

Frontiers in Nuclear Theory: From Light Nuclei to Astrophysics

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CANADA'S NATIONAL LABORATORY FOR PARTICLE AND NUCLEAR PHYSICS

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University of British Columbia, Vancouver



What is Nuclear Physics?

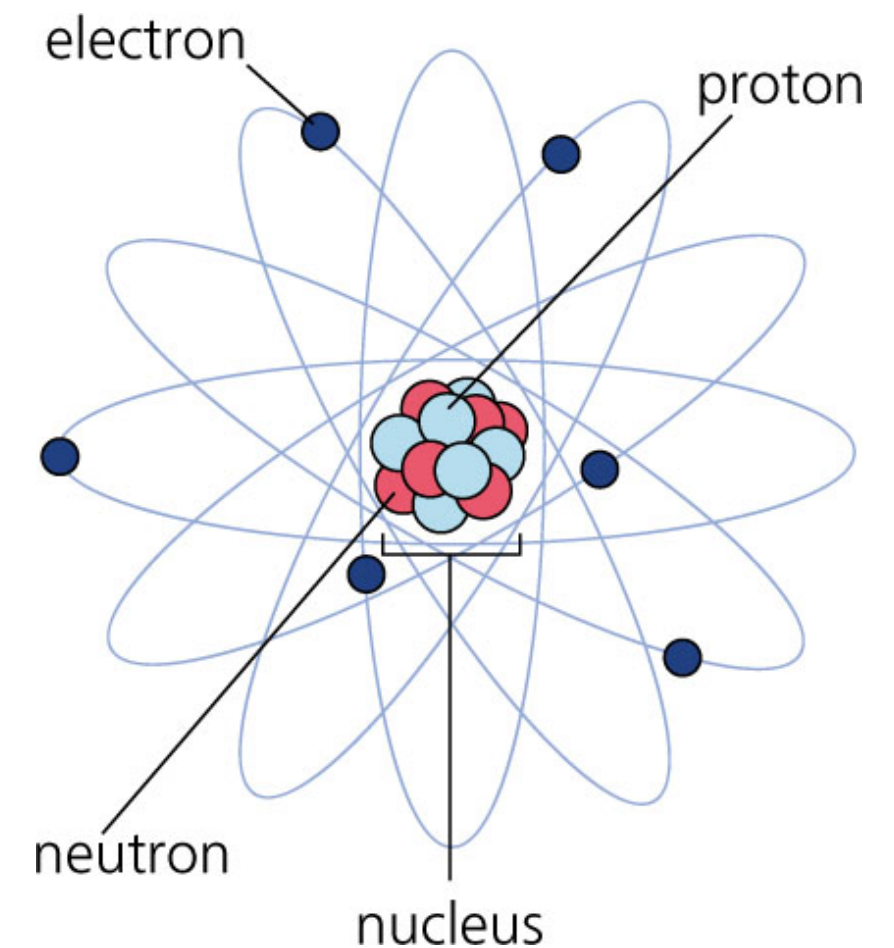


"**Nuclear Physics** is the field of physics that studies the building blocks and interactions in atomic nuclei"

What is Nuclear Physics?



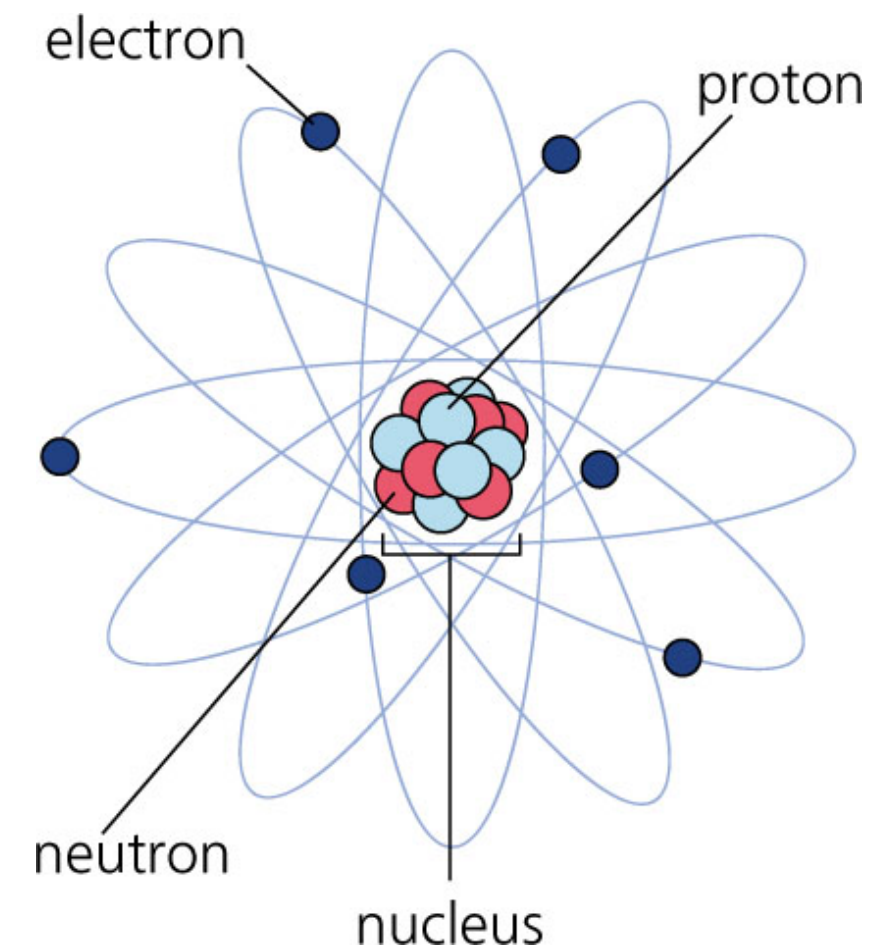
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What is Nuclear Physics?



"Nuclear Physics is the field of physics that studies the building blocks and interactions in atomic nuclei" ✓



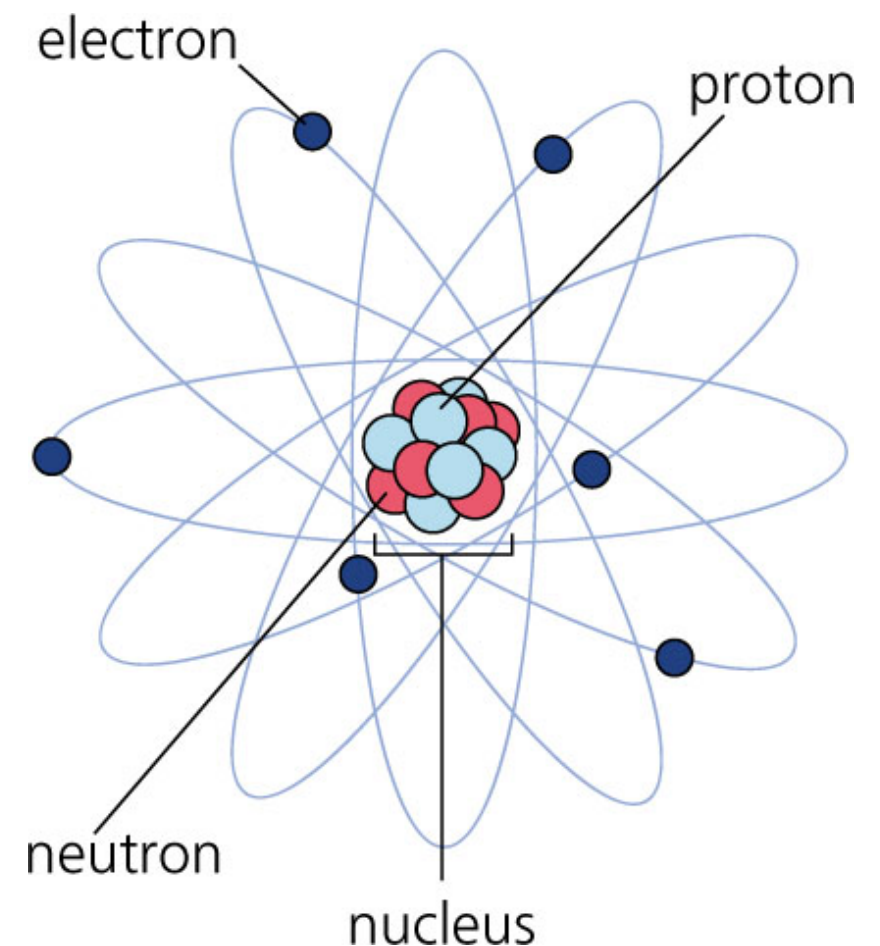
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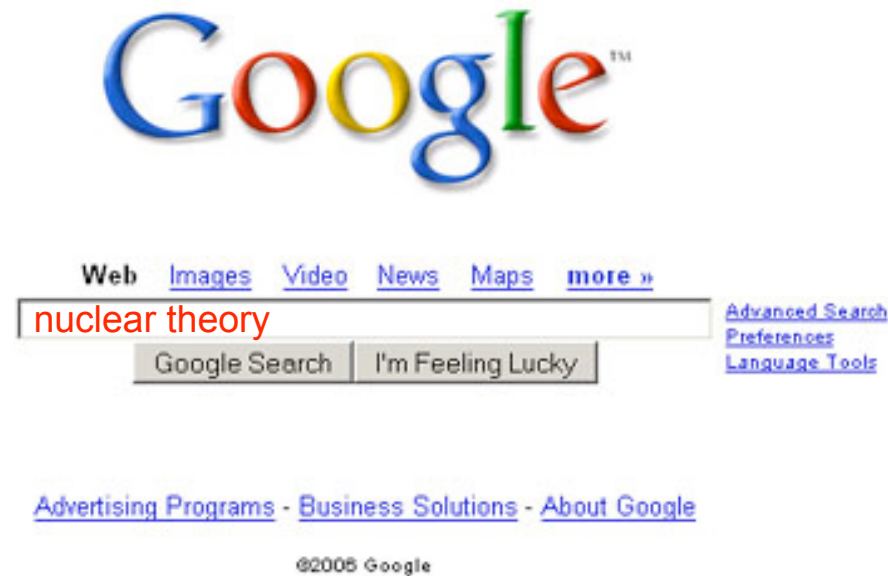
“Nuclear Physics is the field of physics that studies the building blocks and interactions in atomic nuclei” ✓

- It is a science build on a strong connection between theory and experiment
- It has also many interesting applications that influence and improve our daily life:
 - ★ nuclear medicine (radiopharmaceuticals)
 - ★ hadron therapy (cure of cancer)
 - ★ engineering materials (ion implantation)
 - ★ archaeology (carbon dating)

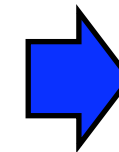
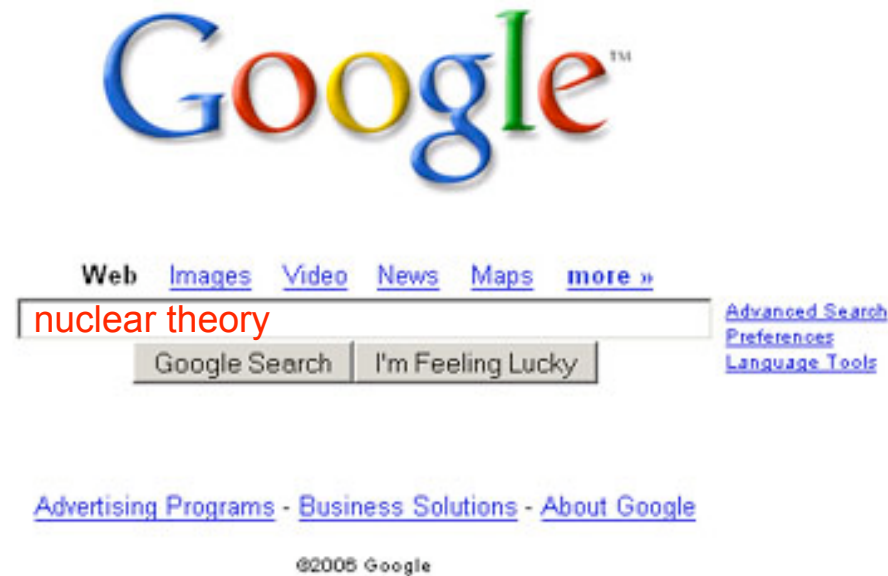
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What is Nuclear Theory?



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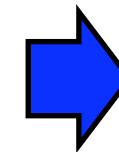
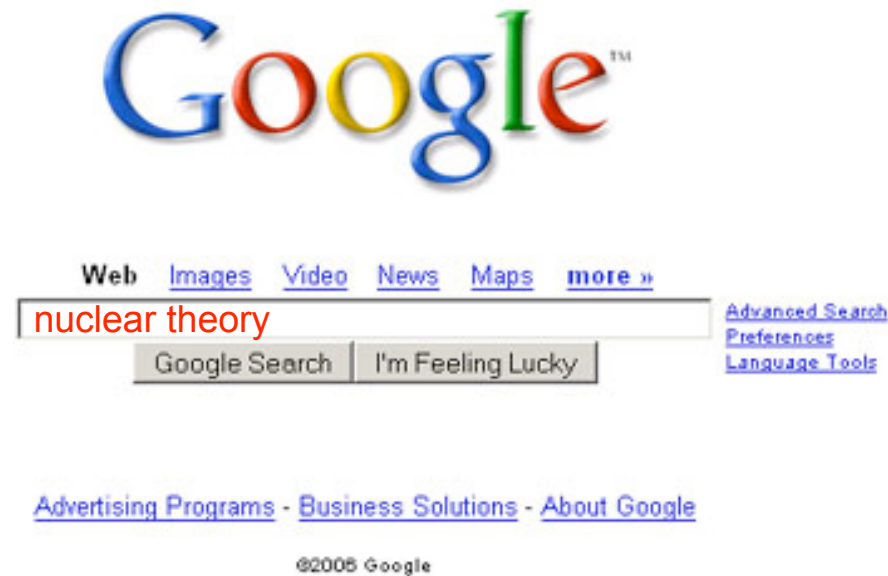


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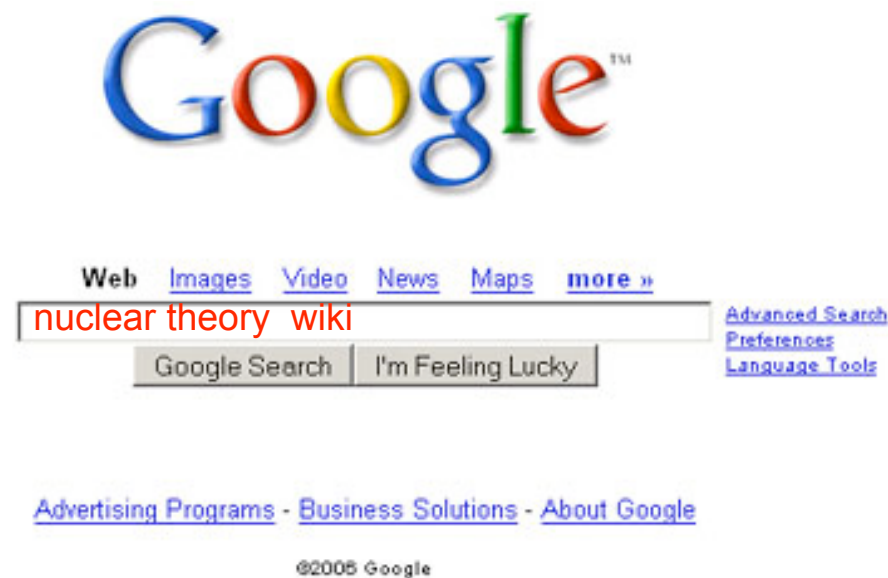


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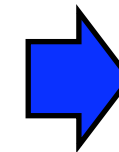
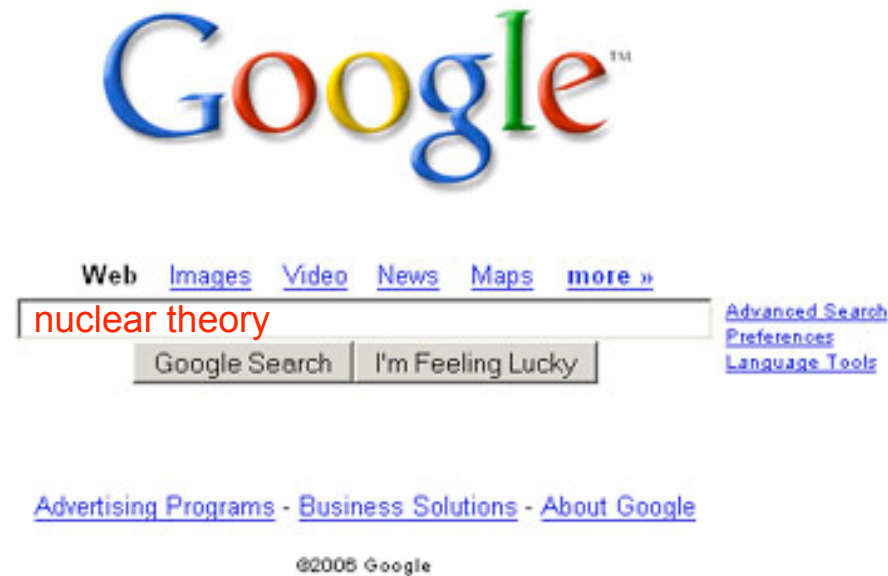
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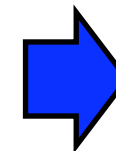
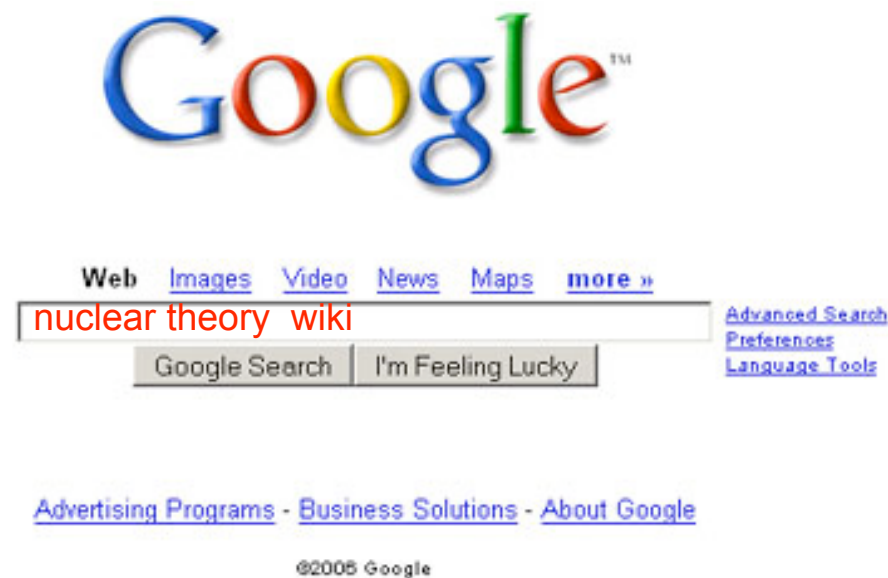
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It is the theory that tries to understand and predict nuclear properties, by studying the way protons and neutrons interact to form nuclei

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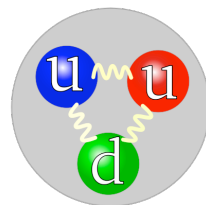
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- ★ What is the interaction that binds nucleons together?
What is its relation to Quantum Chromo Dynamics?



