http://www.ics.uci.edu/~mlearn/MLRepository.html](http://www.ics.uci.edu/~mlearn/MLRepository.html)
can pause the mining engine to tighten or relax the parameter settings based on the partial result.

In the current implementation of PSV, users are able to specify the following types of constraints for interactive constrained frequent-set mining:

(a) **aggregation constraints** of the form “$\text{agg}(\text{resultSet.}A) \theta \text{const}$”, where (i) $\text{agg}$ is an aggregate operator (e.g., MAX, MIN, MEAN, MEDIUM, SUM), (ii) $A$ is an auxiliary attribute (e.g., class size, class average for the student record database), (iii) $\theta$ is a comparison operator (e.g., $=, >, <, \geq, \leq$), and (iv) $\text{const}$ is an integer constant. For example, the constraint “$\text{MAX(resultSet. classSize)} < 100$” finds all the sets of courses having a maximum class size of less than 100.

(b) the **frequency constraint** “$\text{frequency(resultSet)} \geq \text{threshold}$”, which finds all the sets whose occurrences in the dataset meet or exceed the user-specified threshold. For example, the constraint “$\text{frequency(resultSet)} \geq 0.001$” finds all the sets that appear in at least 0.1% of the transactions in the dataset.

(c) **containment constraints** of the form “$\text{resultSet contains ConstSet}$”, where $\text{ConstSet}$ is a set of constants. Here, this type of constraints finds all the sets that contain any of the constants in $\text{ConstSet}$. For example, the constraint “$\text{resultSet contains \{CPSC124, CPSC126\}}$” finds all the sets that contain the course CPSC124 or CPSC126.

Constraints are processed at different locations within PSV: some can be handled by both the visualizer and the miner, while others are only
processed by the miner or only processed by the visualizer. Frequency constraints are computationally intensive, and are thus "pushed inside" to the miner, in order to provide as much pruning as possible. The miner can handle a combination of frequency and aggregation constraints. Sets that satisfy these miner constraints are sent to the visualizer for display. Specifying constraints for the miner is also a way of filtering datasets larger than the current 7-million itemset capacity of the visualizer, which maintains all loaded itemsets in main memory to support fluid realtime exploration.

The visualizer supports aggregation and containment constraints by visually highlighting the matching sets from among those it has loaded. It can handle multiple simultaneous constraints, colouring each with a different colour.

The visualizer supports immediate exploration of multiple simple constraints but has the limited capacity of 7 million itemsets, whereas the miner can handle very large datasets and more sophisticated constraints but requires a longer period of time for computation.

### 5.2.2 Usage Scenarios

We present four scenarios of PSV features being used during a data-mining task. These scenarios are built around the real course enrollment database, where an itemset is the set of courses taken by a student during a particular term. The 95,776 items cover the six terms of the academic years 2001, 2002, and 2003. The alphabet size, 4616, is the total number of courses offered. Our example user is an undergraduate course coordinator interested in finding sets of courses that are frequently taken together, so that she can
minimize conflicts when scheduling courses for the following year.

**Scenario 1:** The coordinator first considers medium-sized courses, and decides to start with an enrollment threshold of 100. Her first constrained frequent-set query is \( \text{frequency} \geq 0.005 \) and \( \text{max(courseSize)} \leq 100 \). The result of the query shows all possible sets of courses such that the set appears in at least 0.5% of all student registration records and that have a maximum class size of less than 100. She watches the visualizer display as it dynamically updates to show the progress of the miner, and notices from the sparseness of the display that her initial parameter setting might not be appropriate. Figure 5.1 shows the constrained frequent sets computed so far when she pauses the computation after 10% of the itemsets have been processed. The sets are shown as a distribution of small boxes ordered by cardinality, from singleton sets at the top to 5-sets on the bottom. (Hereafter we use the convention of \( k \)-sets to denote sets of size \( k \).) Each cardinality has a different background colour, and within each cardinality the sets are enumerated in lexicographic order, as discussed in Section 4.1. The coordinator loosens the frequency constraint to .001, and tightens the enrollment parameter to 80 or fewer students before resuming the computation. Figure 5.2 shows the final result with the new constraints. After all ninety-six thousand itemsets have been processed by the miner, the largest constrained frequent itemset is a 9-set, whereas the largest set in the partial result in Figure 5.1 is a 5-set.

