

Impact of Growth Characteristics on the Fracture Perpendicular to the Grain of Timber

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ABSTRACT: The natural material wood is commonly graded with regard to the parallel to the grain strength and stiffness properties and taking into account different growth characteristics such as knots and grain deviations. In this paper the impact of knots and grain deviations on the fracture perpendicular to the grain of timber is analysed by means of numerical models. The results are used for the calibration of an analytical model. With this model it is possible to evaluate the impact of growth characteristics on the perpendicular to the grain fracture and compare the results with test data from literature. The evaluation shows that certain growth characteristics increase the strength perpendicular to the grain. This is in contrast with current grading procedures, where such growth characteristics are considered as being strength decreasing. The results are compared with a model for the description of the effects of growth characteristics on the distribution characteristics of the strength perpendicular to the grain. This strongest link model can be used to describe phenomena with a parallel system of failure events.

1. INTRODUCTION

Although wood is a natural material exhibiting various inhomogeneities, fracture of wood is most often studied on small clear specimens and modeled neglecting these inhomogeneities. However, for the prediction of the structural behavior of full scale glulam members the influence of growth characteristics, like e.g. knots, grain deviations and cracks has to be accounted for.

The failure of boards loaded in tension parallel to grain is often initiated by local growth characteristics. For a safe and reliable use of timber in load-carrying structures it is necessary to grade timber according to certain criteria. These criteria are commonly chosen with respect to the bending (or tensile) strength of timber. For other strength

properties like tension perpendicular to the grain or shear no adequate grading criteria have been specified. However, it is well known that for tension perpendicular to grain the stressed volume has an important impact on the effective strength and that wood checks and other characteristics initiate failure. This effect is often described by means of the Weibull weakest link theory (Weibull, 1939).

Cracks in wood normally propagate parallel to the grain due to the low strength and fracture energy of wood perpendicular to the grain. In the vicinity of knots the wood fibers deviate from the global grain direction. This leads to an increase in effective resistance against crack growth. Therefore knots and grain deviations along the crack path can lead to an increase of the load-carrying capacity of

Table 1: Shear stresses at failure in the reduced cross-section of beams with variable notch height in 3-point bending, separated into samples with and without knots (Larsen and Riberholt, 1972)

α [-]	all		
	$\tau_{u,\text{mean}}$ (CoV) [N/mm ²] (%)	$\tau_{u,0.05}$ [N/mm ²]	$\tau_{u,0.10}$ [N/mm ²]
1	4.38 (3.1)	4.02	4.12
0.75	2.93 (29.6)	1.70	1.90
0.5	2.19 (26.5)	1.36	1.51
0.25	2.00 (38.0)	1.02	1.17
	with knots		
1	-	-	-
0.75	3.63 (30.6)	1.78	2.04
0.5	2.41 (20.9)	1.55	1.71
0.25	2.77 (31.6)	1.47	1.70
	without knots		
1	-	-	-
0.75	2.72 (24.1)	1.75	1.92
0.5	2.12 (27.9)	1.32	1.45
0.25	1.78 (31.8)	1.02	1.15

e.g. end-notched beams (Jockwer, 2014).

Early experimental research on the impact of knots on the fracture behaviour of timber is reported in (Larsen and Riberholt, 1972). 200 end-notched solid timber beams of the quality grade "ungraded" with varying height of the reduced cross-section $\alpha \cdot h$ were tested in 3-point bending. Fracture of the notch corner was the failure mode in the tests and the results are summarized in Tab. 1. The failure load of the notched beams with knots was found to be higher both on mean and 5th- and 10th-percentile levels.

Riberholt et al. (1991) tested a large series of end-notched beams in order to study the influence of various geometrical parameters on the load-carrying capacity. A crack retarding effect of knots was observed and specimens with knots showed higher load-carrying capacities. In addition to full-size specimens also tests on small clear specimens were carried out. One specimen contained a knot along the crack surface and showed a considerable higher fracture energy.

Similar impacts of knots on the load-carrying behavior of end-notched beams were detected in the tests reported in (Möhler and Mistler, 1978). A reduction of load-carrying capacity was observed for

beams with checks along the crack path.