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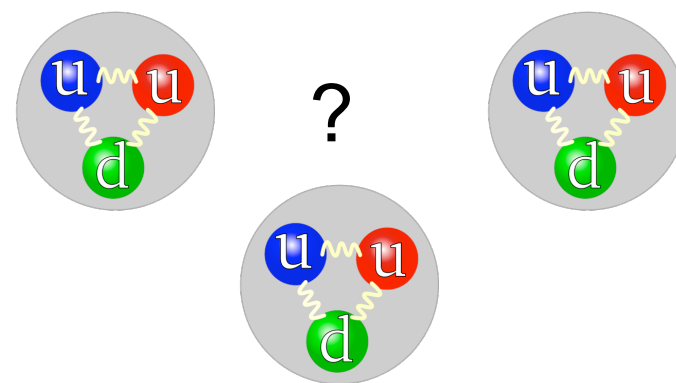


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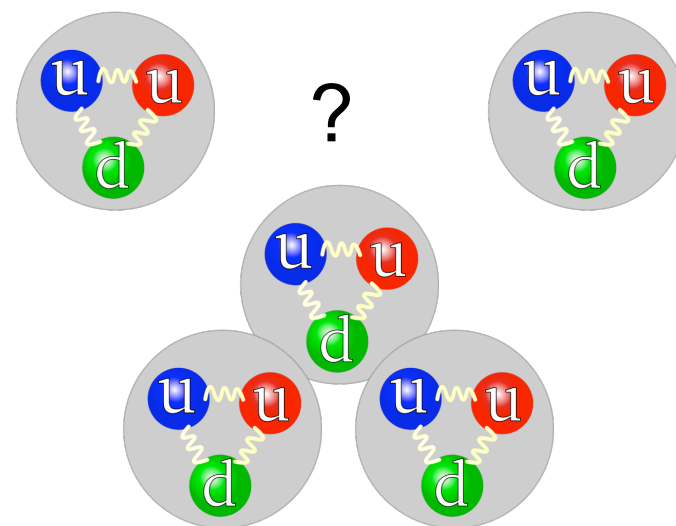


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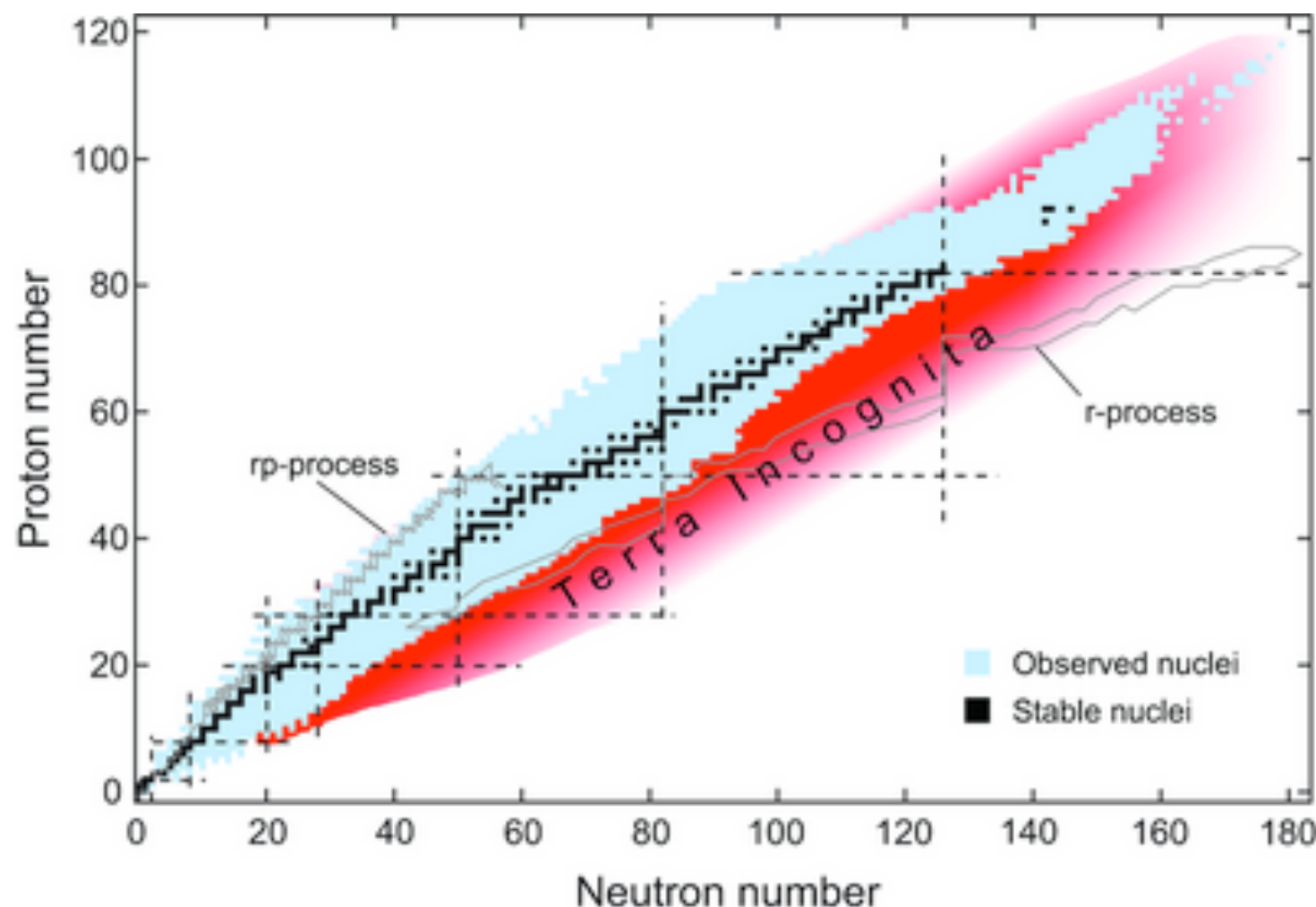
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What are the interesting questions we try to answer?



★ How happens that protons and neutrons are bound into stable and rare isotopes?
What are the limits of their existence?

★ How did the nucleosynthesis of elements occur?
Big Bang Nucleosynthesis
r-process ...

What is Nuclear Theory?

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What are the interesting questions we try to answer?

★ What is the nature of neutron stars?



★ What are the nuclear reactions that drive supernovae explosions?

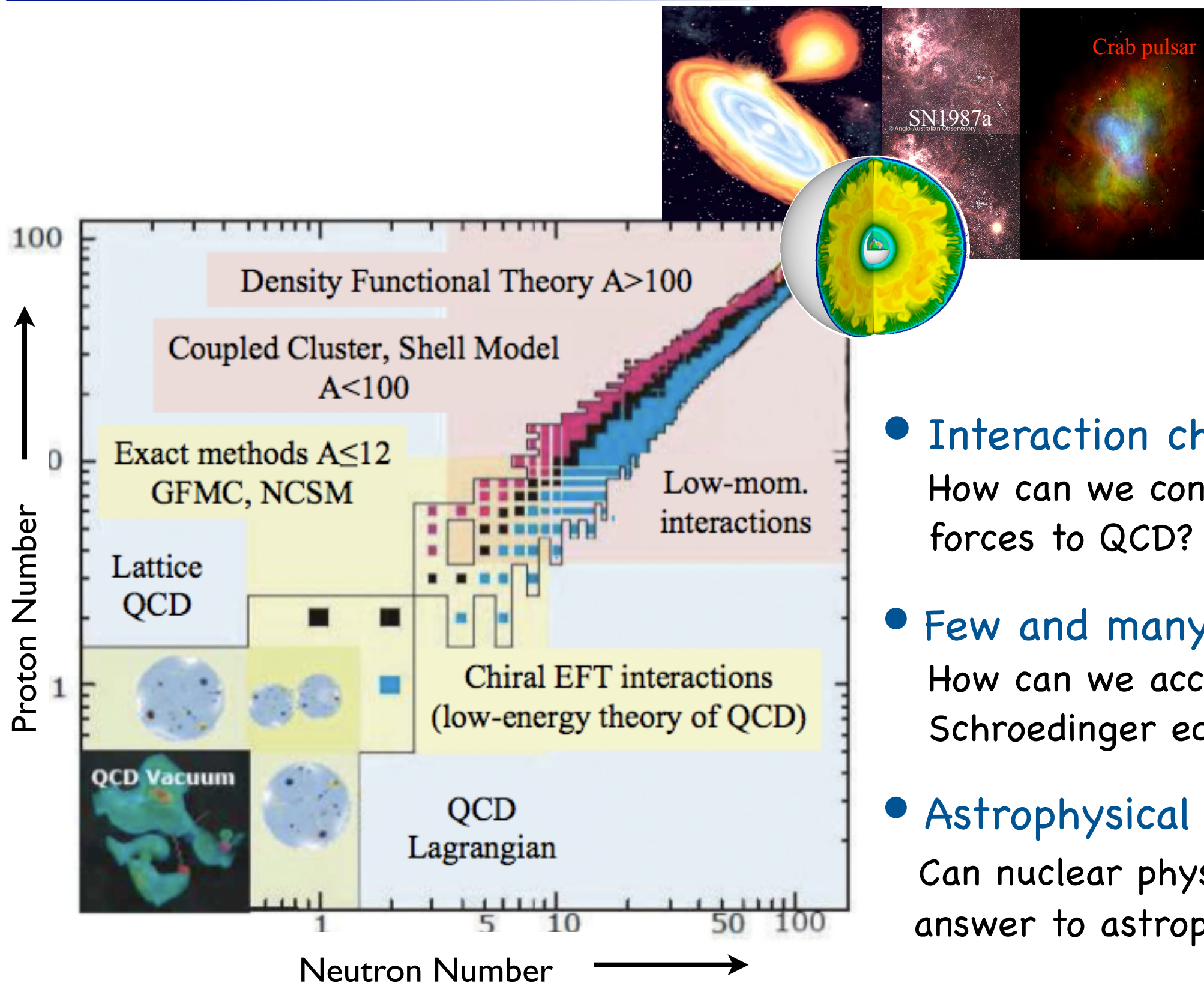


before



after

Frontiers in Nuclear Theory

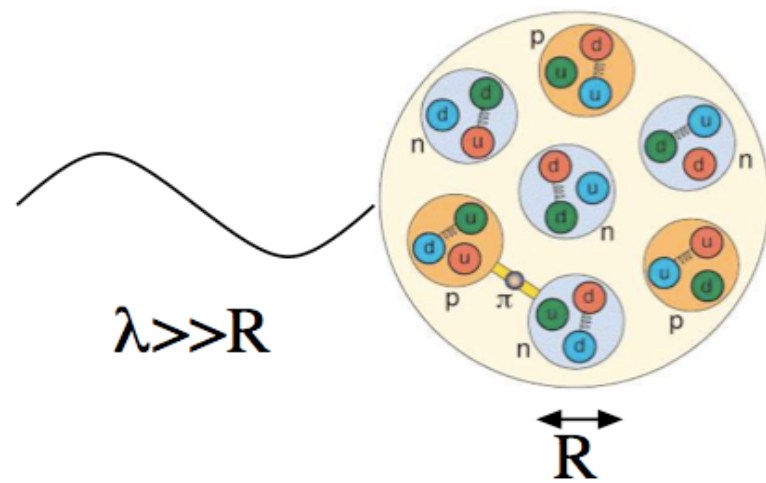


- **Interaction challenges**
How can we connect nuclear forces to QCD?
- **Few and many-body challenges**
How can we accurately solve the Schroedinger equation?
- **Astrophysical challenges**
Can nuclear physics provide an answer to astrophysical questions?

Interaction challenges

The Chiral Effective Field Theory Approach

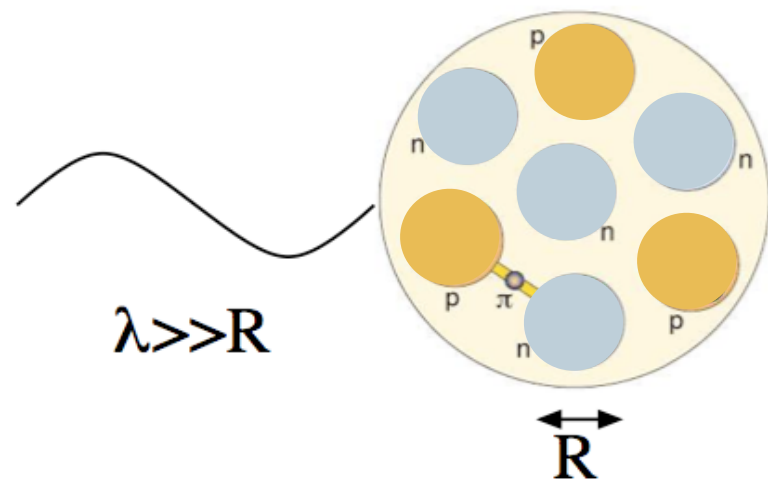
Separation of scales $\frac{1}{\lambda} = Q \ll \Lambda_b = \frac{1}{R}$



Interaction challenges

The Chiral Effective Field Theory Approach

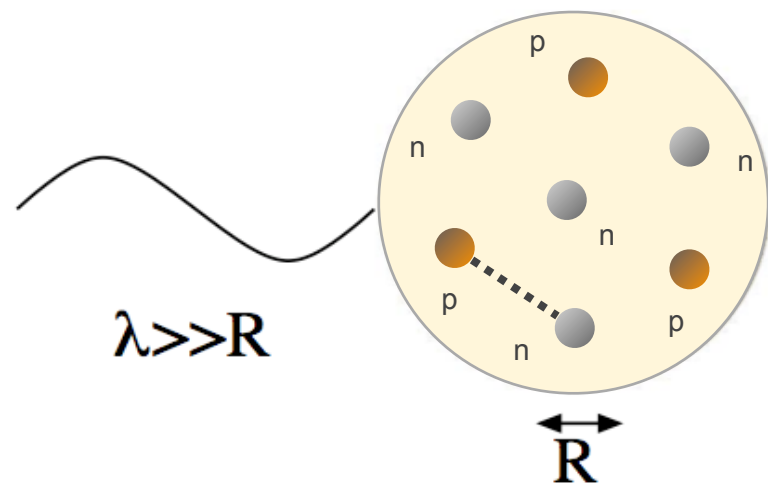
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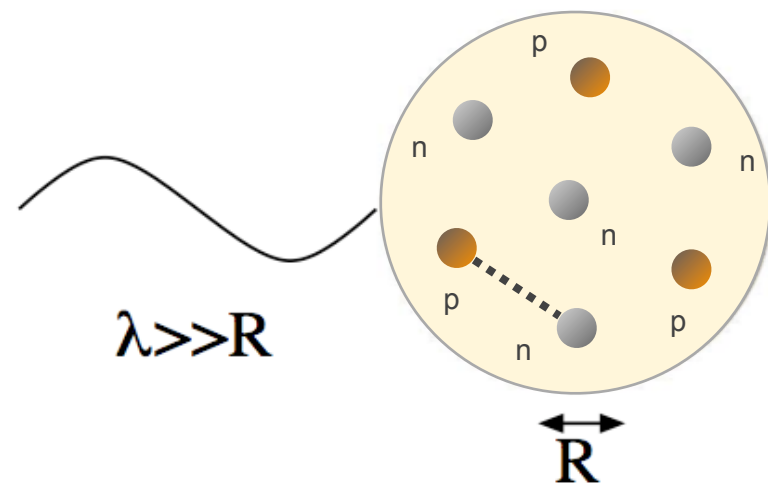
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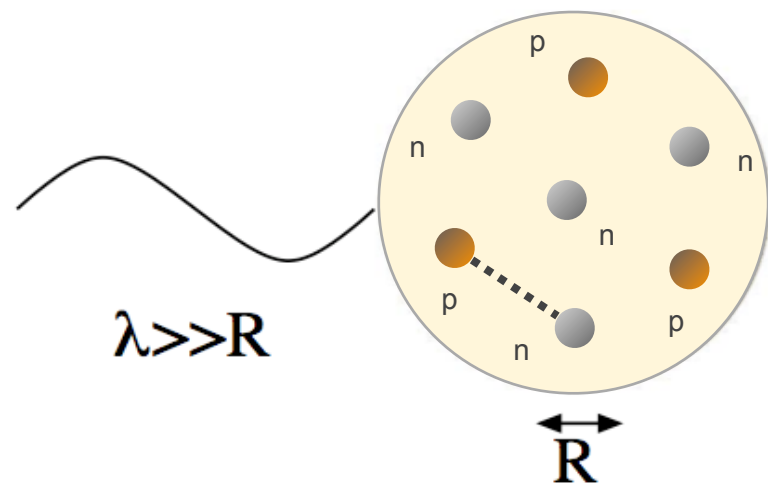


Limited resolution at low energy
expand in powers $\frac{Q}{\Lambda_b}$




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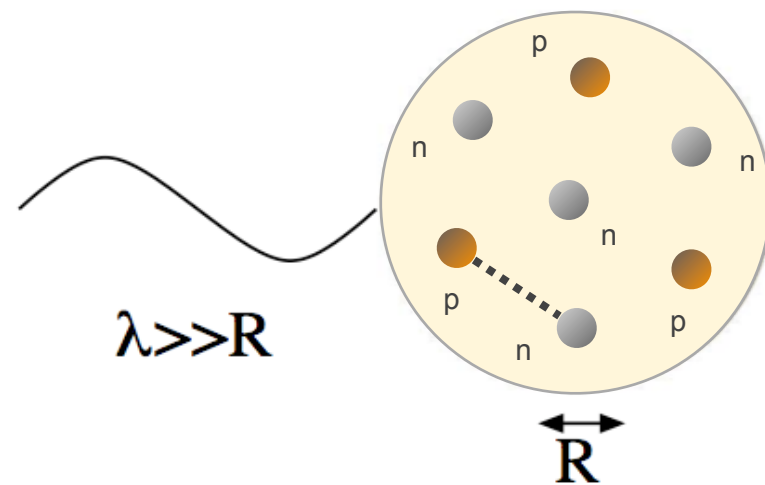
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	NN	3N	4N
LO $\mathcal{O}\left(\frac{Q^0}{\Lambda^0}\right)$			

Interaction challenges

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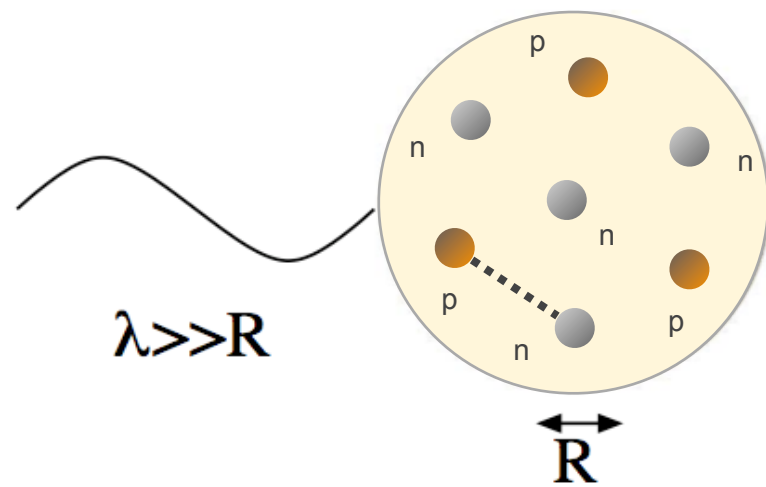
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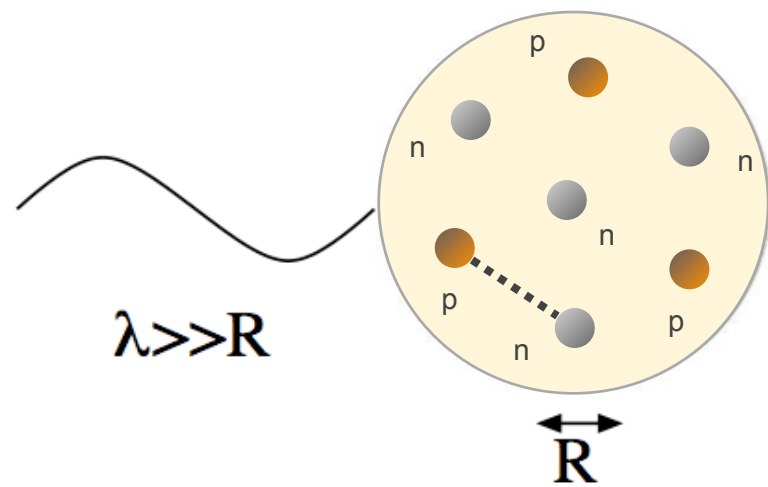
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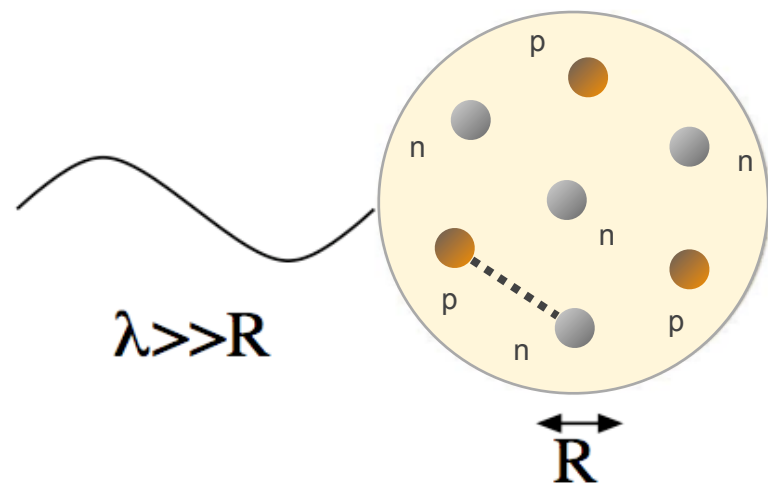
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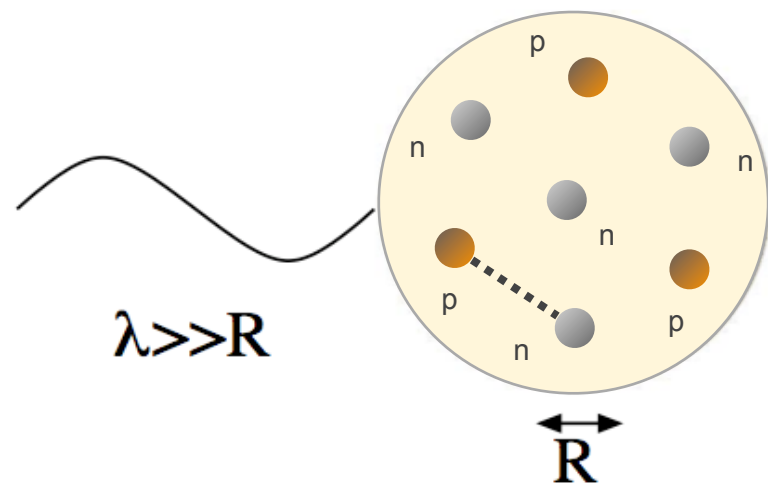
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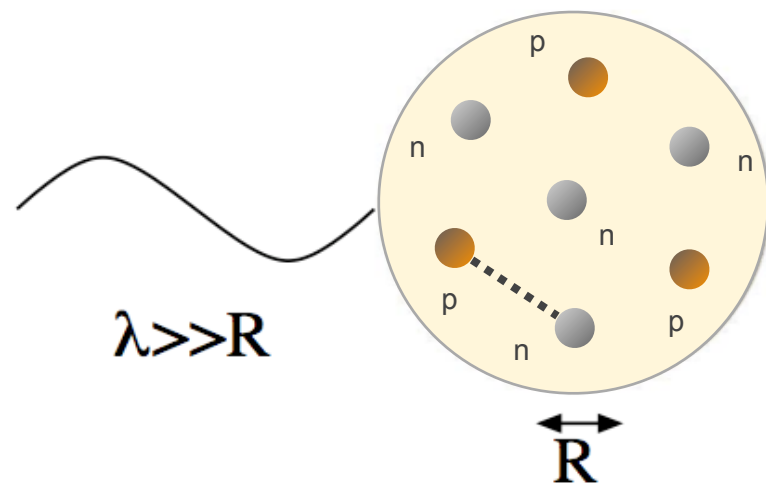
Systematic and can provide error estimates

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	+ ...	+ ...	+ ...