**Scenario 2:** The coordinator now returns to the question of what course size would represent her intuitive idea of "medium". Instead of filtering the itemsets with the miner, she loads in the entire database in **pass-through**
Figure 5.1: Scenario 1 for data mining with PSV. The user pauses after 10% of the itemsets are processed to loosen the frequency constraint and tighten the other parameters.

Figure 5.2: Scenario 1 for data mining with PSV. After the user's refinement, the view is considerably denser, showing higher cardinality sets, after all the itemsets are processed.
Figure 5.3: Scenario 2 for data mining with PSV. The user loads in the entire raw dataset to find good parameter settings with lightweight experimentation, using the same unified framework as when the miner was filtering data. Courses with enrollment less than 100 are highlighted.

mode. This way she can quickly explore by highlighting itemsets that satisfy different attribute constraints directly in the visualizer, as shown in Figure 5.3. She tries several values for the maximum enrollment constraint, and in less than a minute settles on a value of 100.

**Scenario 3:** The coordinator continues by zooming in to 2-sets to investigate details that cannot be resolved from the overviews she has seen so far, which show aggregate information about multiple sets if they fall into the same spatial region in the layout. When she zooms in far enough, each on-screen box in the zoomed-in region represents only a single set, as show in Figure 5.4. The relative ordering of itemsets is preserved in both the horizontal and vertical directions. She can still see the highly aggregated information about 1-sets on top and higher cardinality sets on the bottom, so she can easily keep track of the relative position of the area that she
Figure 5.4: Scenario 3 for data mining with PSV. The rubber-sheet navigation technique of stretching and squishing a box shows details.

has zoomed. She can browse many itemsets in a few seconds by moving the cursor over individual boxes to check the course names reported in the lower left corner of the display. Those highlighted sets show the courses that are frequently taken together by students in the current year. Therefore, by looking at those highlighted sets, she easily identifies which courses to avoid scheduling at the same time as CPSC 124.

**Scenario 4:** Having found a good enrollment threshold of 100 that characterizes medium-sized courses, the coordinator is ready to investigate individual courses and determine whether the set of courses frequently taken together changes over time. Instead of looking at the combined data over all academic years, she selects only the 2001 data. She then returns to the miner to filter with the constraints of \( \text{frequency} \geq 0.001 \) and \( \max(\text{courseSize}) \leq 100 \), and clicks on the box representing the 1-set CPSC 124. Figure 5.5(a) shows that this 1-set and all of its supersets are
Figure 5.5: (a): CPSC 124 and its supersets are highlighted for the academic year 2001. (b): the same course and its supersets are highlighted for the academic year 2003.
highlighted. In other words, she can see the upward closure property of the containment relation. Using lattice terminology, the highlighted elements form a lower semi-lattice with CPSC 124 as the bottom element, and satisfy all the specified constraints. The courses contained in these highlighted sets are the ones to avoid scheduling simultaneously with CPSC 124. She then starts up a second copy of PSV with the same configuration on the academic year 2003 data, as shown in Figure 5.5(b). With the 2001 and 2003 displays side by side, she can quickly spot differences and mouseover those boxes to find the names of courses that became less popular to take with CPSC 124.

5.3 Market Dataset

Figure 5.6 shows the result of the Market dataset. The numbers on the left side of the window indicate the size of the sets or the number of items bought together by a customer during a single shopping trip. It is easy to determine that the upper part of the window is much denser than the lower part, which means that customers are less likely to buy many items at a time. After a close look at the final visualization, we confirm that most of the transactions consist of fewer than six items. Interestingly, the top part of the region for singleton sets is denser than the lower part, which implies that the products listed in the head part of the alphabet are more popular than those in the tail part. Unfortunately, we are unable to identify those products to conduct further analysis, since the Market dataset has no attribute.
Figure 5.6: A visualization of the Market dataset. The basket dataset has over half a million itemsets and an alphabet of 1700 items.

5.4 Discussion

The aforementioned case study has demonstrated the power of the PSV system. PSV is good at identifying global distribution of frequent sets as well as the differences between two datasets sharing the same alphabet. However, PSV may not be as useful as the traditional text-based interface when serving as a driving interface to the steerable mining engine. The decision of when and how to relax or tighten the constraints is solely based on quantitative information, which can be accurately and efficiently represented using numbers. More specifically, if the cardinality of the final result is small, then a traditional text-based interface may be a good choice because users can get useful information immediately by reading a short list. In contrast, finding rectangles requires additional navigation. However, if users care more about the distribution of the final result, PSV is obviously a better choice, since the contextual information provided by PSV provides information about the distribution.
In the student enrollment example, given a course, a typical user might be interested in only the top 10 courses that are taken together with the course of interest in a specified period. The result can be shown to the user simply using a short list. The additional contextual information does not facilitate the user’s job. On the contrary, unnecessary navigation resulting from discovering the detailed information requires extra effort.