Jockwer (2014) analyzed impacts on the variation of load-carrying capacity of end-notched beams. In this study it was shown that the large variation of load-carrying capacities can not be explained only by the variation of the elastic material properties and fracture energy in mode I (opening mode). The additional variation in the test results can be represented by including a model uncertainty with a considerably high coefficient of variation $CoV \approx 23\%$. The variation of this model uncertainty can be justified by the presence of knots along the crack path. In (Jockwer, 2014) it is described how the crack retarding effect of knots was studied in tests by means of optical measurement systems.

This paper aims at investigating and quantifying the impact of different growth characteristics on the fracture behaviour of timber. In numerical models the impact of the shape of the crack path is analysed. Analytical models are used to study the impact of varying fracture energy along the crack path. The results of these studies are used to evaluate the distribution characteristics of the load-carrying capacity of specimens loaded (locally) in tension perpendicular to the grain.

2. GRADING OF TIMBER AND MATERIAL PROPERTIES

2.1. Growth characteristics

The mechanical properties of solid timber mainly depend on the physical and structural characteristics of wood (Forest Products Laboratory, 2010). Key physical parameters are the wood density and the moisture content (MC). In sound, non-decayed wood, the structural characteristics with the highest impact on the fracture behavior and the mechanical properties are:

- Amount and size of knots and knot clusters
- Cross grain
- Orientation and width of the annual rings (the latter as a visible indicator for the density)
- Presence / absence / distance from pith (as a result of the cutting pattern).

Table 2: Distribution parameters of material properties being of relevance for the fracture of glulam equivalent to strength class GL24h at MC = 12% according to EN 338 (2009), JCSS (2001) and Jockwer (2014)

Parameter	Unit	Symbol	Mean	5 th perc.	CoV	PDF
MOE to the grain	[N/mm ²]	$E_{0,\text{mean}}$	11'500	9'600	13 %	lognormal
MOE ⊥ to the grain	[N/mm ²]	$E_{90,\text{mean}}$	300	250	13 %	lognormal
Shear modulus	[N/mm ²]	$G_{v,\text{mean}}$	650	540	13 %	lognormal
Fracture energy Mode 1 (clear wood)	[N/mm]	$G_{f,I,\text{mean}}$	0.3	0.218	20 %	lognormal
Fracture energy Mode 2 (clear wood)	[N/mm]	$G_{f,II,\text{mean}}$	1.15	0.695	30 %	lognormal

In order to reach the intended mechanical properties of glued-laminated products the raw material has to be strength graded. Selected mechanical properties of the resulting glulam of the strength class GL24h common in Europe are summarized in Tab. 2 (EN 14080 (2013); JCSS (2001)).

2.2. Knot clusters and clear wood sections

The natural structure of the spruce wood makes a distinction between clear wood and knot sections possible. Fink et al. (2013) used a constant length of the knot sections of 150 mm for the description of the structure of the boards although the length of the knot sections in reality is varying. It is suggested by (Fink et al., 2013) to model the clear wood section as being Gamma-distributed with an expected length of $d_{\text{mean}} = 530$ mm and a standard deviation of $\sigma = 250$ mm.

2.3. Cross grain

In a previous investigation reported in (Oscarsson et al., 2014) 450 glulam laminations were scanned for surface fibre directions. Here, the same data set was used to quantify the cross grain. The median of the nominal grain direction on the edges of the laminations (for all laminations) was used as a measure in order not to have the data corrupted by the local grain deviation close to knots. A median deviation from perfectly aligned grain in the range of up to 2 degrees was found to be quite common and the extreme 10% fractile values of the median included deviations of approximately 4-6 degrees.

2.4. Fracture related material parameters

The fracture energy of mode 1 is commonly determined by testing single edge notched beam (SENB) specimens as specified in a Draft Standard of CIB-W18 by Larsen and Gustafsson (1990), also known

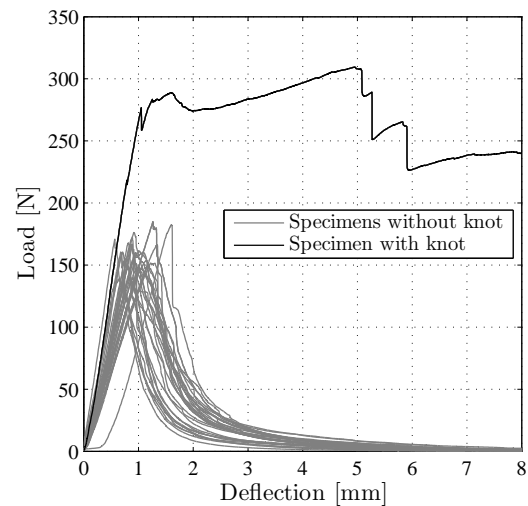


Figure 1: Force-displacement behaviour of a SENB specimen without and with knots (Jockwer, 2014).