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Limited resolution at low energy
expand in powers $\frac{Q}{\Lambda_b}$

Systematic and can provide error estimates

Details of short distance physics not resolved,
but captured in short range couplings

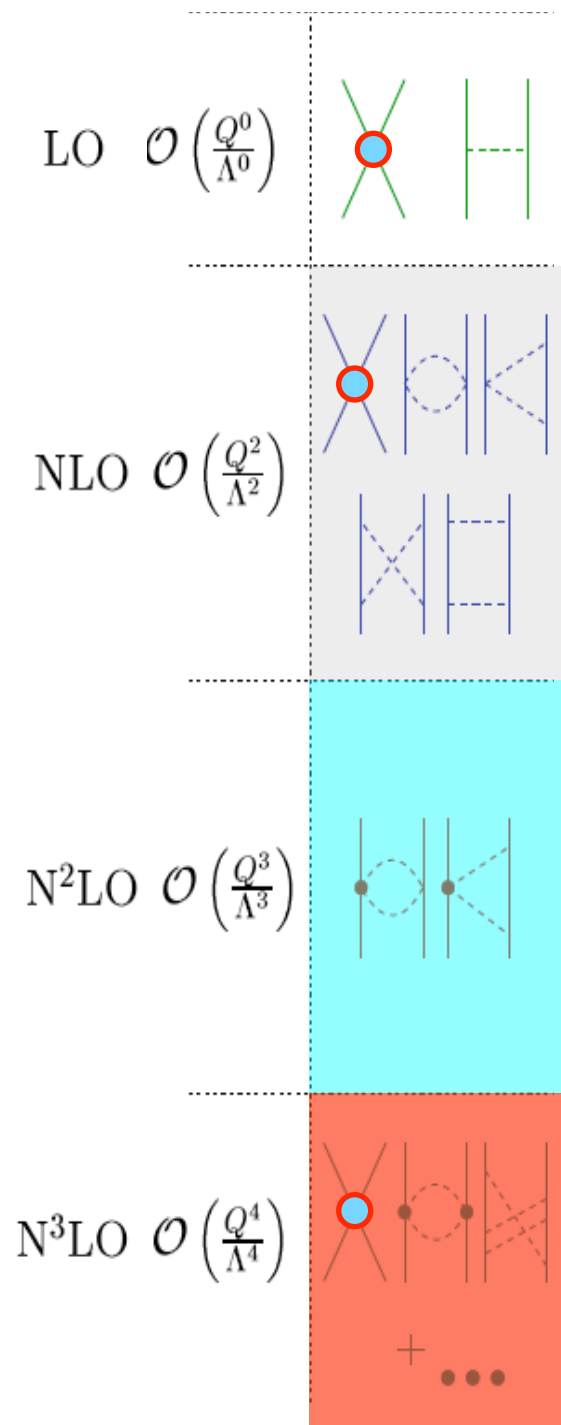
➡ fit to experiment

	NN	3N	4N
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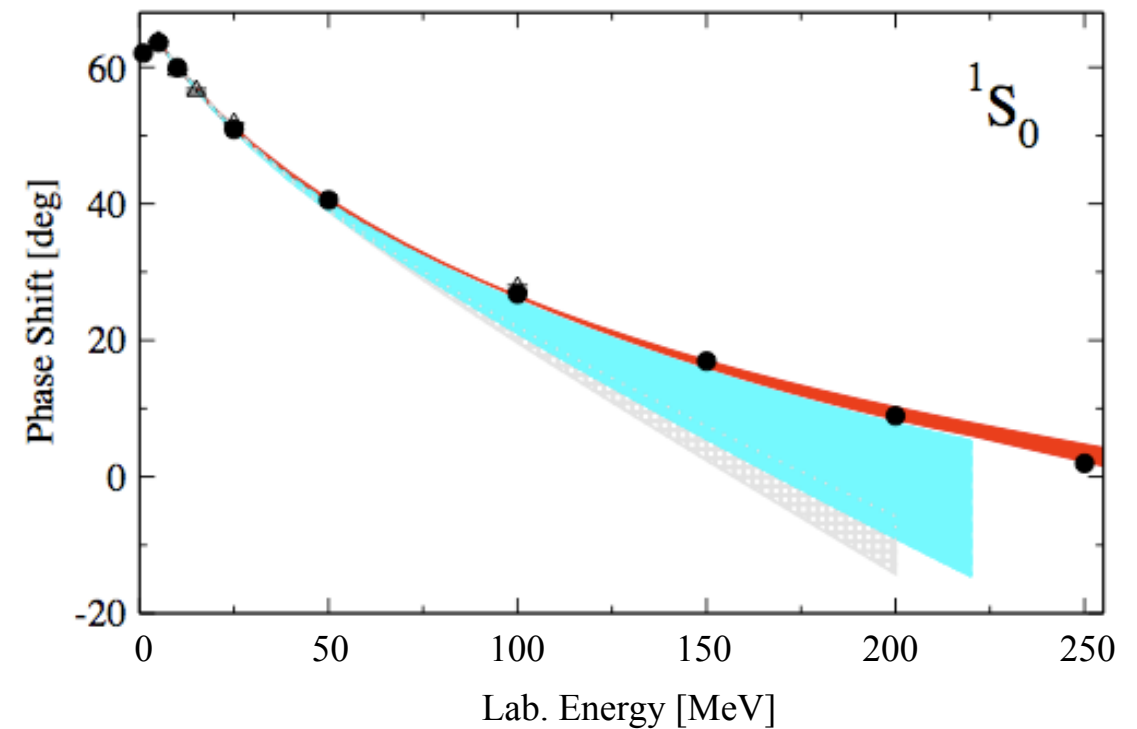
Interaction challenges

The Chiral Effective Field Theory Approach

- NN Sector -



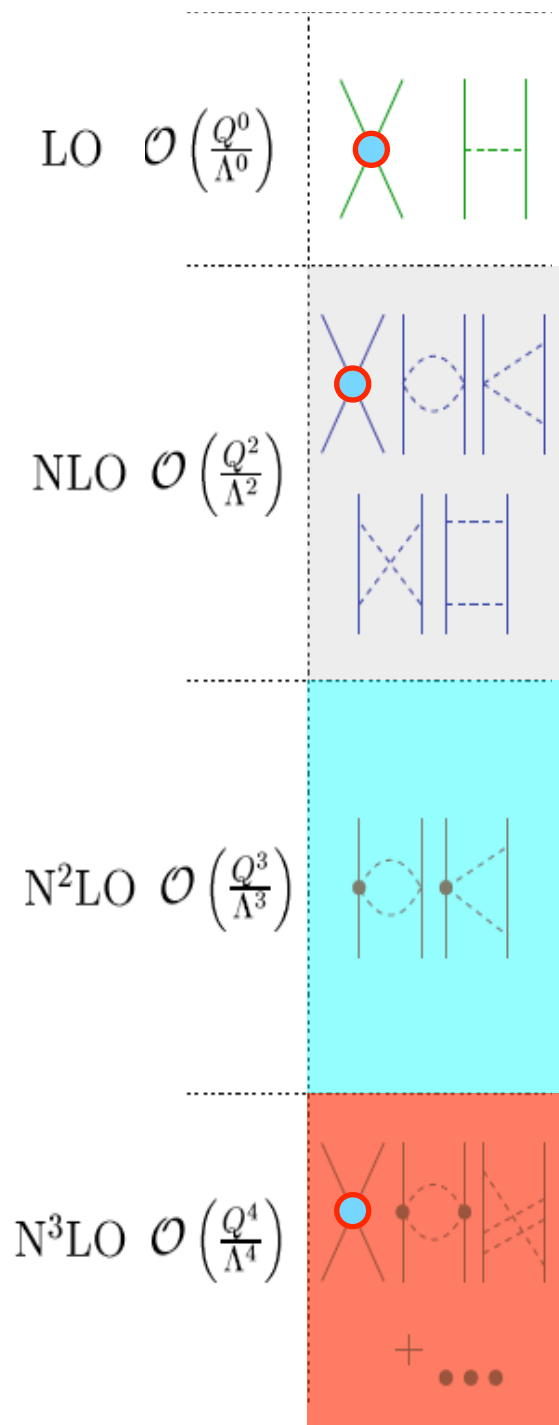
coupling constants fitted to
NN scattering phase-shifts



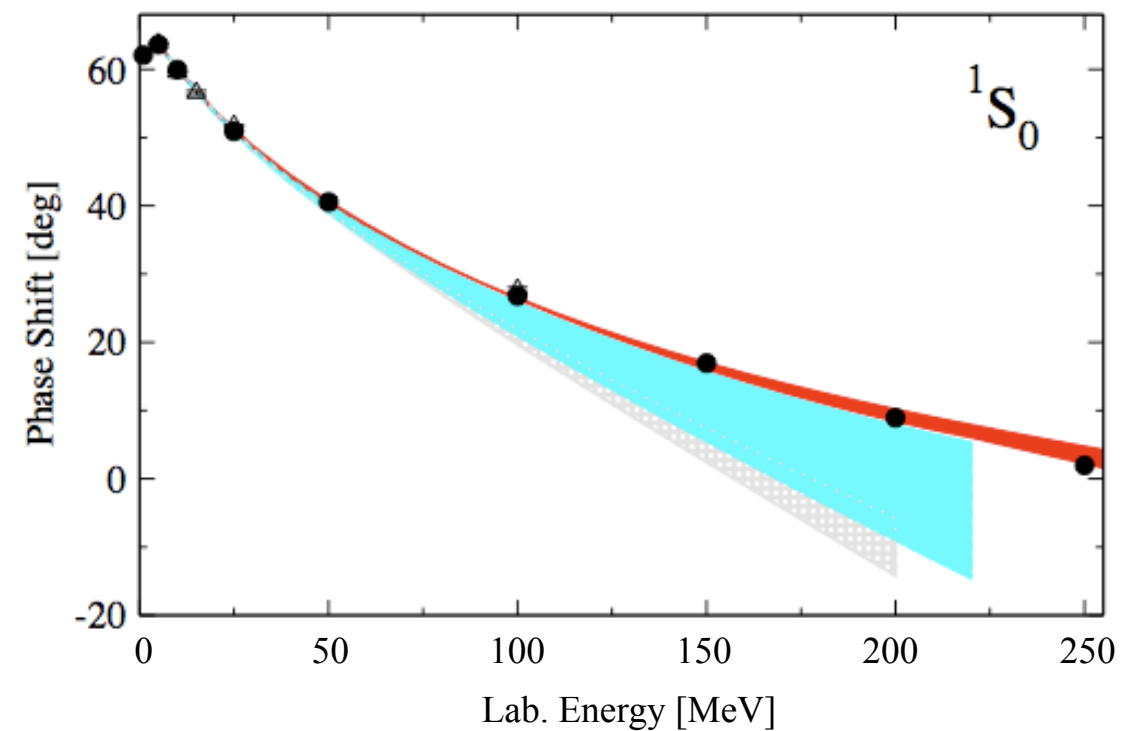
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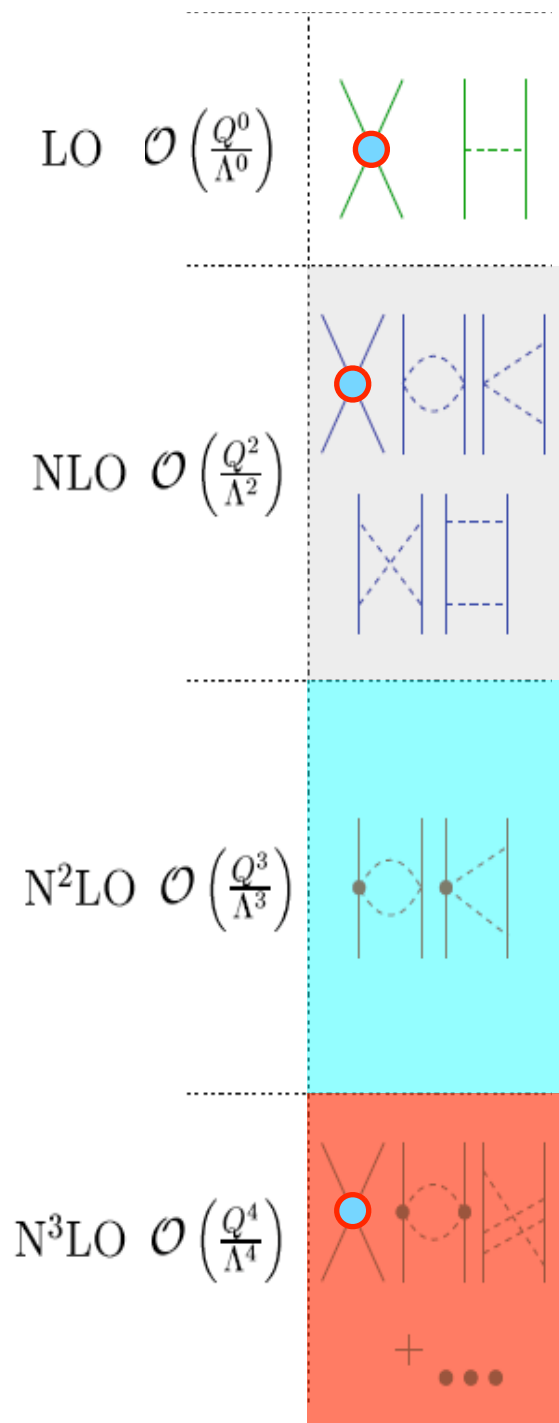
We have a resolution dependence!

Coupling constants run with the resolution scale Λ

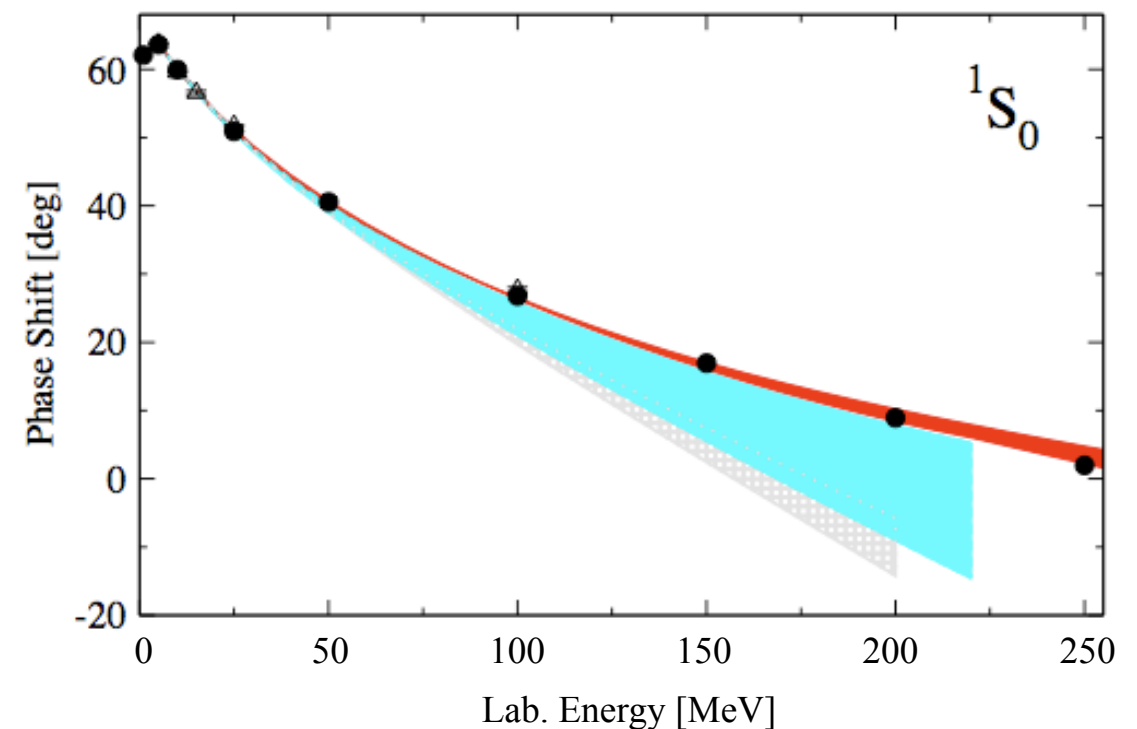
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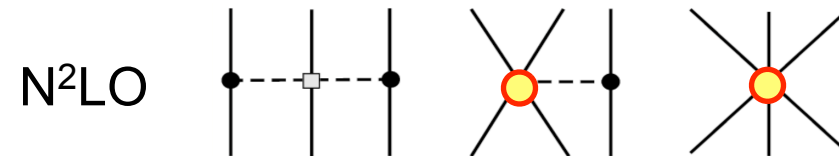
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Coupling constants run with the resolution scale Λ

The dependence on the cutoff leads to different potentials,
but observables should be cutoff independent

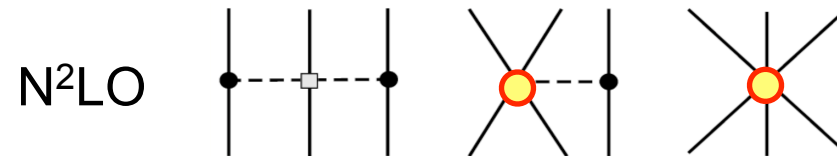
Interaction challenges

The Chiral Effective Field Theory Approach - 3N Sector -



Interaction challenges

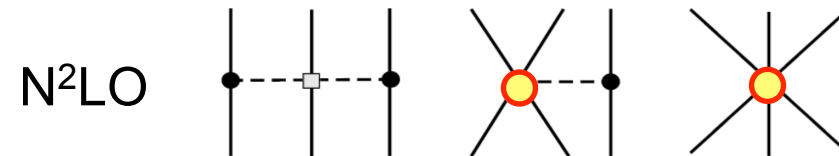
The Chiral Effective Field Theory Approach - 3N Sector -



- What is its origin? Nucleons are effective degrees of freedom

Interaction challenges

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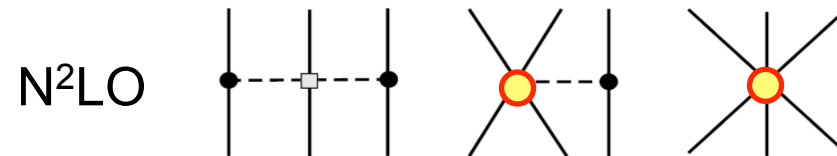


- What is its origin? Nucleons are effective degrees of freedom

“The three-body force is a force that does not exist in a two-nucleon system, but appears in a system with three objects or more” $A \geq 3$

Interaction challenges

The Chiral Effective Field Theory Approach - 3N Sector -



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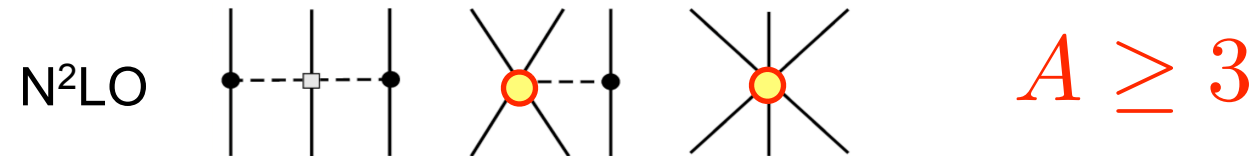
As an analogy, if we identify **objects** with **human beings** and **forces** with **emotions**, then **jealousy** is a good example of a **three-body force**: it is not felt as long as two-person are acting, but it shows up as soon as a third person enters the scene.