We tried to showcase the utility of PSV in other domains, such as software engineering and algorithms. However, based on our research and interviews with several domain experts, it was difficult to find examples that required the full power of PSV. PSV has the ability to allow users to explore in a huge search space, but most domain-specific problems do not require showing or searching the result in the context of the entire search space.
Chapter 6

Performance

In this chapter, we discuss the performance of the PSV system with both real and synthetic datasets. We document that PSV can scale to datasets of up to 7 million itemsets and alphabet sizes of over 40,000 items, while maintaining interactive rendering speeds of under 60 milliseconds per frame.

6.1 Datasets

6.1.1 Mozilla Dataset

We use the Mozilla dataset to show that PSV can accommodate datasets with alphabet sizes of over 40,000 items. The Mozilla dataset is a software engineering dataset from the open-source Mozilla project \(^1\). It was downloaded from the Bugzilla \(^2\) bug database and was compiled by Anne Ying. An itemset is a set of files that have been checked in together after a revision task is done. Each itemset contains the file names and their version numbers. There are 33,407 check-in records and 42,028 files in the Mozilla dataset. The final visualization is shown in Figure 6.1.

\(^1\)http://www.mozilla.org
\(^2\)http://www.bugzilla.org/
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Figure 6.1: The Mozilla dataset has 42,028 itemsets and an alphabet of 42,028 items.

6.1.2 Synthetic Datasets

To showcase the memory usage and rendering performance of PSV, we generate two synthetic datasets, sparse and dense. The dense synthetic dataset is the extreme case of the densest possible distribution: items in the dataset are the first 10 million items in the full powerset generated from a dataset with an alphabet of 10,000 items. The sparse synthetic dataset has a distribution density roughly similar to the market dataset, and uses the same alphabet.

6.1.3 Datasets Summary

Table 6.1 summarizes the datasets introduced in the previous sections.
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<table>
<thead>
<tr>
<th>Name</th>
<th>Alphabet Size</th>
<th>Transaction Size</th>
</tr>
</thead>
<tbody>
<tr>
<td>Enrollment</td>
<td>4,616</td>
<td>95,776</td>
</tr>
<tr>
<td>Market</td>
<td>1,657</td>
<td>300,000</td>
</tr>
<tr>
<td>Mozilla</td>
<td>42,028</td>
<td>33,407</td>
</tr>
<tr>
<td>Sparse</td>
<td>10,000</td>
<td>10,000,000</td>
</tr>
<tr>
<td>Dense</td>
<td>10,000</td>
<td>10,000,000</td>
</tr>
</tbody>
</table>

Table 6.1: A summary of the datasets.

6.2 Scalability and Benchmarks

The performance results discussed in this section are based on the following computer configuration: a 3.0GHz Pentium 4 with 2GB of main memory running SuSE Linux with a 2.6.5 kernel and Java 1.4.1_02-b06 (HotSpot), with an nVidia Quadro FX 3000 graphics card and an 800x600 pixel window.

Figures 6.2 and 6.3 show the PSV performance results for memory usage and render speed respectively, for the enrollment, Mozilla, market datasets as well as for two synthetic datasets. As shown in Figure 6.2, datasets that share the same alphabet size of nearly 5000 items have the same initial memory requirements. The Mozilla dataset has the much larger alphabet size of over 40,000 items, and requires more initial memory. A large alphabet requires a relatively larger initial memory to build a lookup table that speeds up calculation of the index of a set in the powerset enumeration, where the size of the table is proportional to the size of the alphabet. Initial memory requirements are also noticeably higher because most elements in the lookup table are BigIntegers, which require much more memory than do primitive variables.

PSV can handle 7 million itemsets from the dense dataset before run-
ning out of memory, which limits supportable dataset size. The limits of PSV depend on the distribution of the dataset within the powerset. Sparser datasets require the instantiation of more SplitLines than do dense ones, resulting in less total capacity in the visualizer. The sparse dataset represents a typical use case. PSV can handle over 1.5 million itemsets from this dataset family before its memory footprint outstrips the maximum Java heap size of 1.7GB. We reiterate that when using the miner as a filter, PSV as a client-server system can handle much larger datasets than the limits of the visualizer.