as the Nordtest method (Nordtest, 1993). Parameters for PDFs fitted to the fracture energy values of individual data are summarised in Tab. 2. The correlation between density and $G_{f,I}$ is low for the observed range of densities being of relevance for structural applications. No general trend of the fracture energy with regard to the spatial distribution in grain direction can be found. However, there is a considerable impact of the presence of knots in the fracture plane as can be seen in Fig. 1. This impact can be explained by the resulting larger fracture surface due to grain deviations and the doweling effect of the knot interfering the separation of the specimen and allowing further load transfer along the fracture plane. Such extended studies do not exist for the mode 2 fracture energy $G_{f,II}$. However, a similar impact of growth characteristics can be assumed.

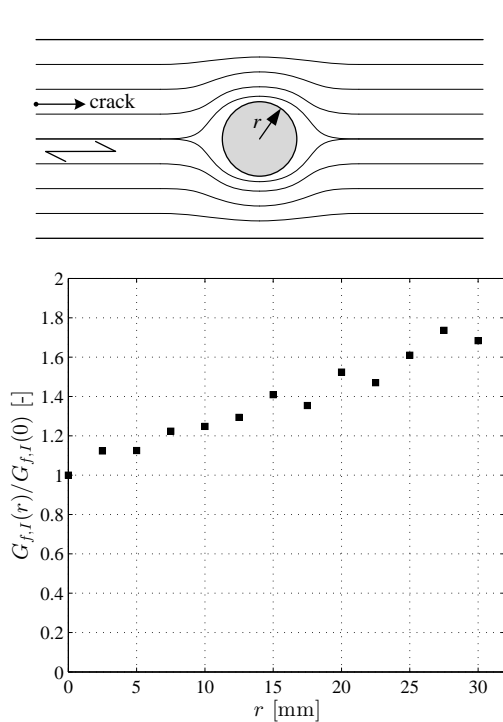


Figure 2: Grain deviation in the region of a knot and impact of the amplitude of grain deviation on the fracture energy $G_{f,I}$.

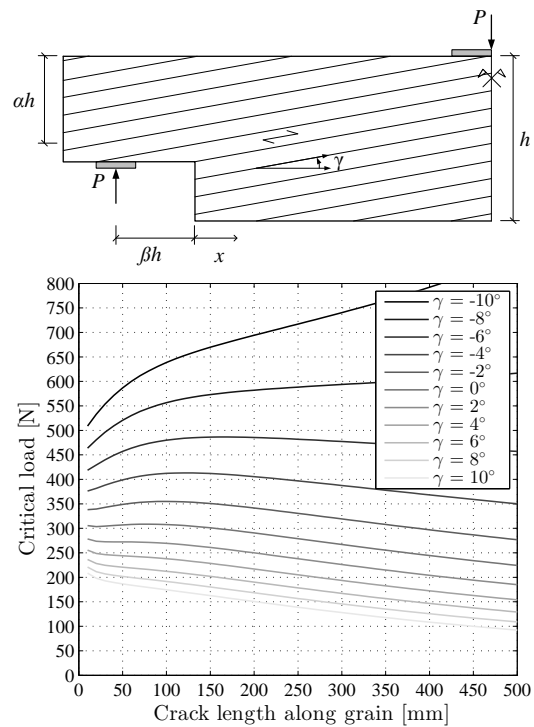


Figure 3: Model of a beam with cross grain and development of the critical load causing crack propagation.

3. IMPACT OF GROWTH CHARACTERISTICS ON THE FRACTURE OF WOOD

The impact of knots and grain deviations and of cross grain on the fracture energy of a SENB and the crack propagation load of a notched beam, respectively, is analyzed by means of numerical models.