From N. Kalantar, FM50

Interaction challenges

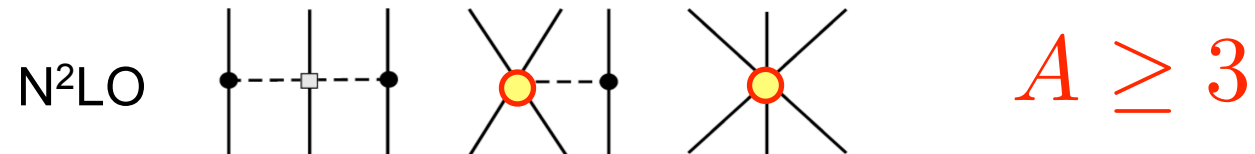
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- How to realize if they are important? By comparing theoretical calculations with two-nucleon forces only with experimental data

Interaction challenges

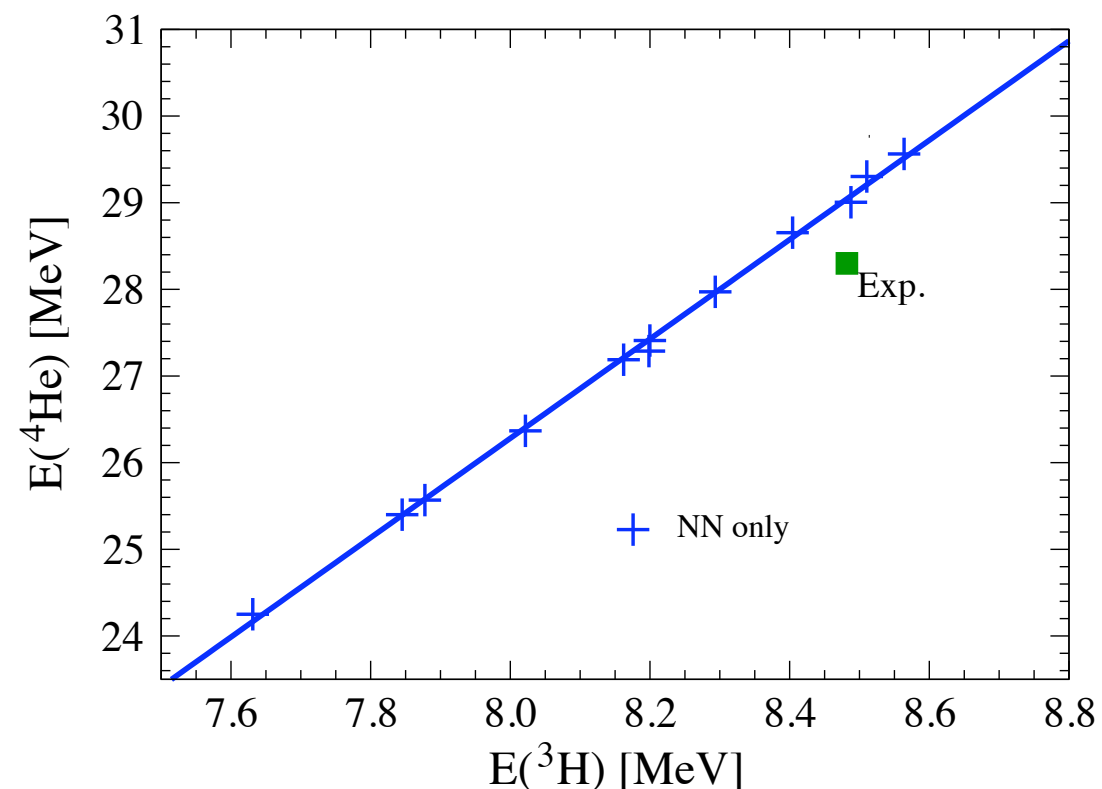
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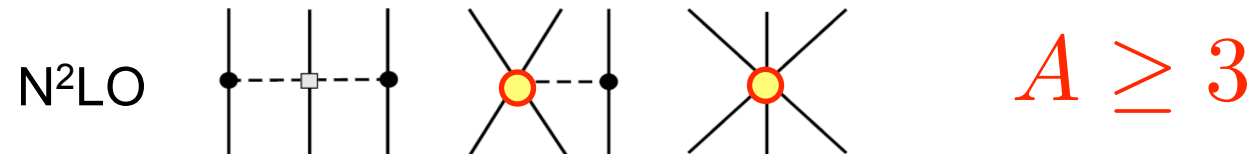
- How to constrain it?

By fitting the coupling constants to data for an observable which is sensitive to 3NF



Interaction challenges

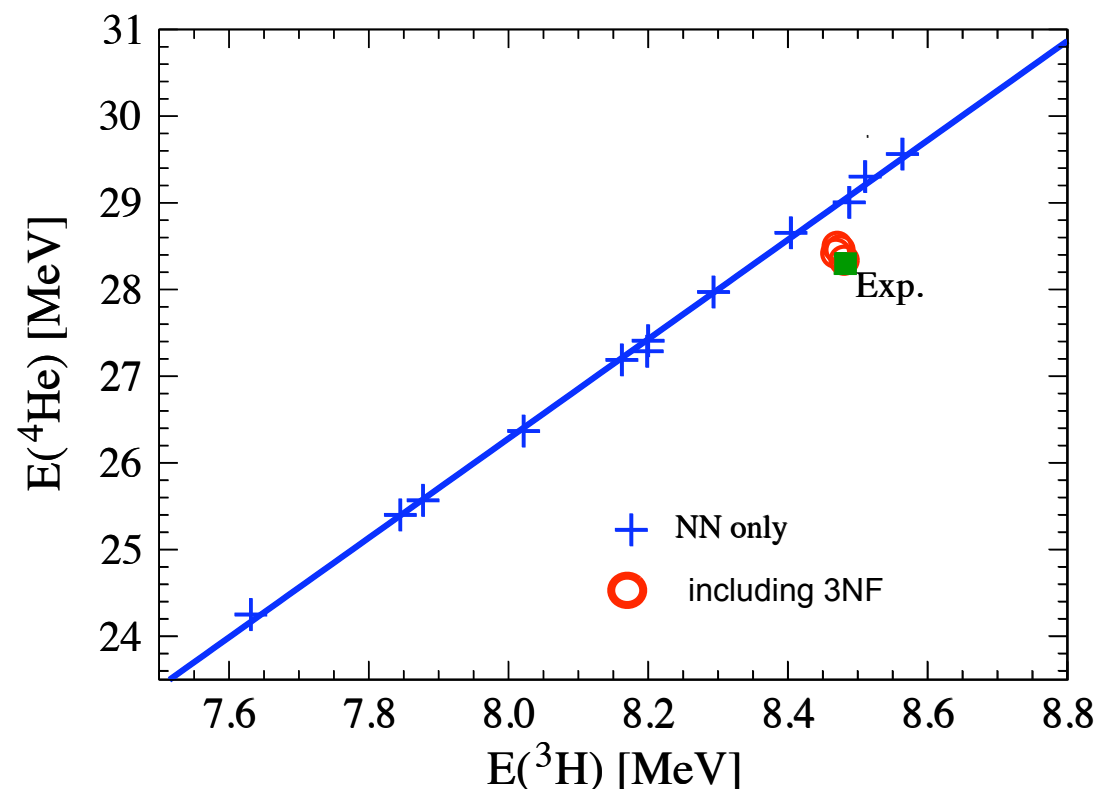
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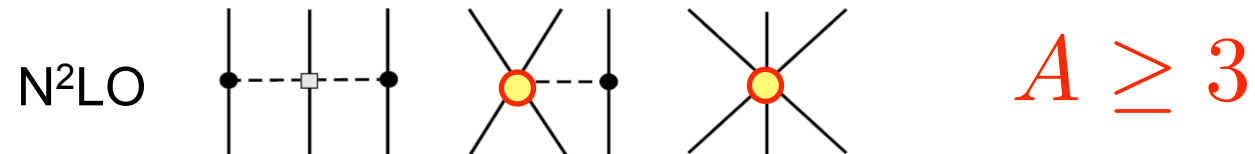
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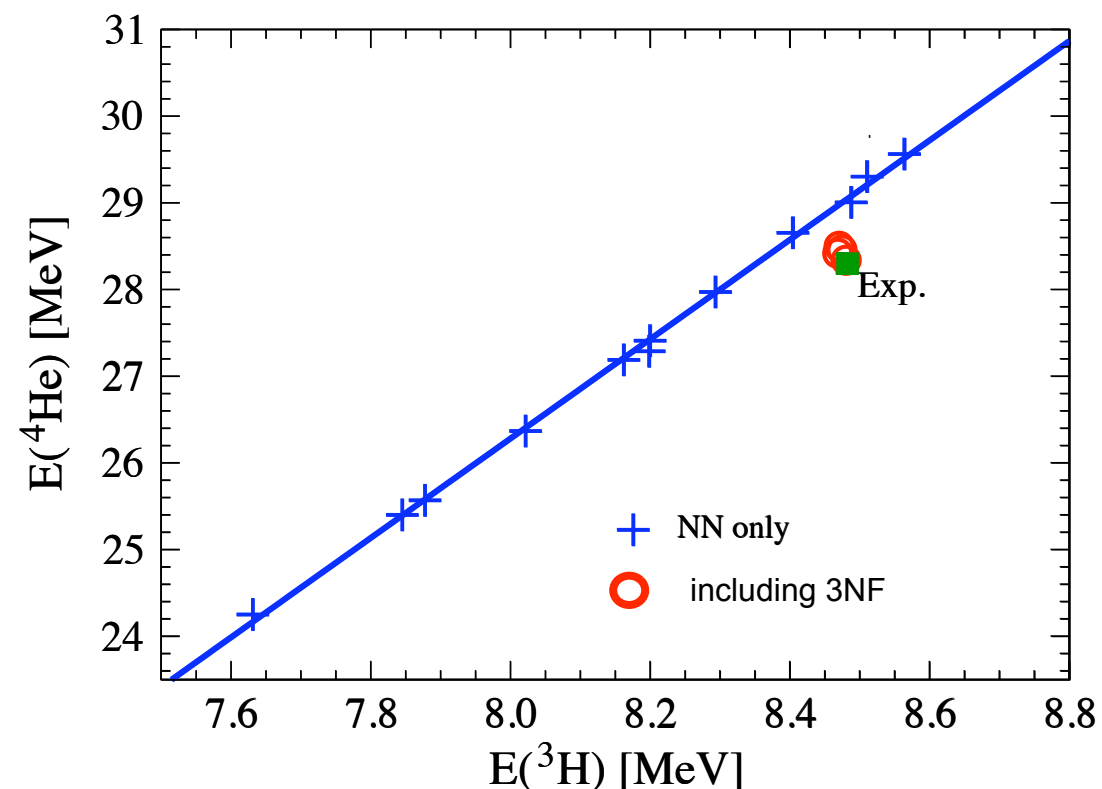


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- How to constrain it?

By fitting the coupling constants to data for an observable which is sensitive to 3NF

- Predict new observables!



Few- and many-body challenges

In the sector of few-body nuclei ($A < 5$) we have reached an incredible level of accuracy.

Challenge: develop new many-body methods that can extend the frontiers to heavier nuclei

Coupled Cluster Theory



Nucleus	E/A [MeV]	V/A [MeV]	$\Delta E/A$ [MeV]
${}^4\text{He}$	-5.99	-22.75	1.08
${}^{16}\text{O}$	-6.72	-30.69	1.25
${}^{40}\text{Ca}$	-7.72	-36.40	0.84
${}^{48}\text{Ca}$	-7.40	-37.97	1.27
${}^{48}\text{Ni}$	-6.02	-36.04	1.21

Hagen et al., PRL 101 (2008)

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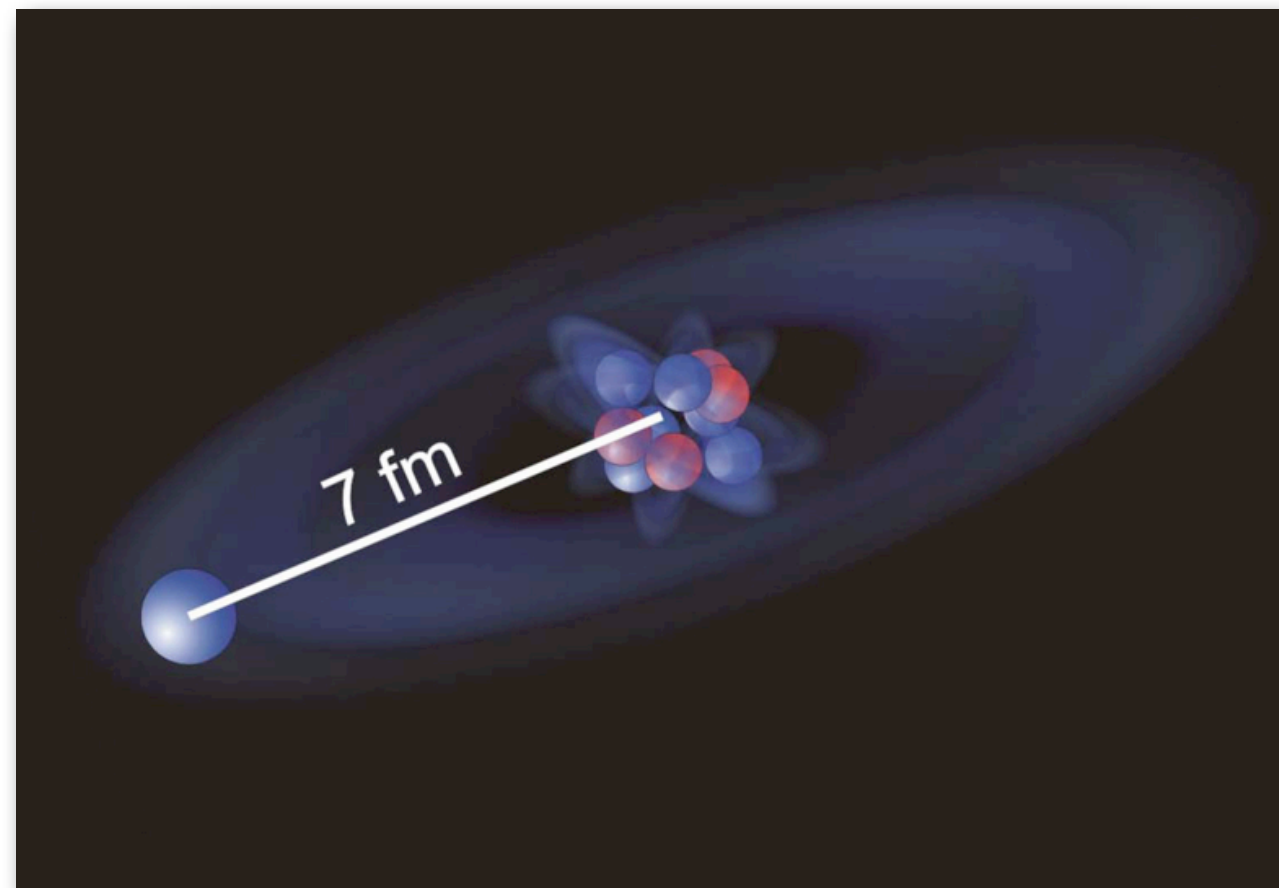
Future: advance ab-initio methods to heavier and neutron rich nuclei

The physics of Halo Systems



Moon Halo

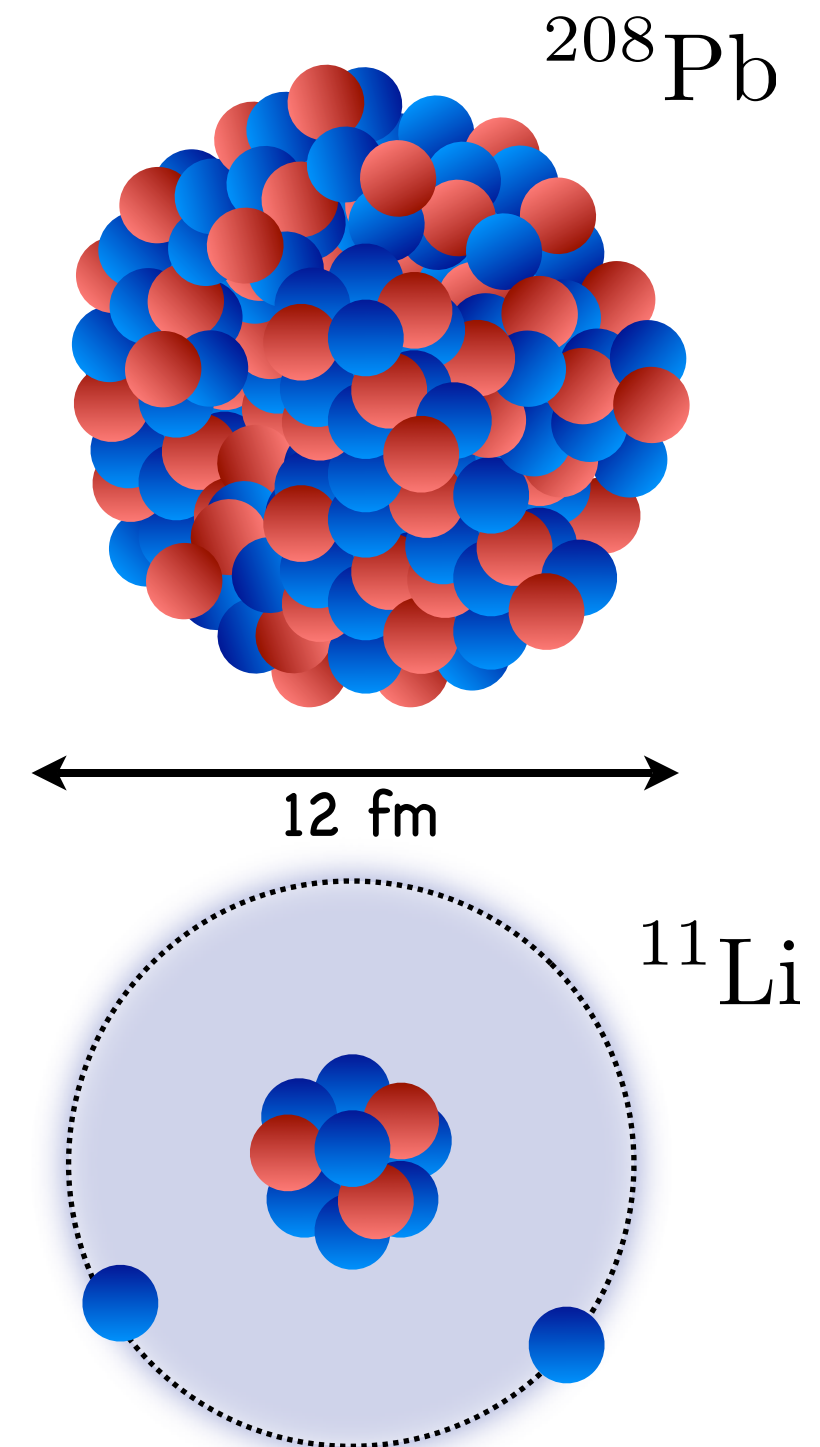
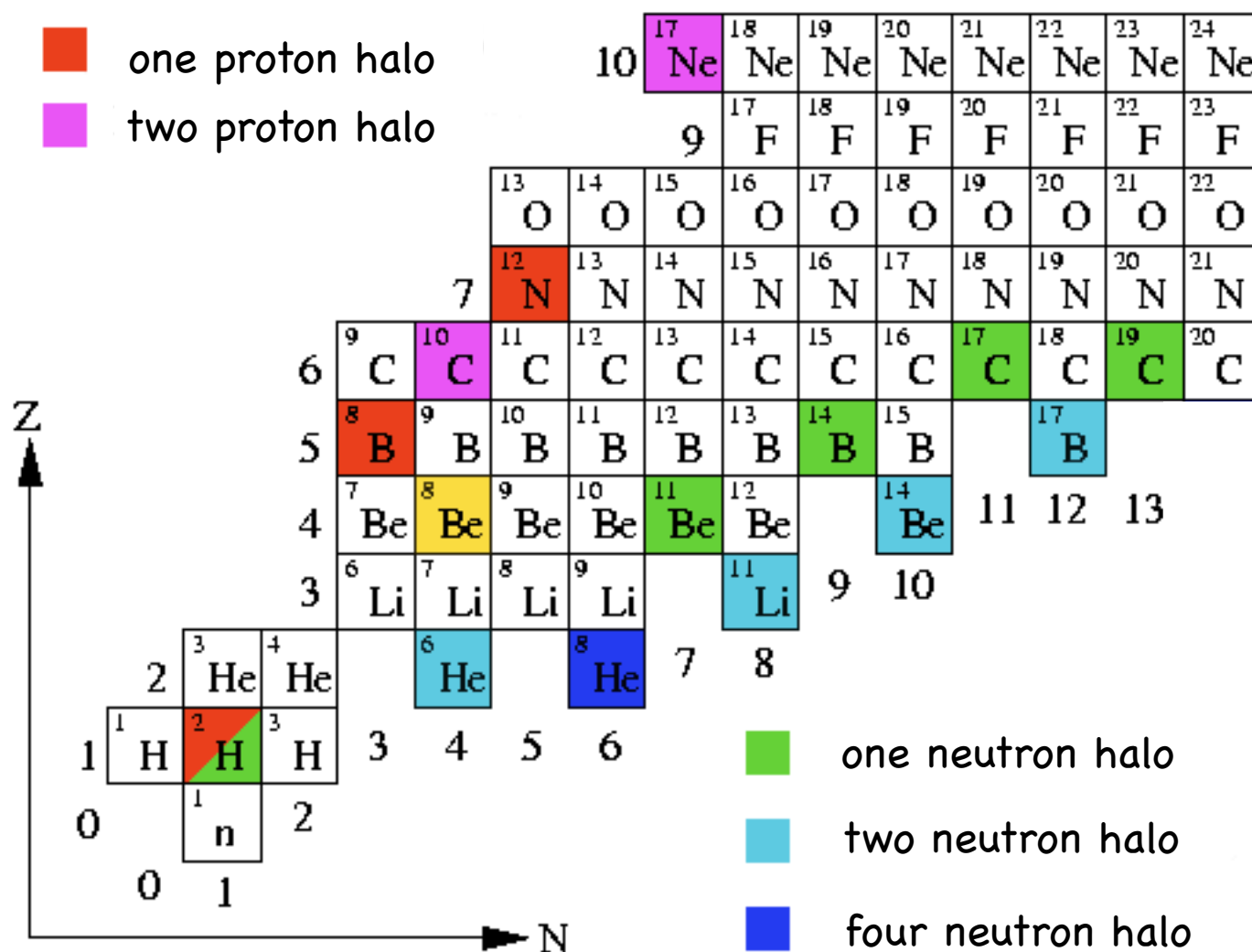
The physics of Halo Systems



Nuclear Halo



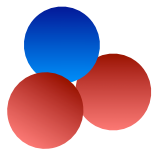
Halo nuclei



The helium isotope chain

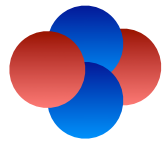
Shows many interesting features:

^3He



bound

^4He

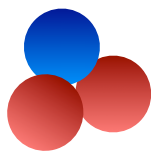


bound

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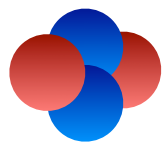
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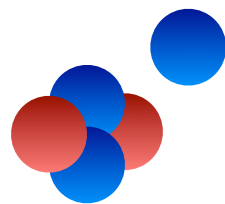
bound