Figure 6.3 top shows that the rendering time is near-constant after a threshold dataset size has been reached. This constant time is very small: 60 milliseconds per scene, allowing over 15 frames per second even in the worst-case scenario. Render time also depends linearly on the horizontal width of the grid.

We are also interested in the performance when part or all of the on-screen sets are highlighted, since grouping and highlighting are the two most commonly used features in PSV. In PSV, a set can belong to multiple groups at the same time. The colour of the set is determined by the colour of the group having the highest priority. However, we do not determine colour on the fly, since the cost of querying and of changing OpenGL context may be very high. In the current implementation, when a set belongs to \( n \) groups we simply redraw the set \( n \) times in \( n \) different depths based on the group priorities. We rely on the Z-buffer to assign the correct colour to the set. Based on the results of our empirical experiments, the cost of redrawing a set multiple times is much less than that of determining the colour on the
fly, considering that a set is not likely to belong to more than three groups at the same time. In the worst-case scenario, when each of the \( n \) groups contains all sets, rendering time is \( n \) times that of the normal case where no sets are highlighted.

The main challenge PSV presented with us was to accommodate large alphabet and maximum set sizes, a difficult goal given the exponential nature of the powerset used for spatial layout. We have done so, showing examples of PSV in use on alphabets ranging from 4,000 to over 40,000 items. Larger alphabets require more bits in the bignums used in enumeration, affecting both the speed and memory usage of PSV.
Figure 6.2: Top: PSV memory usage is linear in the transaction log size, and depends on the sparsity of the dataset distribution within the powerset. Bottom: Inset showing memory usage for small datasets.
Figure 6.3: Top: PSV rendering time is under 60 milliseconds per frame, near-constant after passing a threshold, and linear in the width of the grid. Bottom: Inset showing render times for small datasets.
Chapter 7

Conclusion and Future Work

In this thesis, we have reported the design and implementation of the PSV visualization system for lattice-based mining of powersets. PSV provides a unified visual framework at three different levels: data mining on the filtered dataset and the entire dataset, and comparison between multiple datasets sharing the same alphabet. PSV is also connected to a dynamic frequent-set mining server, showcasing how this visualization approach helps users exploit the power of steerability.

The key technical challenge for PSV is the size of the alphabet. We develop a fast scheme for computing the enumeration position of a given $m$-set in $O(m)$ time, devise a dynamic data structure for managing SplitLines, and handle bignums carefully to avoid inefficiencies. We conduct case studies of the PSV system with real datasets. We also use synthetic datasets to expose the limits of the current implementation of the PSV system. Empirical evaluation shows that the current version is capable of handling an alphabet size over 40,000 items and a transaction dataset exceeding 7 million transactions. Maintaining high frame rates is critical to the success of interactive visual mining, and our framework successfully keeps the time required to render the entire visible scene under one tenth of a second.
Chapter 7. Conclusion and Future Work

There are several limitations of our work. As the main motivation of PSV, frequent-set mining is not the perfect example for showcasing its power, since showing the final result in the context of the entire search space is not a key factor in achieving the tasks introduced in Chapter 5. This leads to a central question concerning PSV: when do we require distribution information? It is not easy to find compelling examples in other domains, however, we are still in search of clear tasks and/or datasets with more attributes, where the full power of PSV will be utilized.

There are several directions we would like to pursue in future work. First, we would like to characterize the effectiveness of different enumeration orderings in helping users find visual patterns that convey important information about the dataset. We would like to offer users flexibility in ordering the powerset. Specifically, people may attach different weights to all or some of the items. The second-tier ordering of the powersets will be based on the weight of the item, to ensure that itemsets containing “heavier” or more important items will appear before “lighter” or less important itemsets.

Second, we would like to juxtapose different datasets sharing the same alphabet in a single window. In the current implementation, users need to run two copies of PSV to compare two datasets that share the same alphabet; they must switch back and force to compare the two visualizations. It would be ideal to offer users the opportunity to view different datasets in a single copy of PSV. We may also employ a brushing and linking technique, so that users may easily identify the relationships among different datasets.

Finally, we would like to adapt the current version of PSV to support
comparing different partial data-mining outcomes for other data-mining tasks, including sequential-pattern mining [2], decision-tree construction [4, 12], and clustering [18]. Moreover, because finding frequent set is the first step in identifying association rules, we would like to enable PSV to support discovering association rules. We also would like to continue to explore the possibility of applying PSV in other domains, such as software engineering and algorithms.
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