^4He



bound

^5He

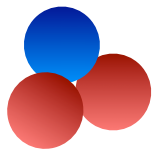


unbound

The helium isotope chain

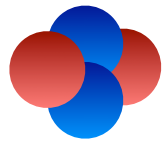
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^3He



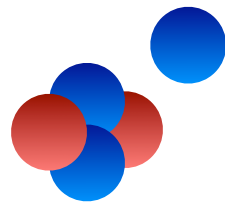
bound

^4He



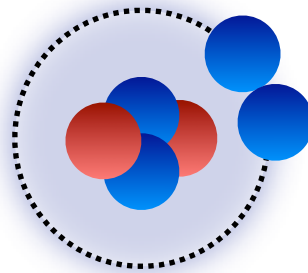
bound

^5He



unbound

^6He



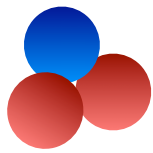
bound

halo

The helium isotope chain

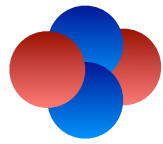
Shows many interesting features:

^3He



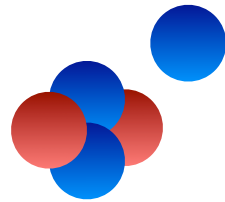
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^4He



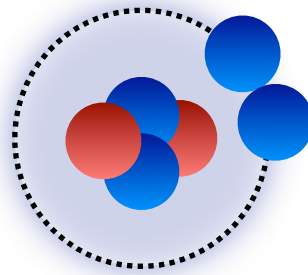
bound

^5He



unbound

^6He



bound

halo

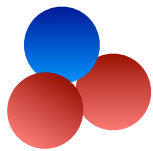
Borromean system



The helium isotope chain

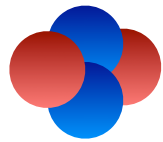
Shows many interesting features:

^3He



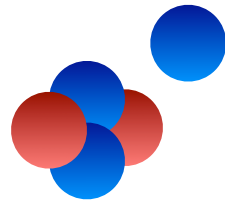
bound

^4He



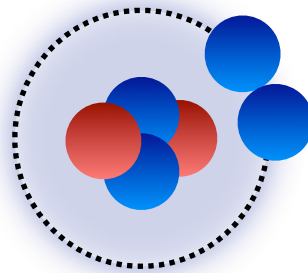
bound

^5He



unbound

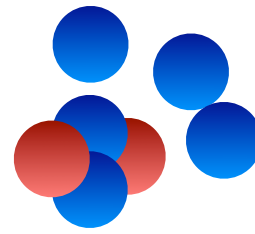
^6He



bound

halo

^7He



unbound

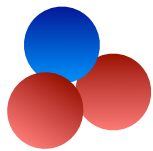
Borromean system



The helium isotope chain

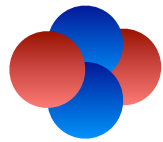
Shows many interesting features:

^3He



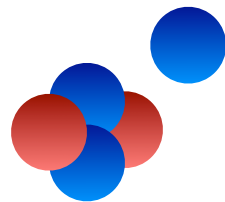
bound

^4He



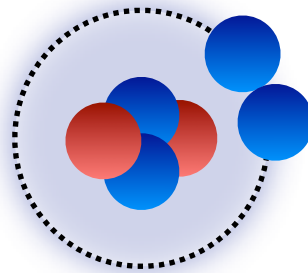
bound

^5He



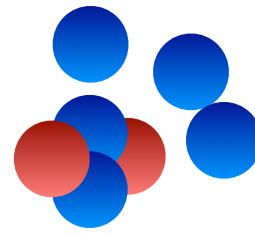
unbound

^6He



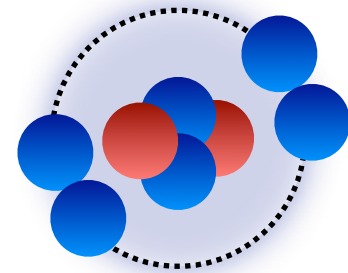
bound
halo

^7He



unbound

^8He



bound
halo

...

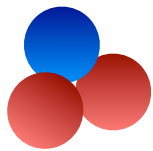
Borromean system



The helium isotope chain

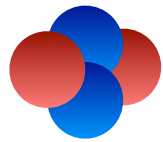
Shows many interesting features:

^3He



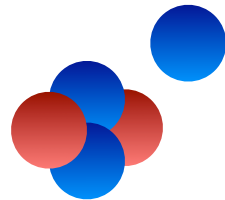
bound

^4He



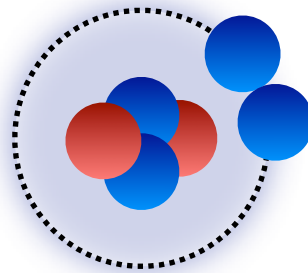
bound

^5He



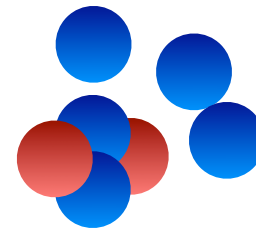
unbound

^6He



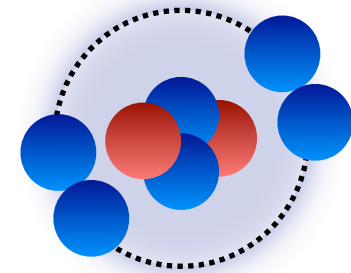
bound
halo

^7He



unbound

^8He



bound
halo

...

Borromean system



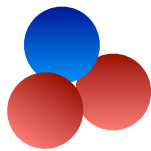
Most exotic nucleus
"on earth"

$$\frac{N}{Z} = 3$$

The helium isotope chain

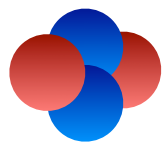
Shows many interesting features:

^3He



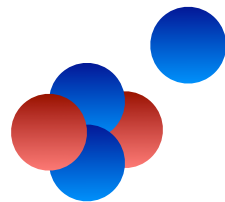
bound

^4He



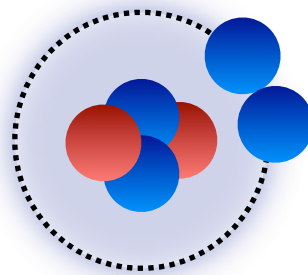
bound

^5He



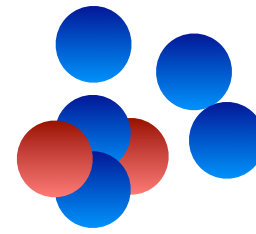
unbound

^6He



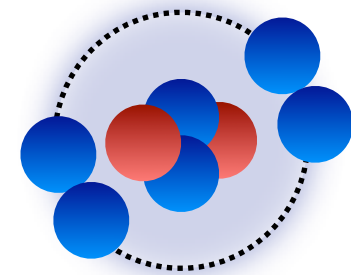
bound
halo

^7He



unbound

^8He



bound
halo

...

Borromean system



lives 806 ms

Most exotic nucleus
"on earth"

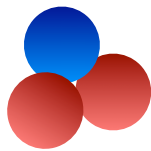
$$\frac{N}{Z} = 3$$

lives 108 ms

The helium isotope chain

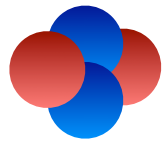
Shows many interesting features:

^3He



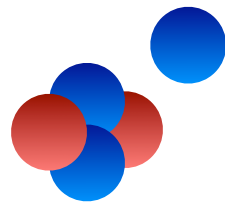
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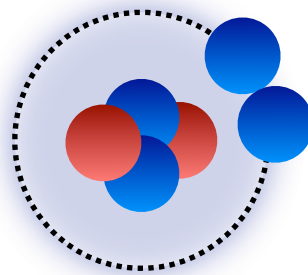
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^5He



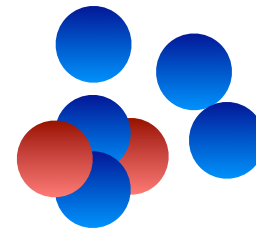
unbound

^6He



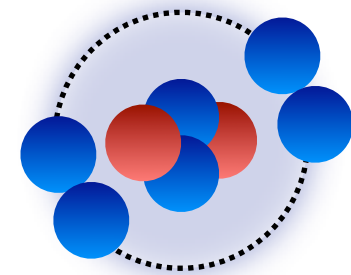
bound
halo

^7He



unbound

^8He



bound
halo

...

Borromean system



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$$\frac{N}{Z} = 3$$

lives 108 ms

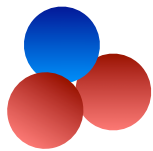
Synthesized in the laboratory



The helium isotope chain

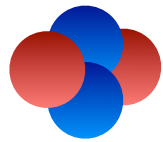
Shows many interesting features:

^3He



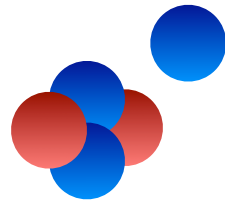
bound

^4He



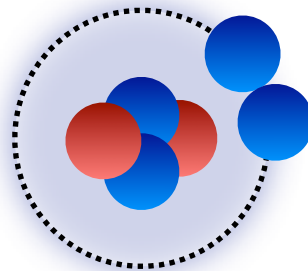
bound

^5He



unbound

^6He



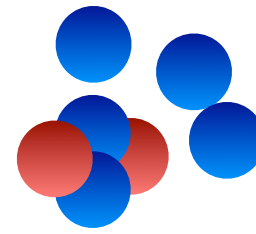
bound
halo

Borromean system



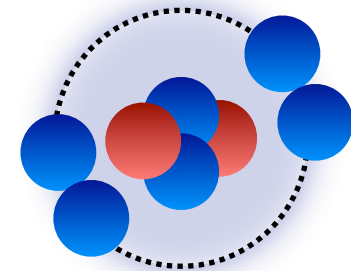
lives 806 ms

^7He



unbound

^8He



bound
halo

Most exotic nucleus
"on earth"

$$\frac{N}{Z} = 3$$

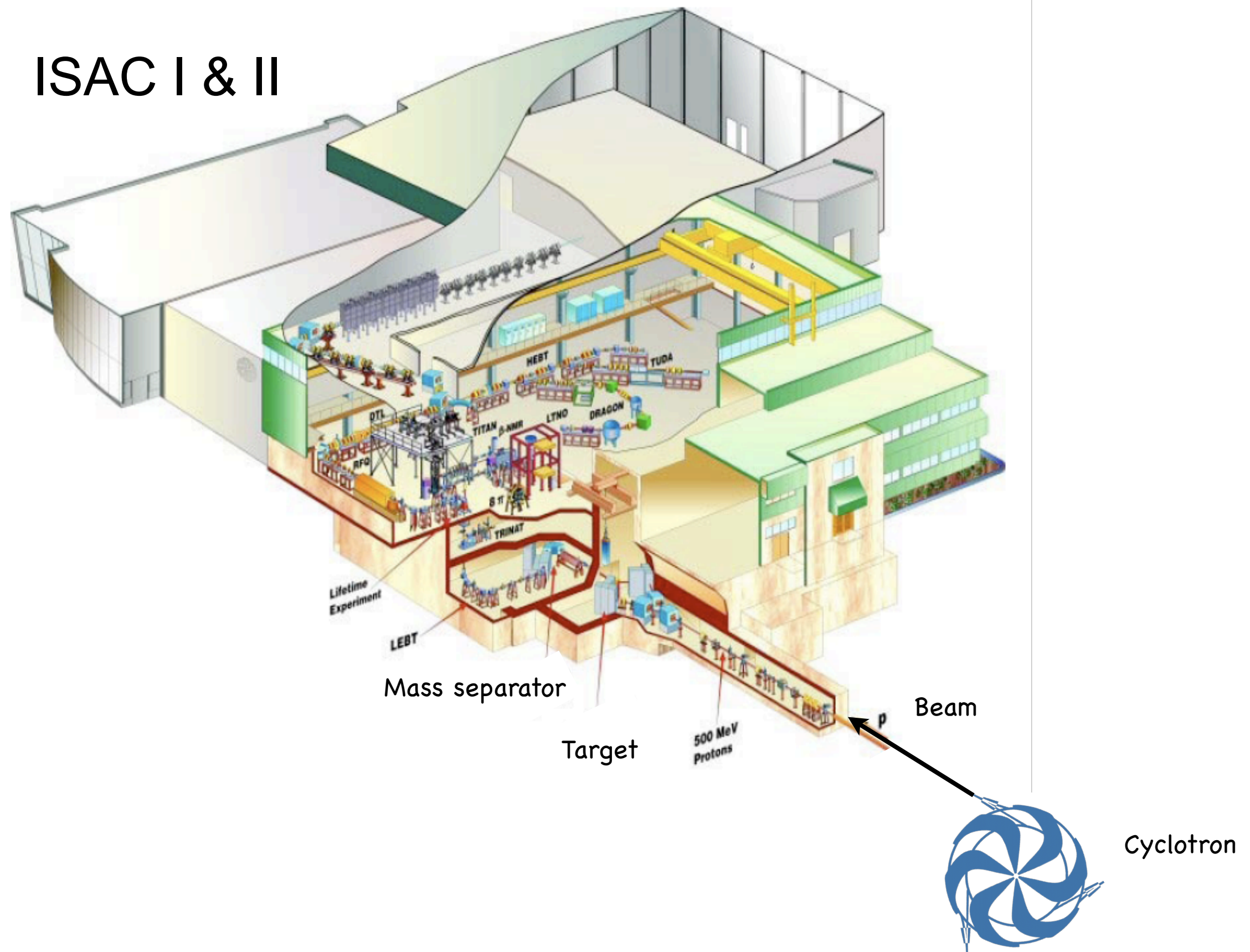
lives 108 ms

Synthesized in the laboratory



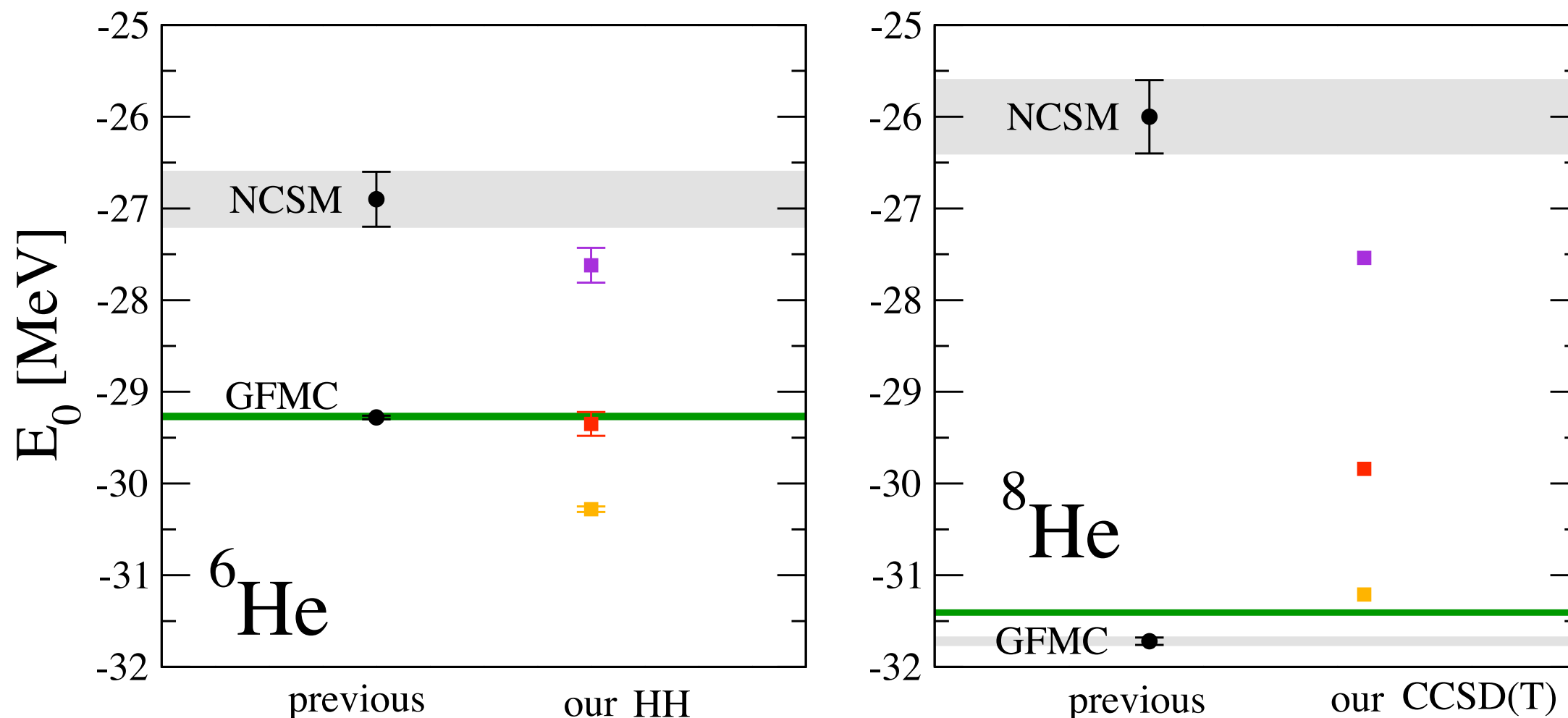
Production of rare isotopes at TRIUMF

ISAC I & II



Ab initio calculations for halo nuclei

S.Bacca et al., [arXiv:0902.1696](https://arxiv.org/abs/0902.1696)



Experimental data



Previous calculations:

NCSM NN only

GFMC NN+3NF

Our calculations:

low-momentum EFT NN force

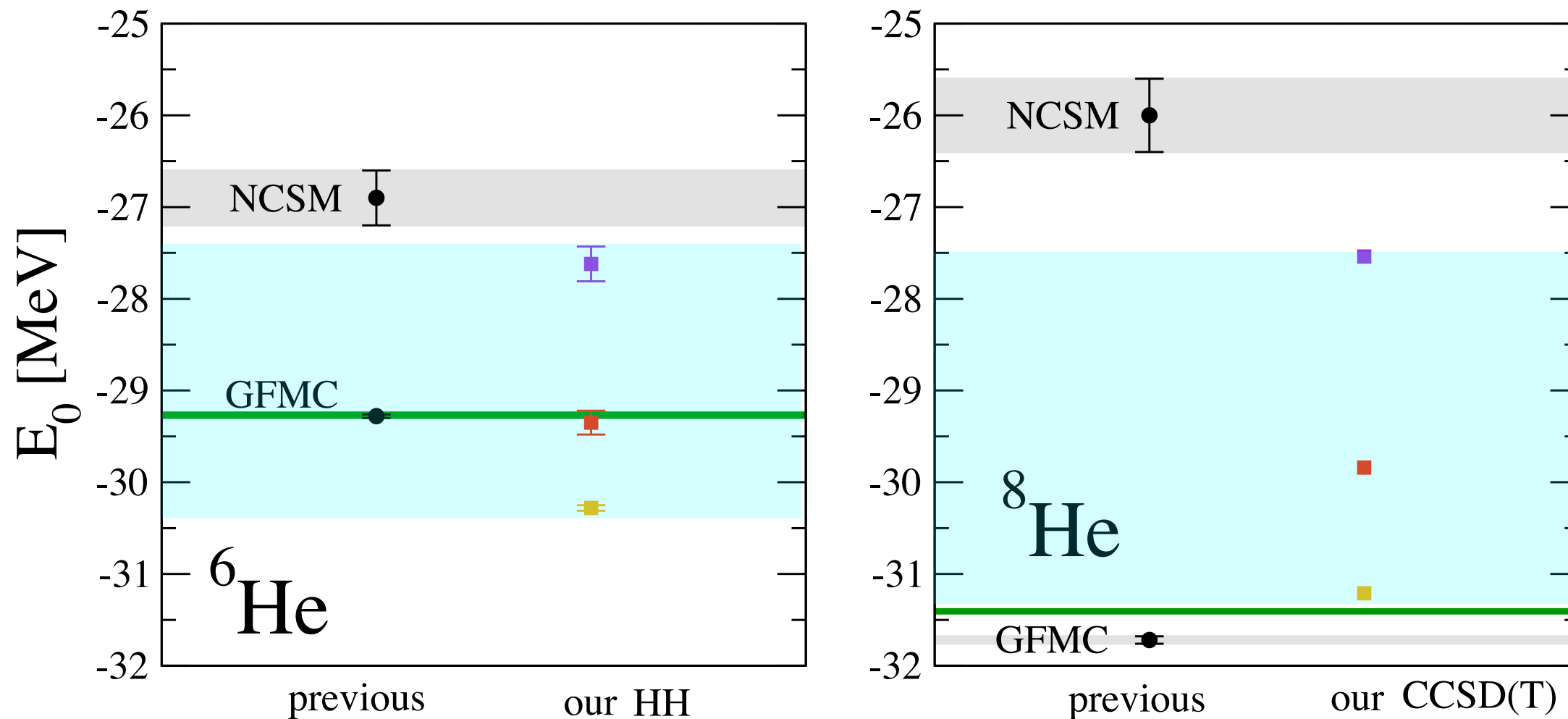
■ $\Lambda = 1.8 \text{ fm}^{-1}$

■ $\Lambda = 2.0 \text{ fm}^{-1}$

■ $\Lambda = 2.4 \text{ fm}^{-1}$

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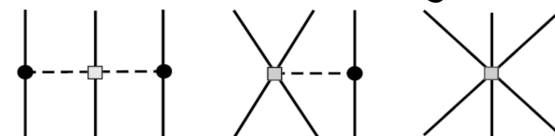
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Previous calculations:

NCSM NN only

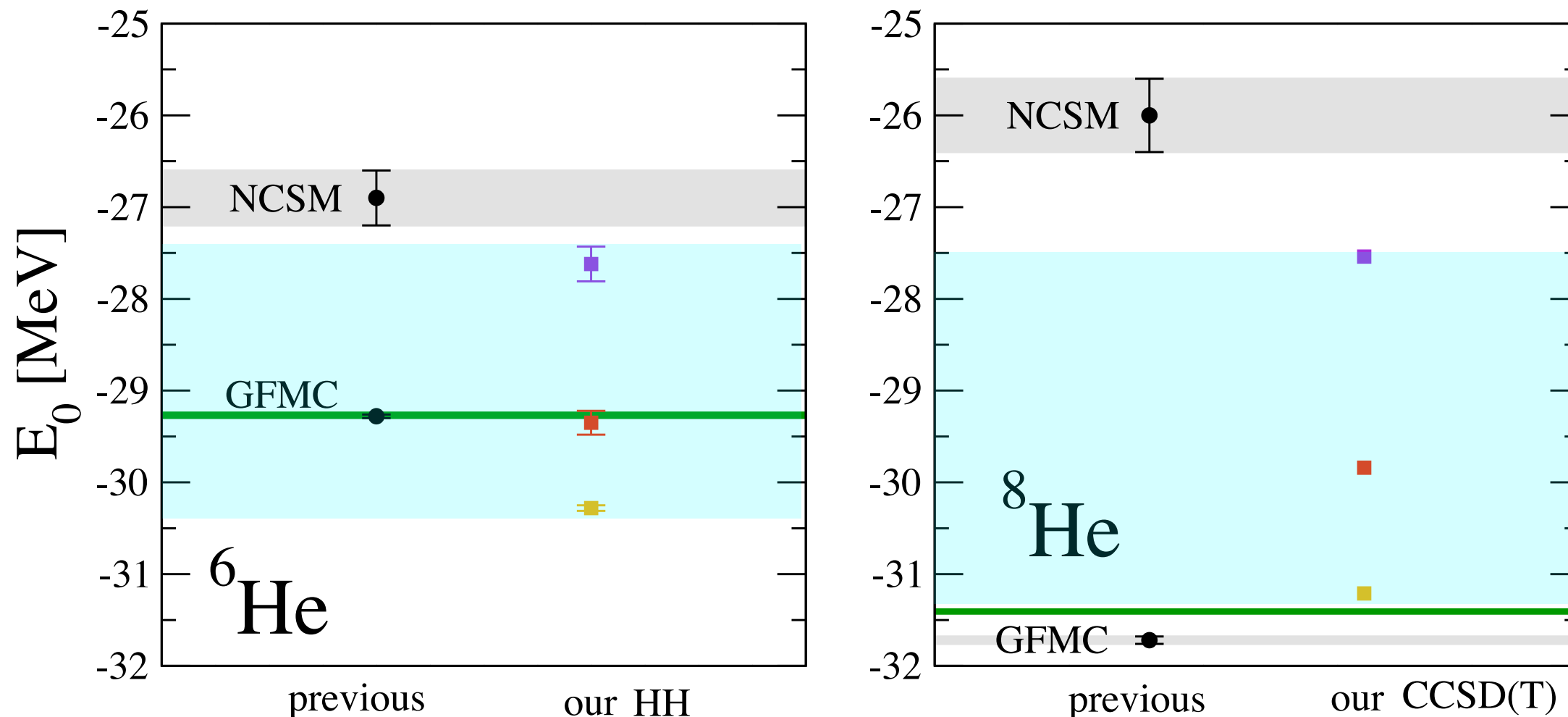
GPMC NN+3NF

estimates error in neglected



Ab initio calculations for halo nuclei

S.Bacca et al., arXiv:0902.1696



Experimental data

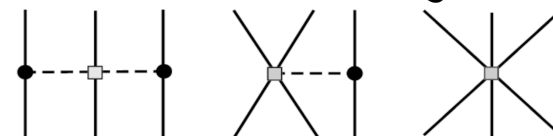


Our calculations:

low-momentum EFT NN force

- $\Lambda = 1.8 \text{ fm}^{-1}$
- $\Lambda = 2.0 \text{ fm}^{-1}$
- $\Lambda = 2.4 \text{ fm}^{-1}$

estimates error in neglected



Future

Previous calculations:

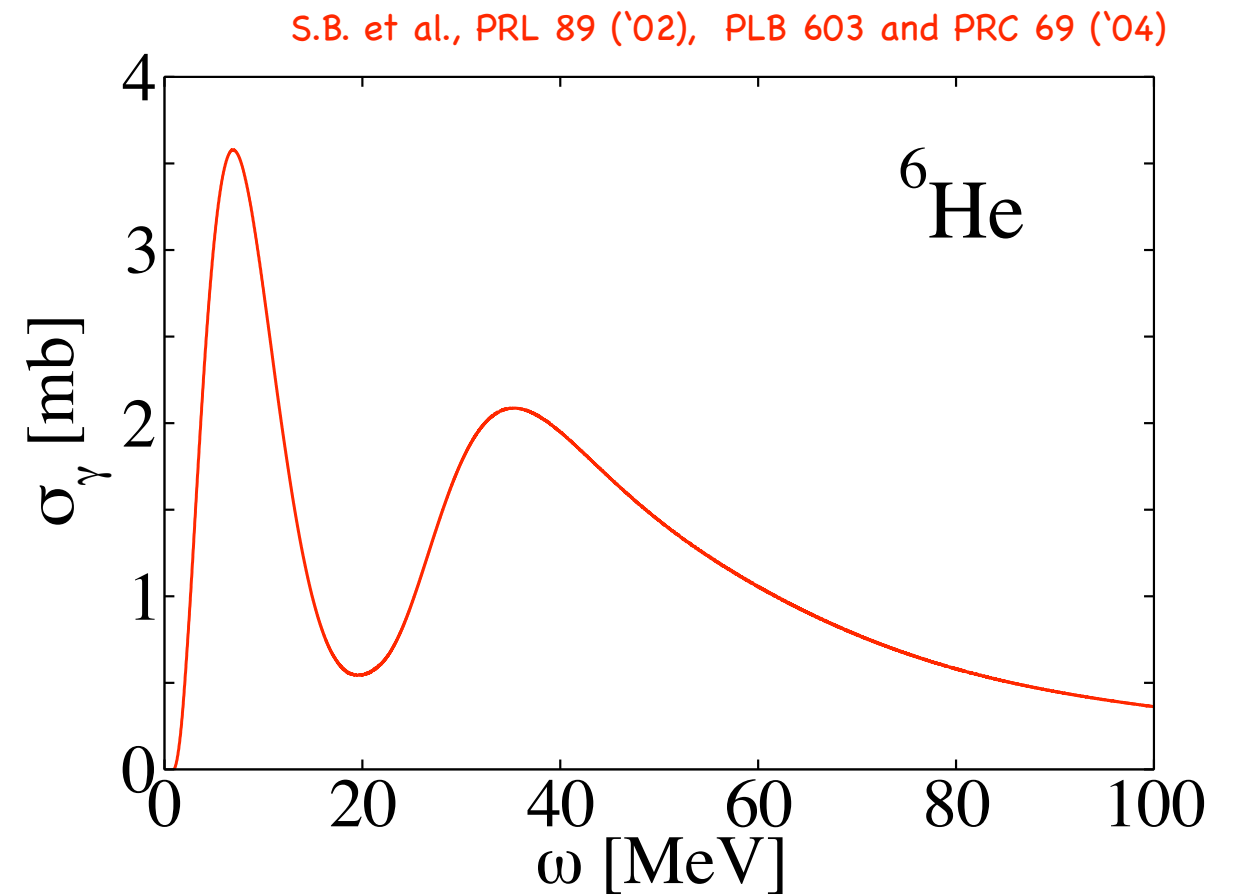
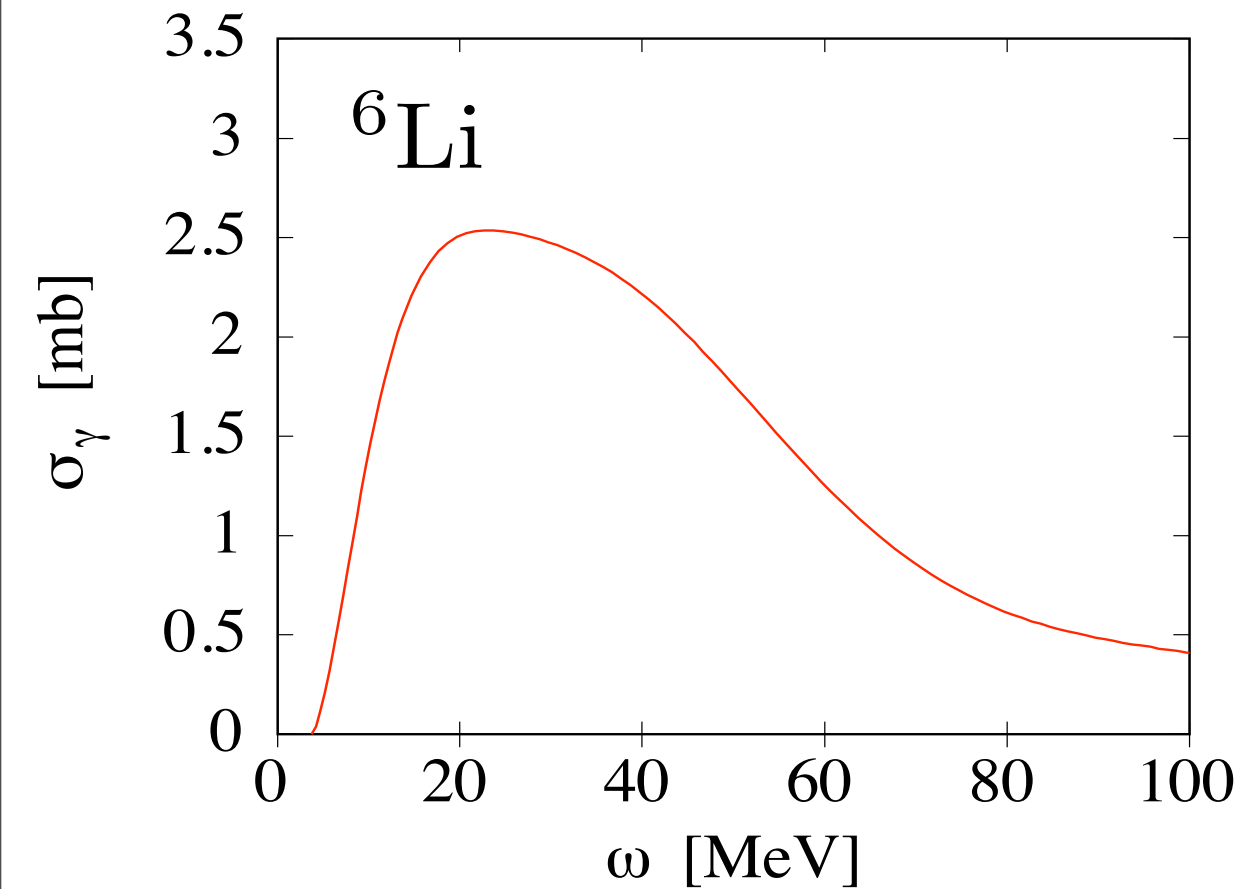
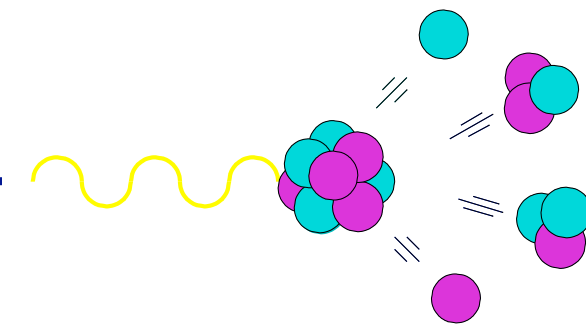
NCSM NN only

GPMC NN+3NF

- Include 3NF
- Apply to other isotope chains with halo features

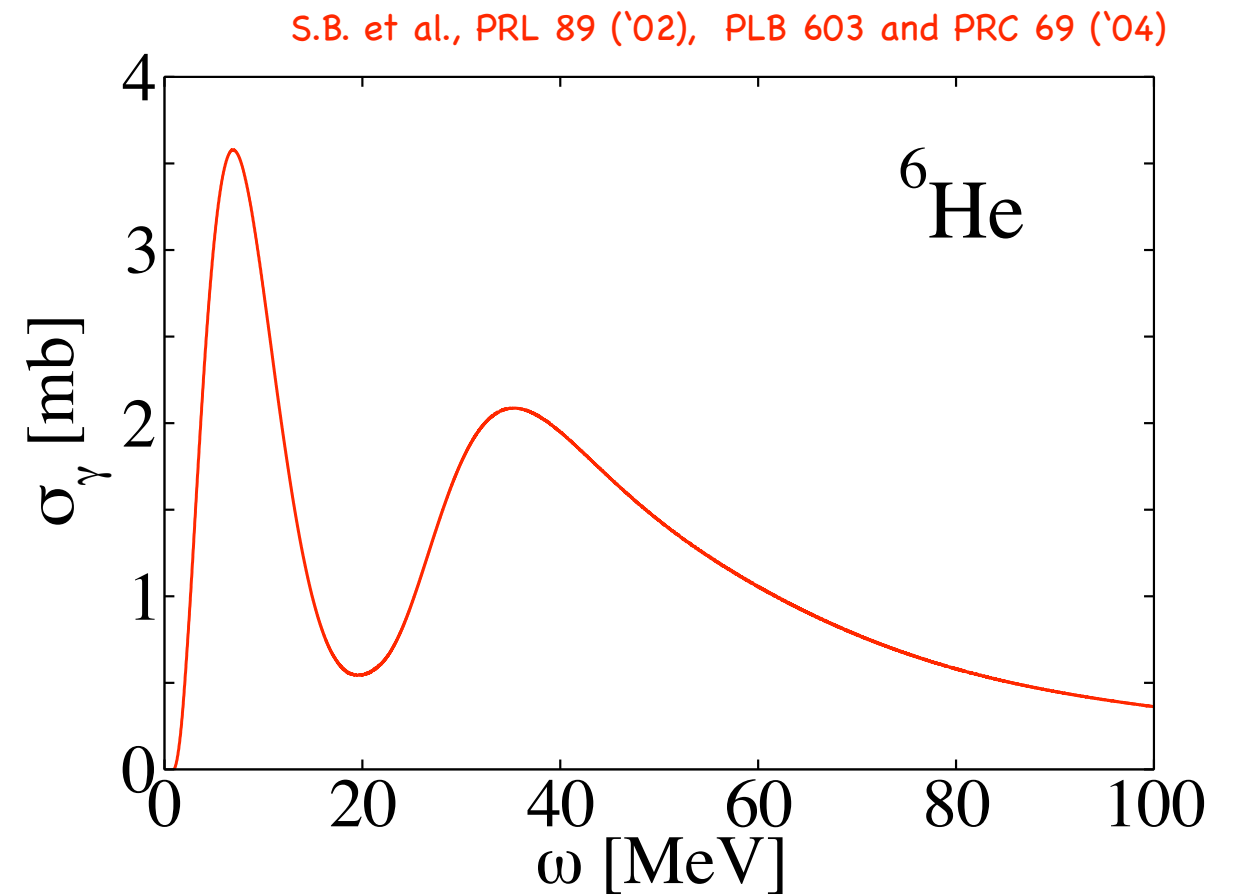
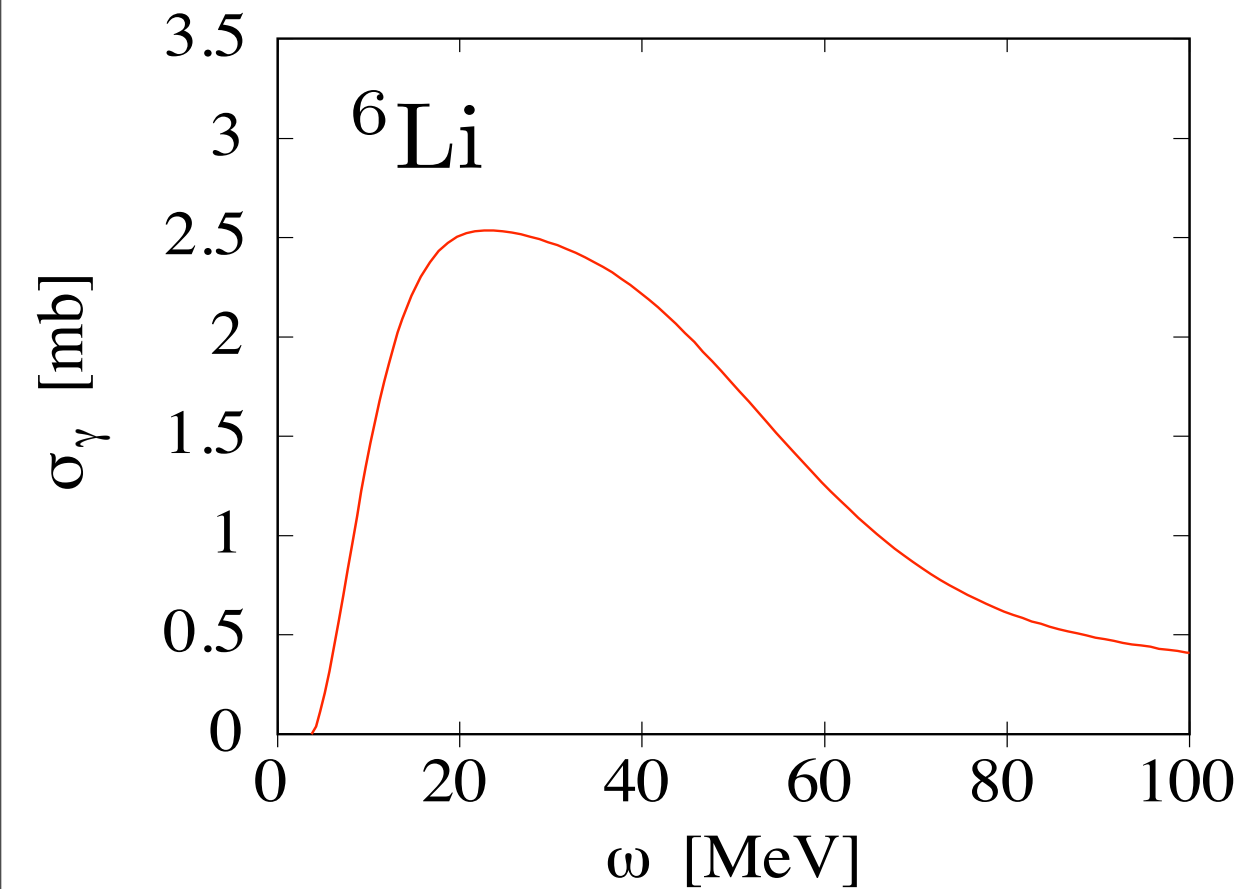
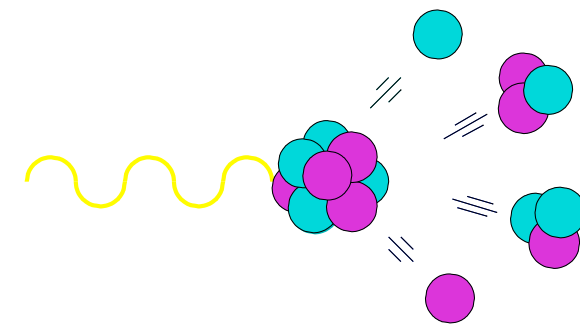
Nuclear Reactions: photo-absorption

Semi-realistic NN force

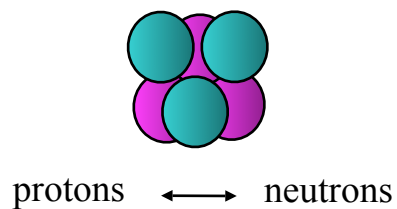


Nuclear Reactions: photo-absorption

Semi-realistic NN force

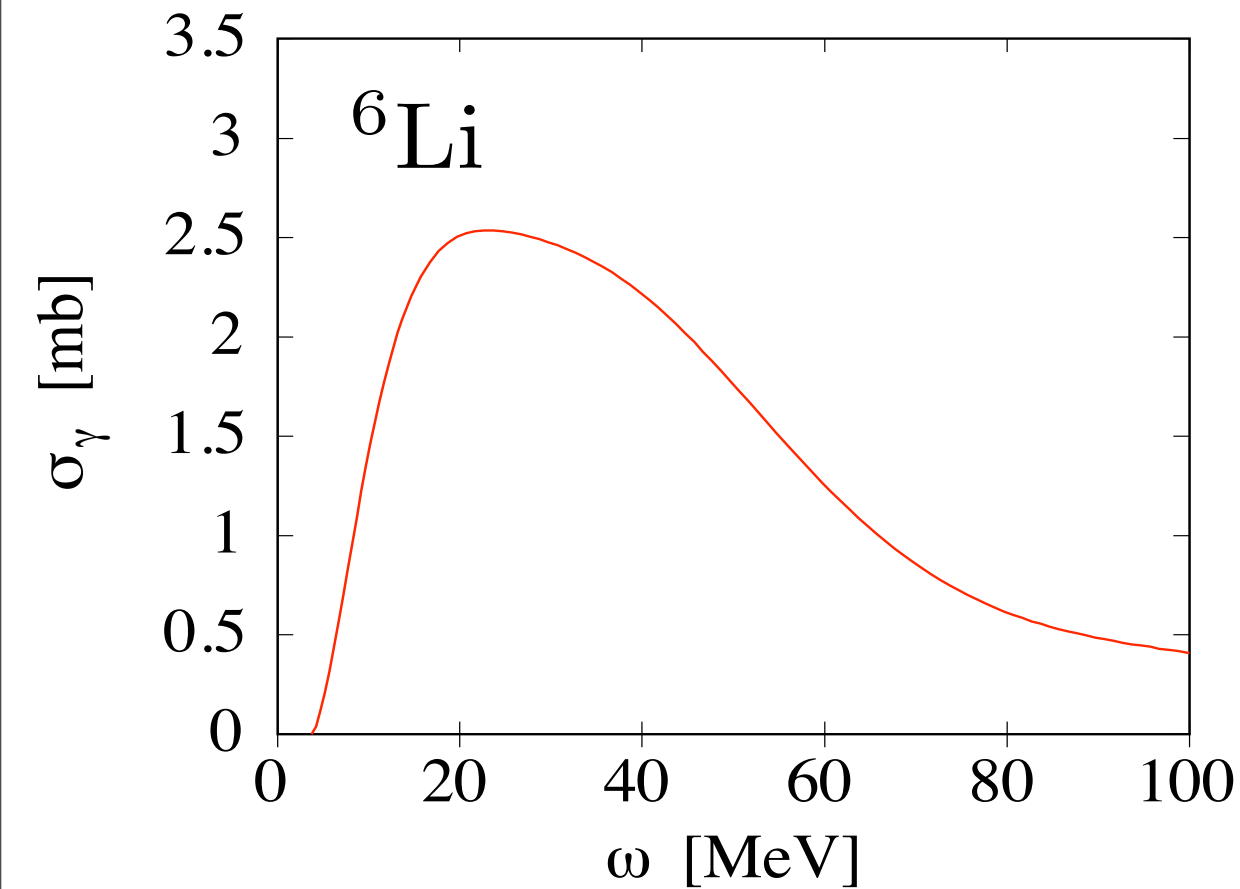
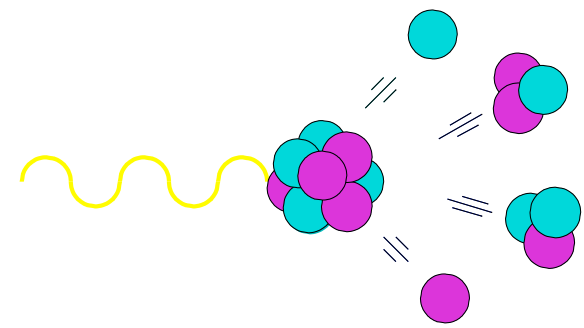


Giant Dipole Resonance

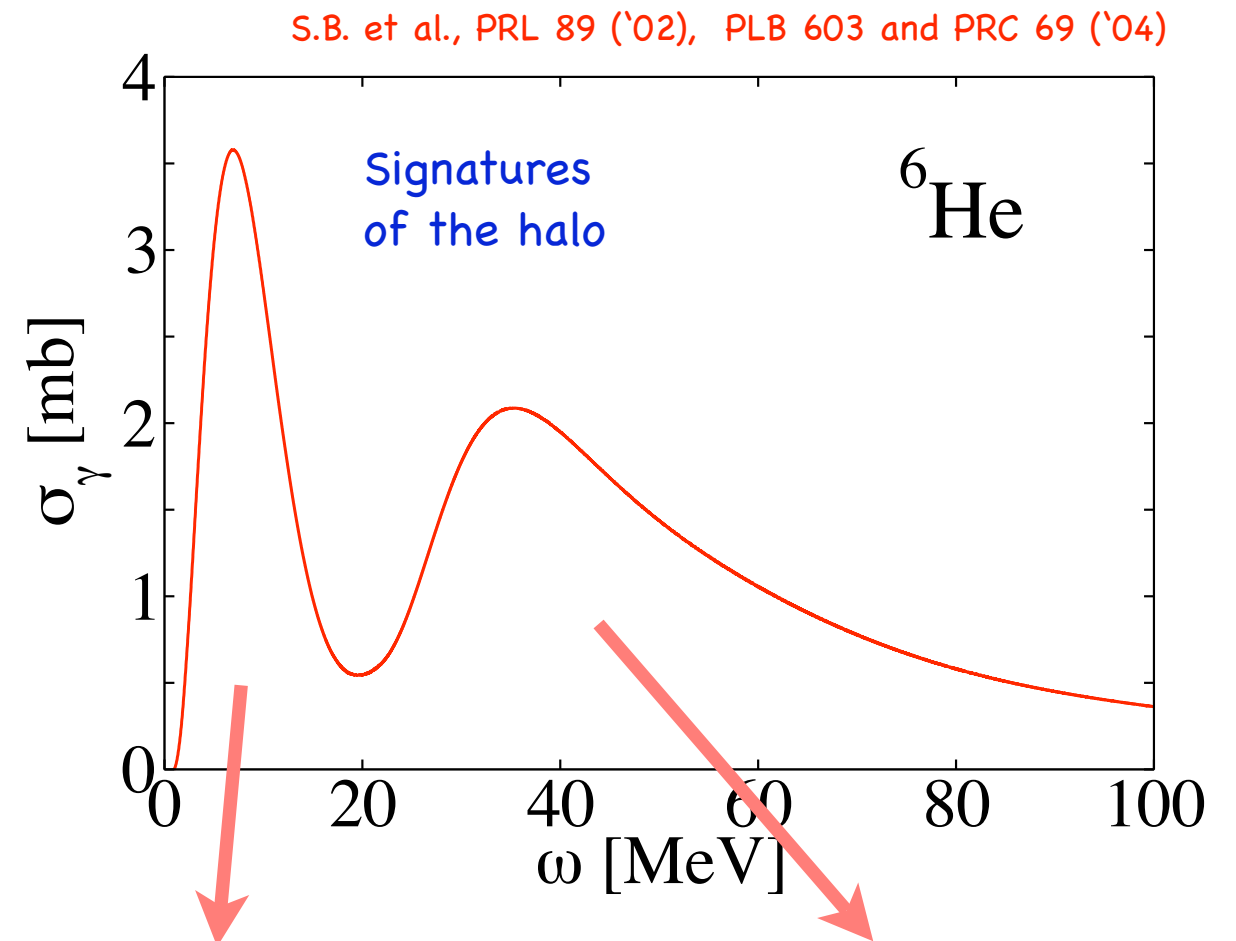
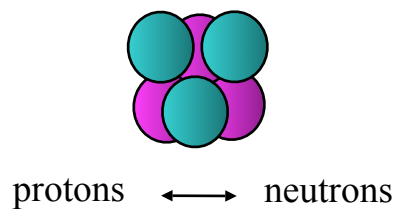


Nuclear Reactions: photo-absorption

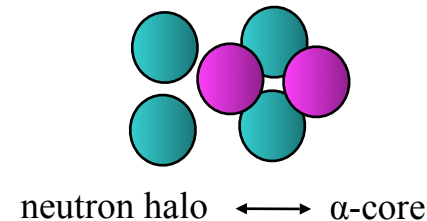
Semi-realistic NN force



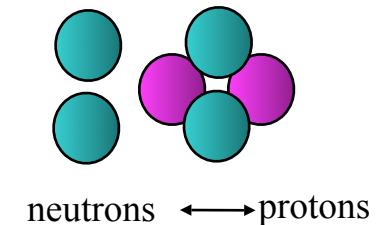
Giant Dipole Resonance



Soft-dipole Mode

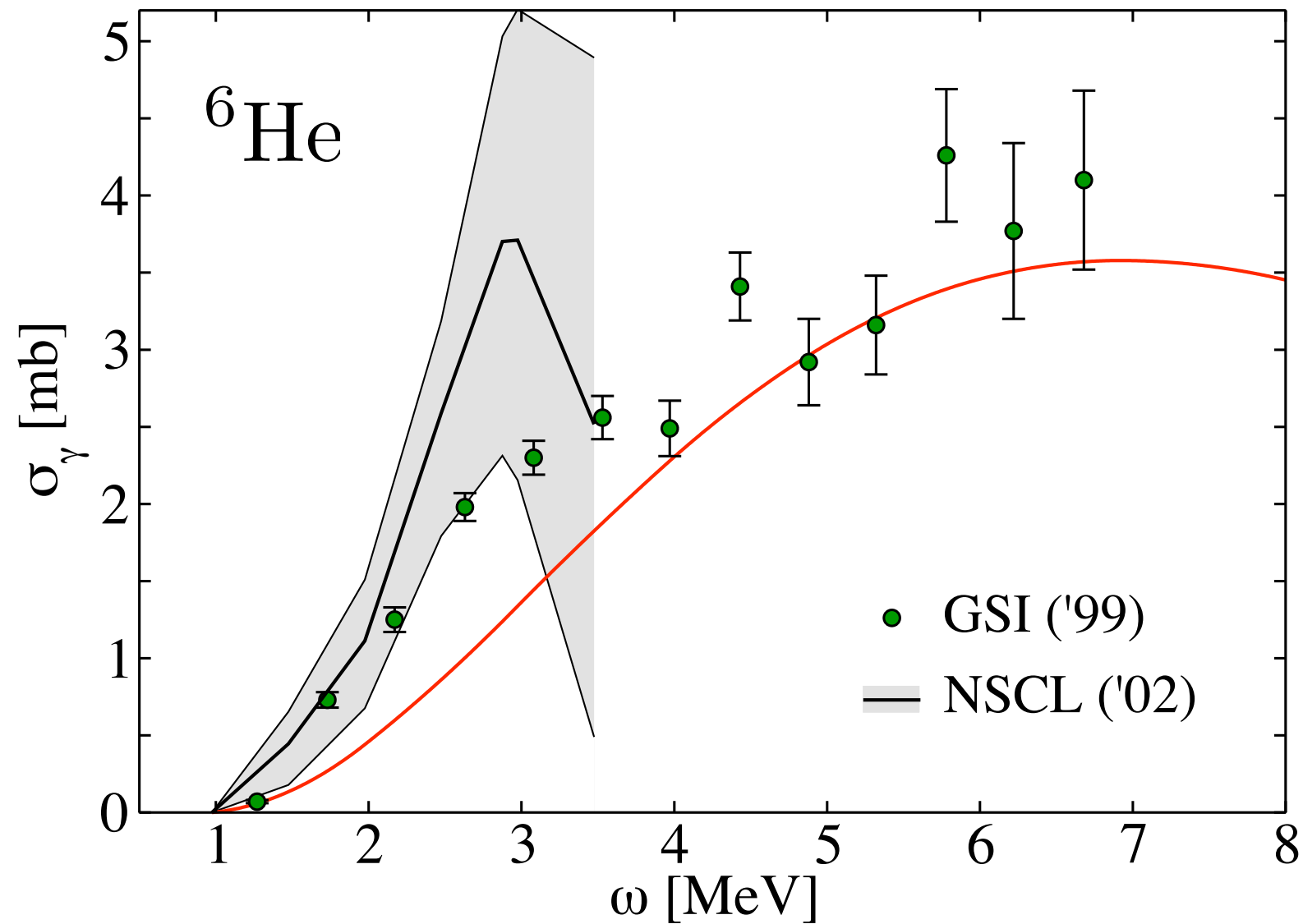
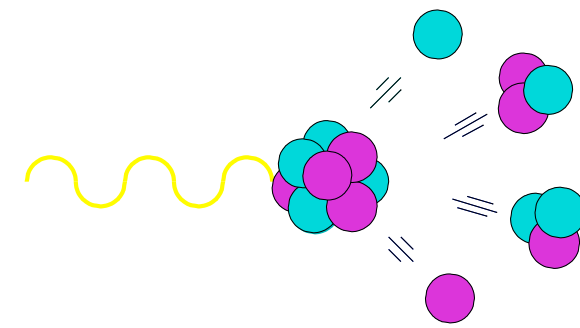


Giant Dipole Mode



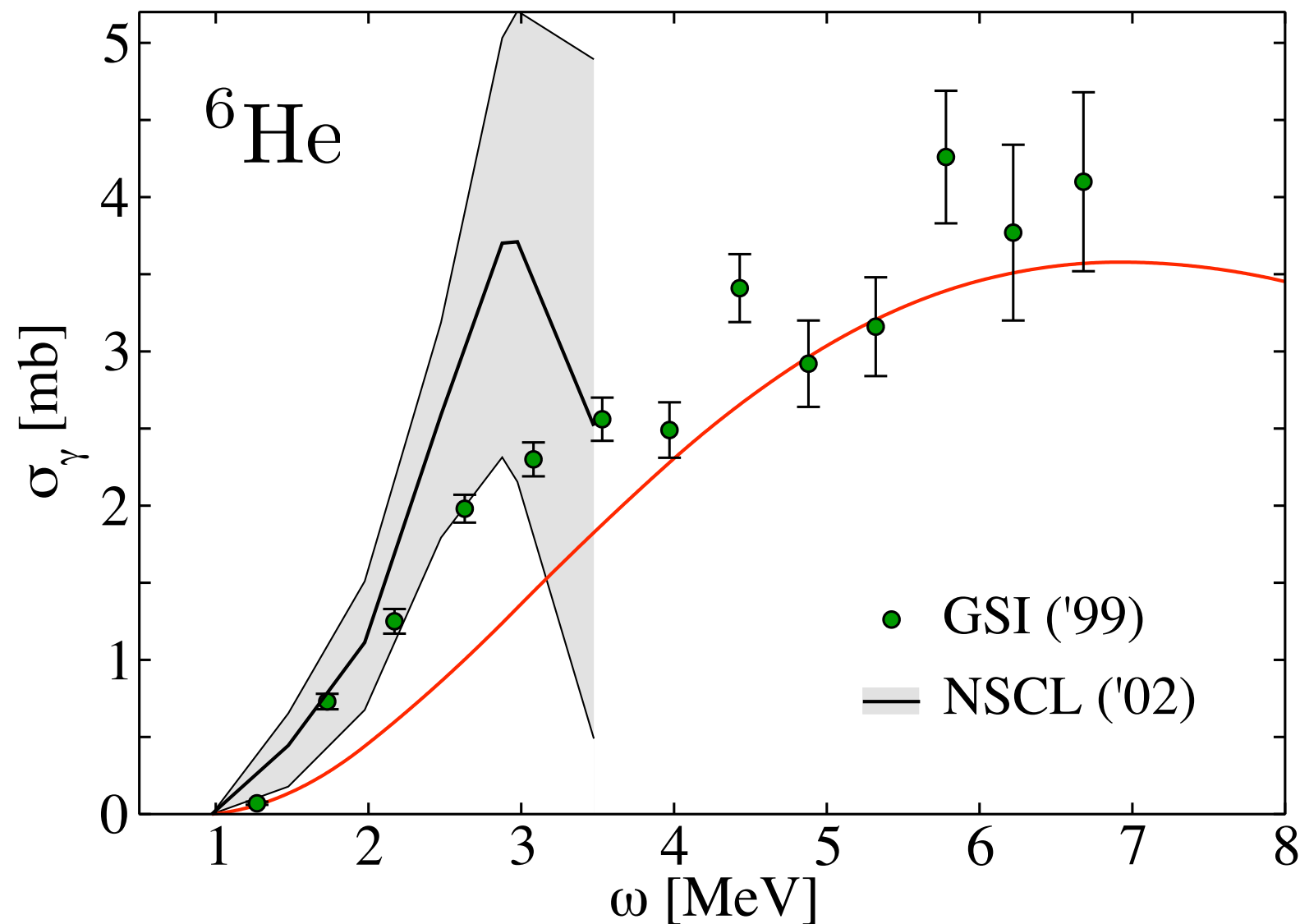
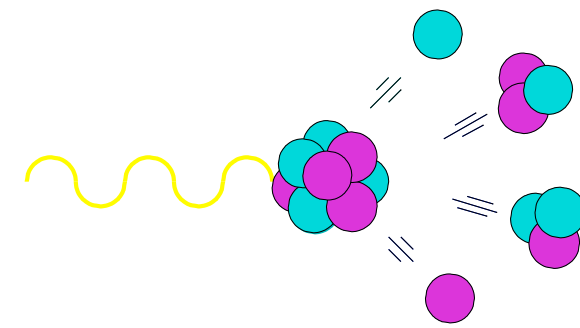
Nuclear Reactions: photo-absorption

Semi-realistic NN force



Nuclear Reactions: photo-absorption

Semi-realistic NN force



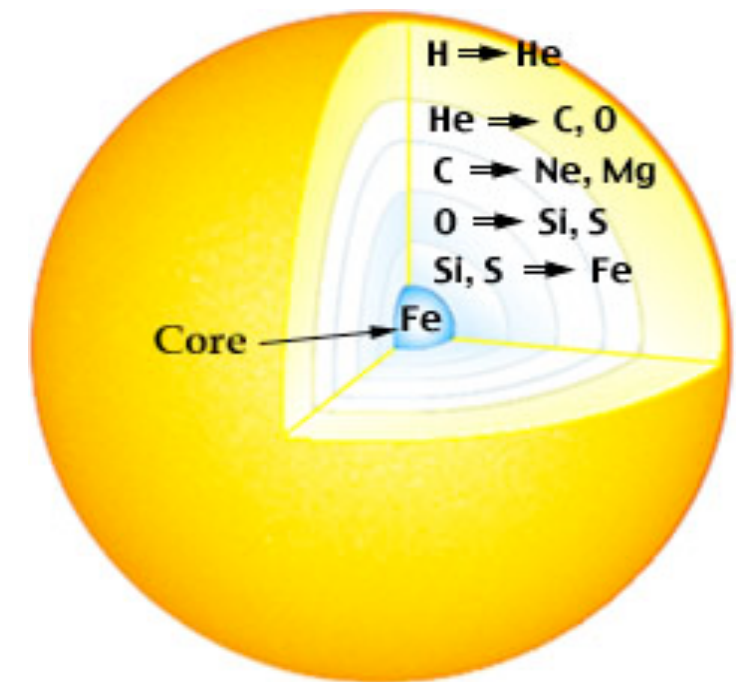
- Photo-absorption can be also related to neutron capture reactions for astrophysics

Astrophysics: Neutrino Reactions in Supernovae

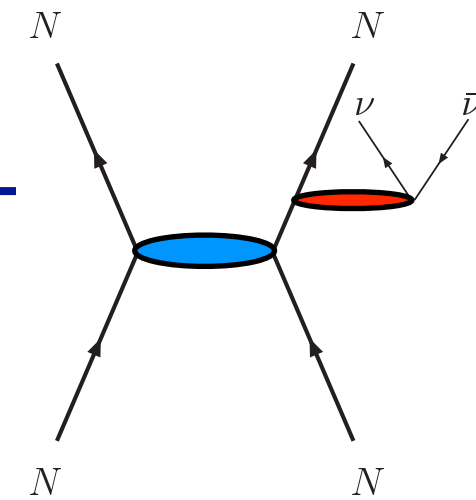


- Core collapse supernovae are gigantic explosions of massive stars
- 99% of the released energy is carried by neutrinos in all flavors, therefore
neutrino interactions with matter are crucial

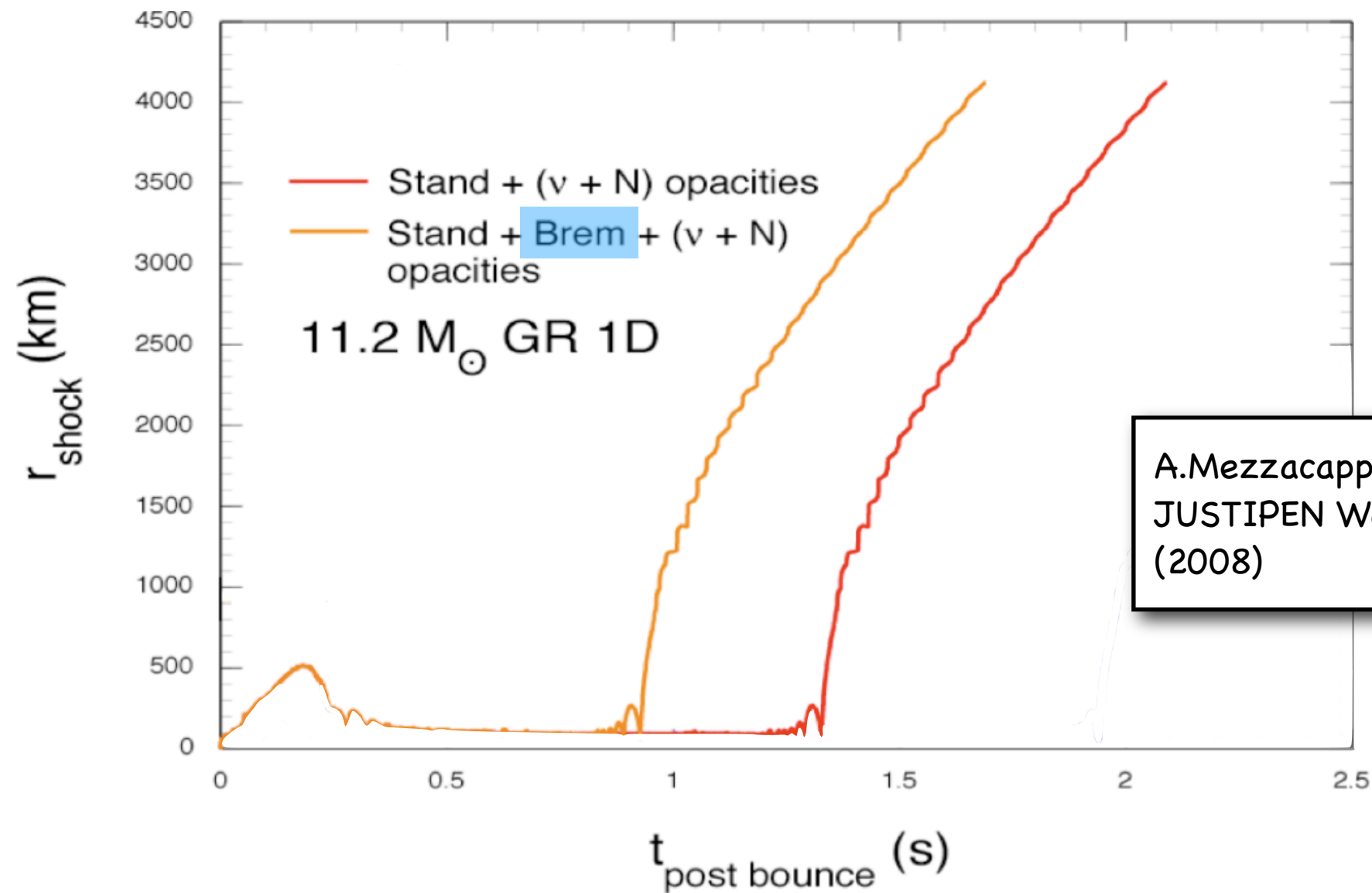
- In the iron core the burning process stops and it becomes gravitationally unstable \rightarrow the core collapses
- Nuclear forces halt the collapse, and drive an outgoing shock, which loses energy due to dissociation, neutrino radiation.
- The shock stalls ... possibly revived by neutrino heating



Neutrino bremsstrahlung reaction $NN \rightarrow NN\nu\bar{\nu}$



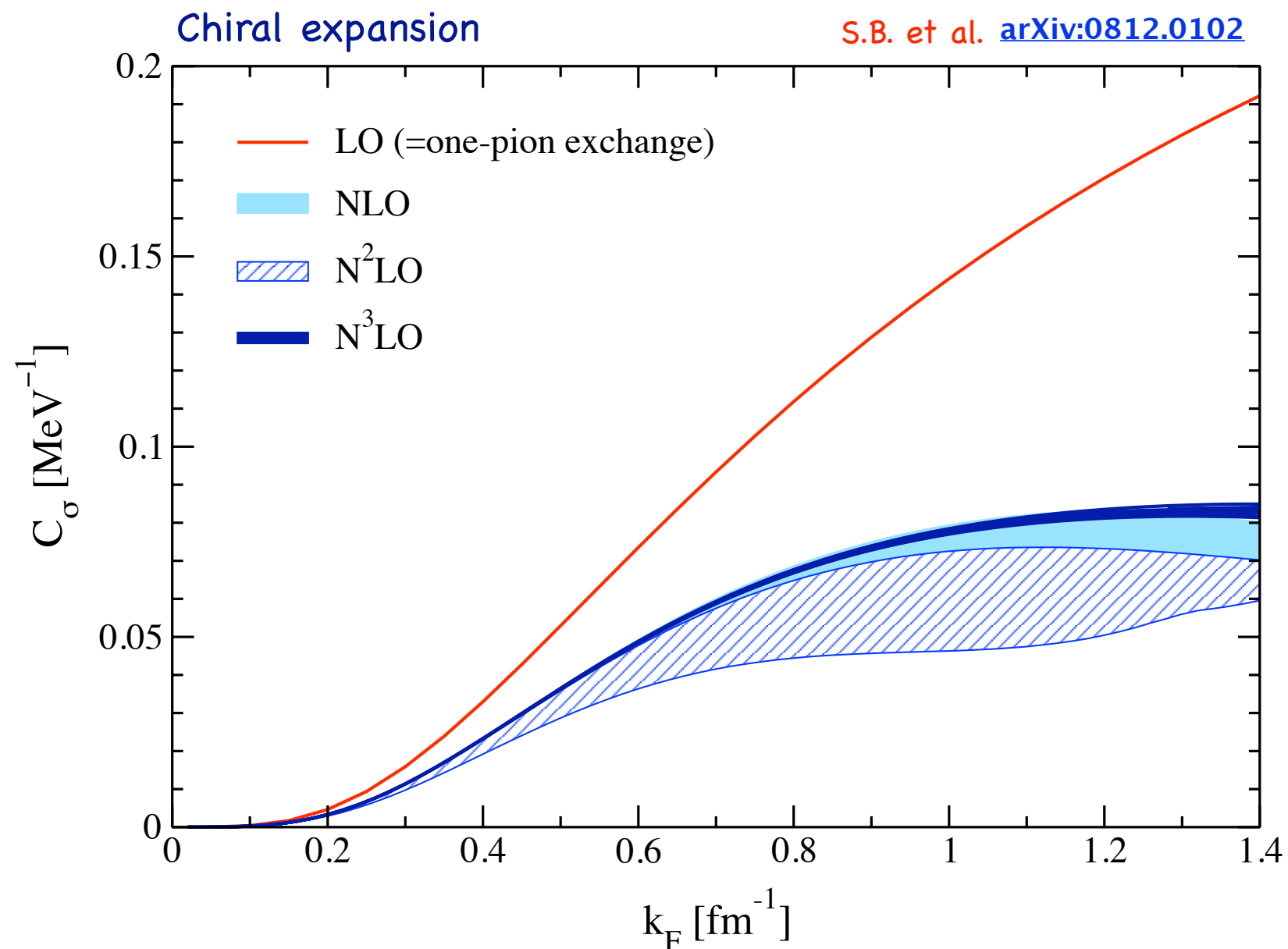
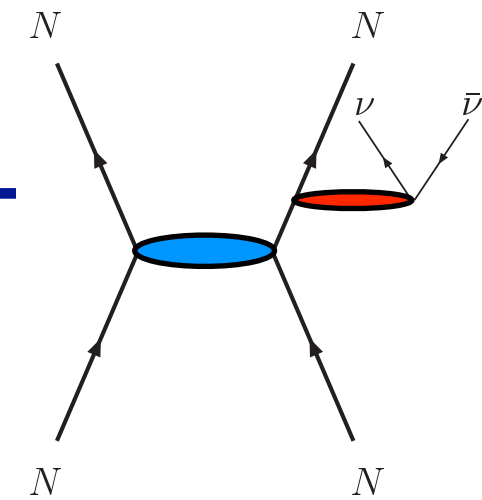
Neutrino bremsstrahlung affects the time scale
of the delayed explosion



but standard neutrino rates are based on one-pion-exchange for NN

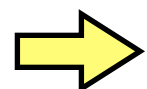
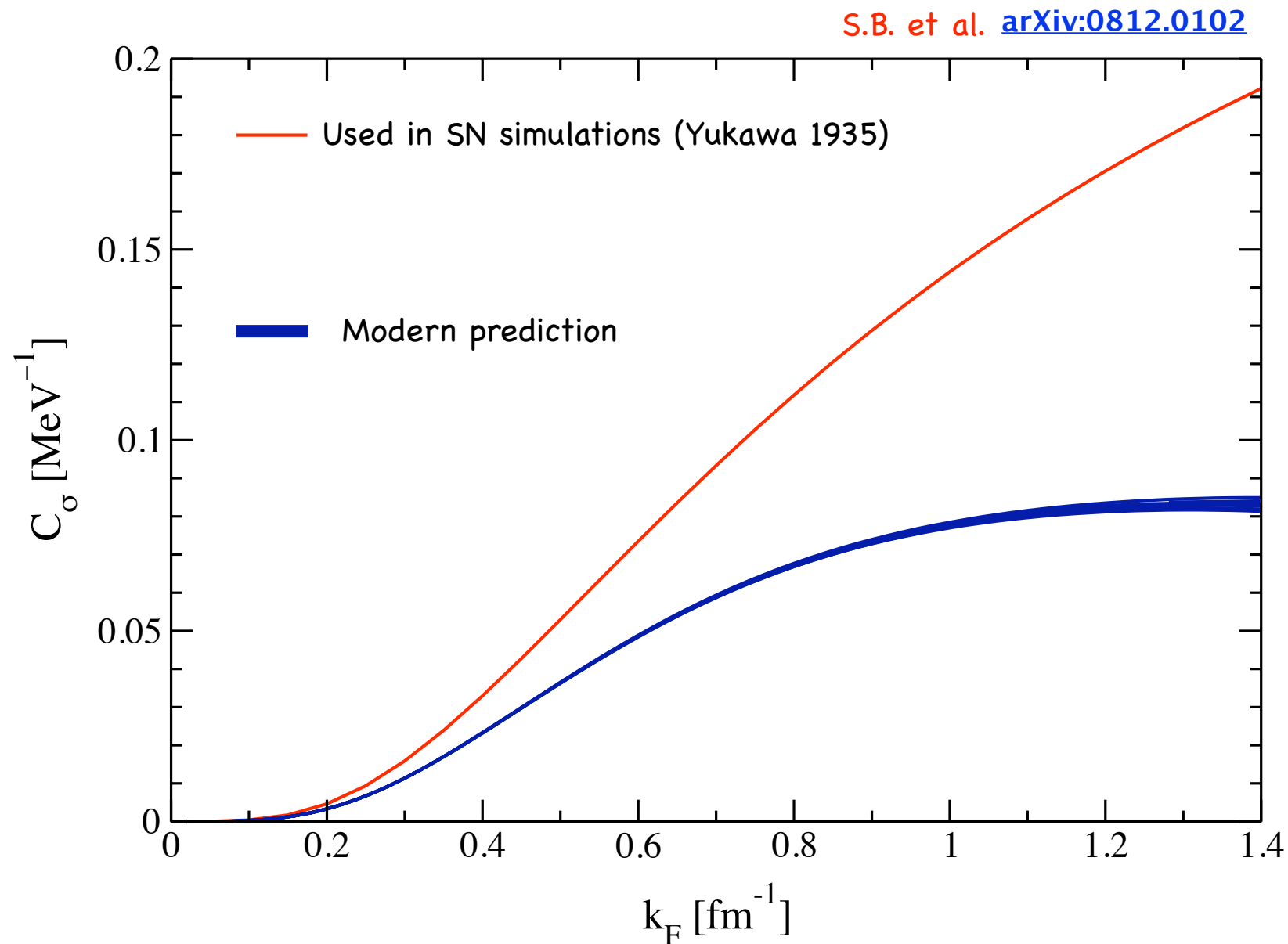
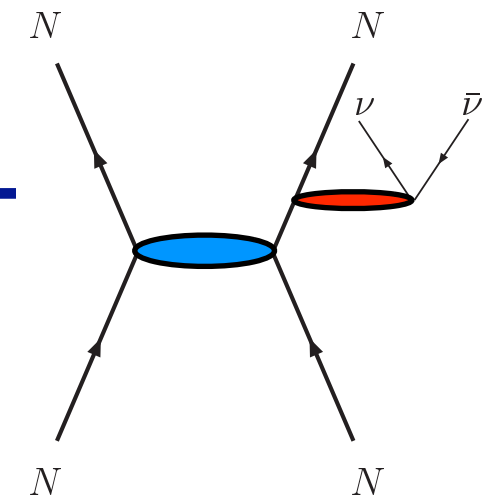
Neutrino bremsstrahlung from EFT

Pure neutron matter $NN \rightarrow NN\nu\bar{\nu}$



Neutrino bremsstrahlung from EFT

Pure neutron matter $NN \rightarrow NN\nu\bar{\nu}$

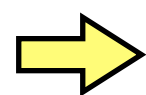
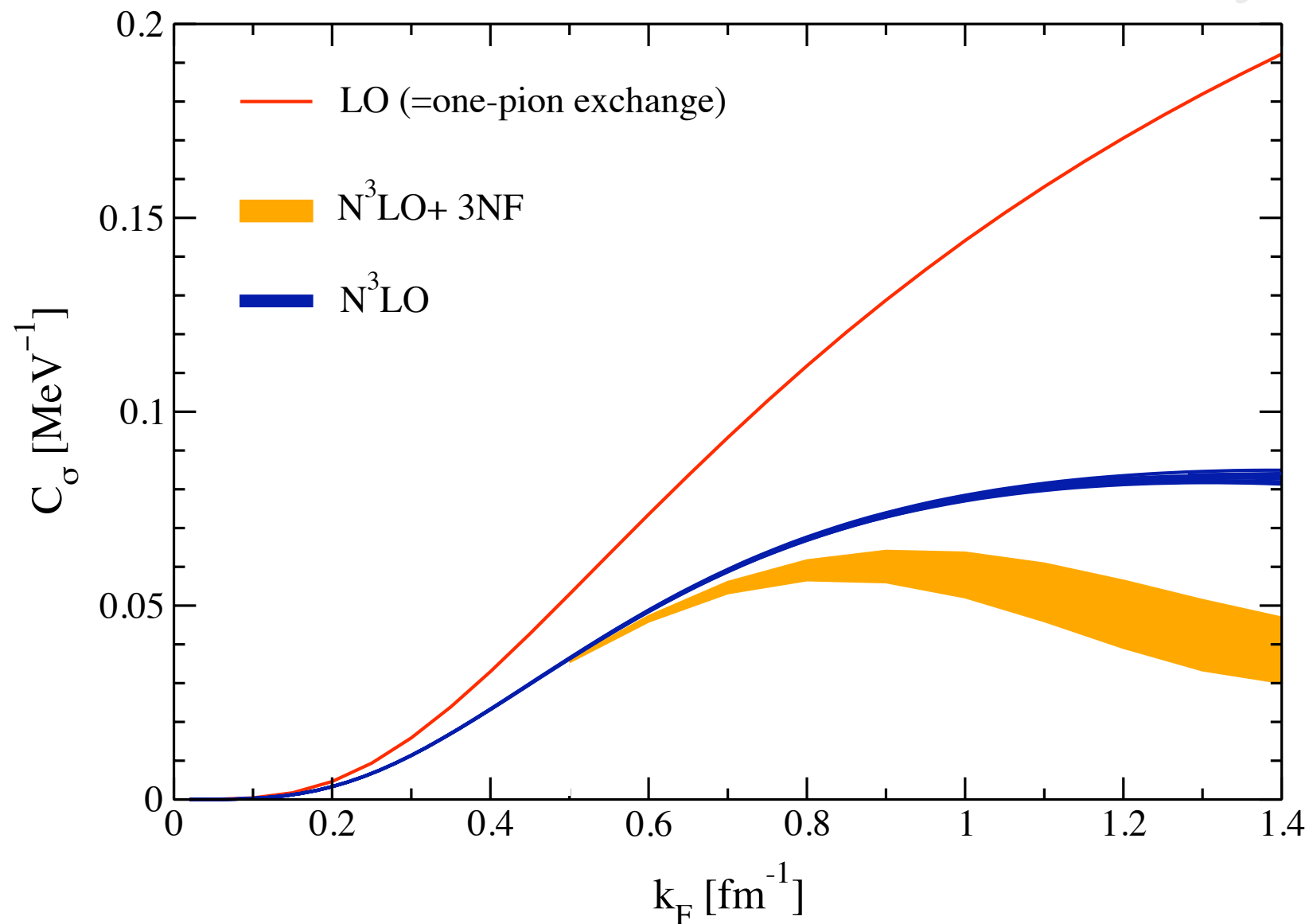


Modern Hamiltonians give a very different result!

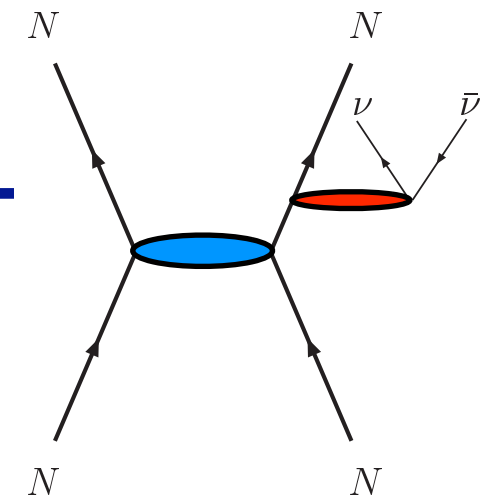
Neutrino bremsstrahlung from EFT

Pure neutron matter $NN \rightarrow NN\nu\bar{\nu}$

Preliminary

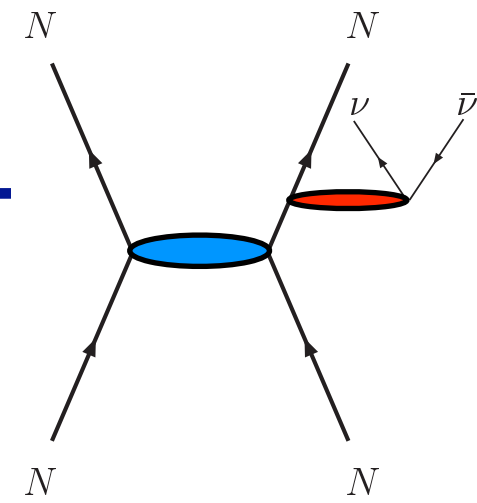


Visible effect of 3NF at higher density

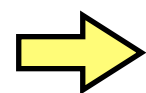
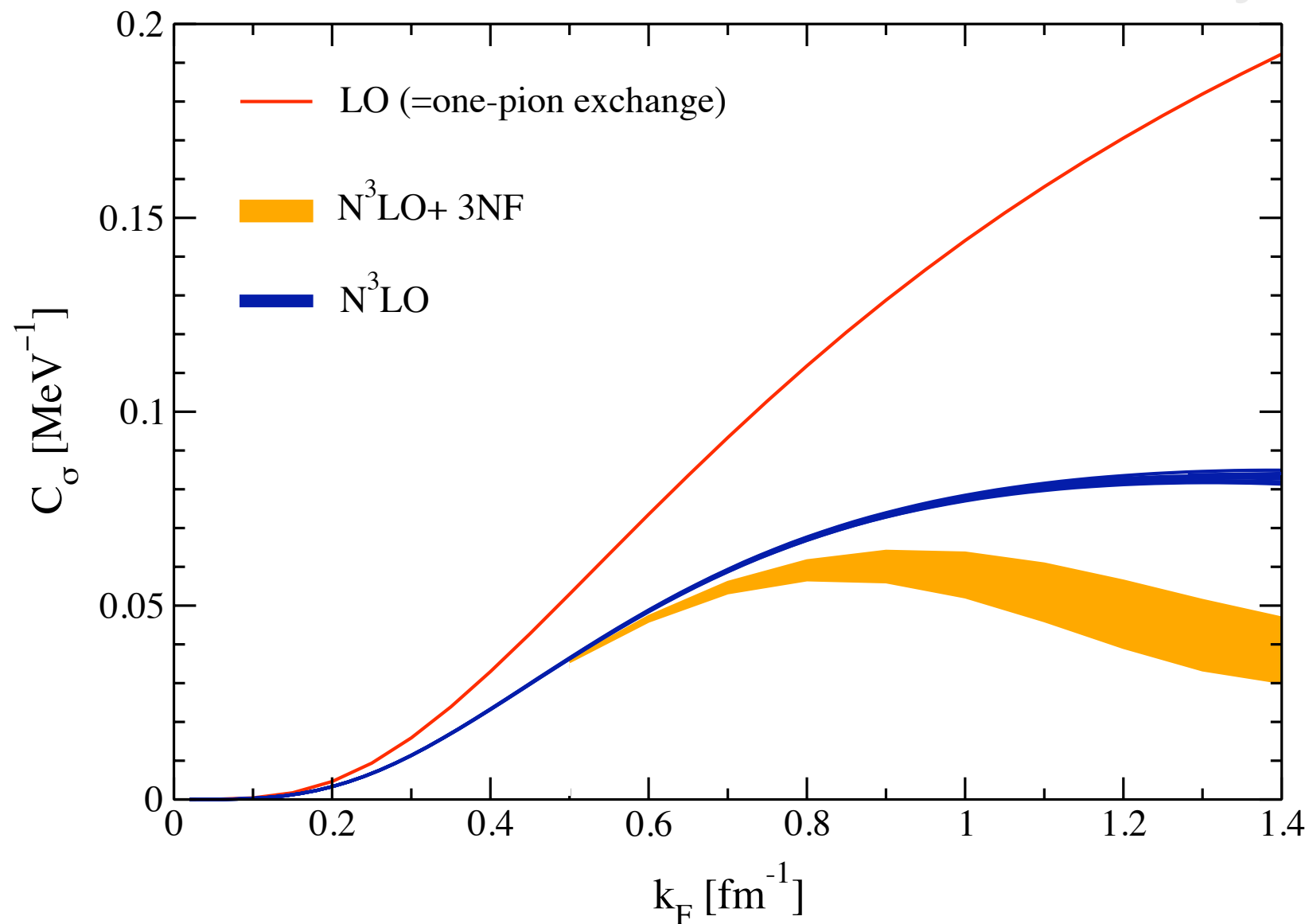


Neutrino bremsstrahlung from EFT

Pure neutron matter $NN \rightarrow NN\nu\bar{\nu}$



Preliminary



Visible effect of 3NF at higher density

Aim: the new standard rates in SN simulation!

Summary

Exciting era in nuclear physics with advances
on many fronts!

Nuclear physics is build upon a strong connection theory-experiment:
fundamental for testing our knowledge of nuclear forces

- Enormous progress done in ab-initio approaches to nuclear structure
 - ★ Description of helium halo isotopes from evolved Effective Field Theory forces
- Advances in the accurate calculation of nuclear reactions
 - ★ Different dipole strength distribution in stable-unstable light nuclei
- Nuclear physics provides fundamental microscopic input for astrophysics
 - ★ First neutrino rates based on Effective Field Theory

Future: the study of the role of 3NF is key in all areas
from light nuclei to astrophysics

Thanks to my collaborators:



האוניברסיטה העברית בירושלים
The Hebrew University of Jerusalem

Nir Barnea



Gaute Hagen, Thomas Papenbrock



ACADIA
UNIVERSITY Katy Hally



Kai Hebeler, Achim Schwenk



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Thank you!
Merci!