3.1. Impact of grain deviations

There are various impacts of knots on the fracture behaviour of timber. One of them is the deviation of grain direction in the vicinity of knots which leads to an increase of the fracture surface. In Fig. 2 an example of the deviation of the crack is illustrated as it might occur in the vicinity of a knot. The impact of the deviation on the load-deflection behaviour can be analysed using SENB specimens. The numerical study was performed by means of the software ABAQUS applying enriched element (xFEM) as described in (Qiu et al., 2014). The results of the study are summarized in Fig. 2: The increase in fracture energy depends on the size and slope of the grain deviation.

An additional impact of knots on the fracture energy is caused by their reinforcing effect on the crack. The reinforcing effect can be assumed to depend on the knot size within one knot cluster. In tests on SENB which included knots in the crack plane a relative increase of up to factor 10 can be observed (Fig. 1).

3.2. Impact of cross grain

The global grain direction of glulam beams is commonly oriented parallel to the beam axis. Hence, a crack will develop along the beam axis, leading to a separation of the notched beam in an upper and a lower part.

In case of an inclination of the grain direction, not only the directions of the orthotropic material properties are different but also the remaining cross-section of the lower and the upper beam change during crack growth.

In Fig. 3 an example of a global inclination of the grain direction of a notched beam by $\gamma = 10^\circ$ is illustrated. The numerical study was performed by means of a MATLAB based FE model using the compliance method for the calculation of energy re-

lease rate and crack propagation load. The ultimate load and also the failure behavior changes considerably already for small inclinations in the order of $\pm 10^\circ$ as shown in Fig. 3.

4. LOAD-CARRYING CAPACITY OF A NOTCHED BEAM

4.1. Notched beam model

Gustafsson (1988) proposed an analytical model for the estimation of the load-carrying capacity of end-notched beams. The strength equation is set up by balancing energies during crack growth initiated in an end-notched beam. The energy release rate is calculated by derivation of beam deflection as a function of crack length. The analysis delivers the load-carrying capacity at a given notch length βh .

Growth characteristics along the crack path can be accounted for in the model by assigning variations of the values of fracture energy to the respective position along the crack path $\beta h + x$. The notched beam shows a brittle failure behavior due to the strong decrease of the crack propagation load with increasing crack length. This leads to a diminishing impact of the variations of fracture energy on the load-carrying capacity with increasing crack length.

Additional lamellas can be inserted in the model in order to simulate the interaction between these lamellas and in order to model weakest link effects during failure of a glulam beam.

4.2. Monte Carlo simulations

Monte Carlo simulations were performed using the material properties as listed in Tab. 2. Within the clear wood sections the fracture energy was modeled as lognormally distributed with $G_{f,mean} = 0.3 \text{ N/mm}$ and $CoV = 20\%$. The variations in stiffness and fracture energy in the clear wood only led to a minor variation of the load-carrying capacities (dash-dotted line "Reference Model" in Fig. 4). Hence, the model has to account for additional variations caused by knots and growth characteristics along the crack path.

For that reason the crack path was divided into different segments representing the clear wood and knot sections. The length and distribution of these sections was chosen in a first estimate as explained

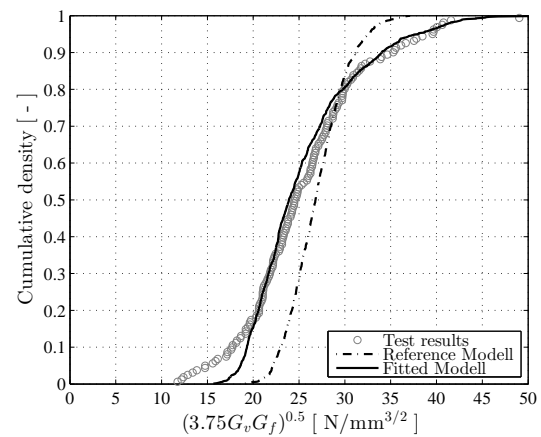


Figure 4: Comparison of the cumulative density distribution of test results with the models accounting for different growth characteristics.

in Section 2.2. Within the knot sections the doweling effect of the knot or the curving of the crack path due to grain deviation was modelled by varying the fracture energy.

The impact of the knot sections on the load-carrying capacity, expressed by the fracture mechanics strength parameter $(3.75G_v G_f)^{0.5}$, is illustrated in Fig. 4 and can be described as follows:

- **Distance between knot sections:** The distance between the knot sections has a strong impact on the distribution of load-carrying capacities. For smaller distances the mean value of the load-carrying capacity increases. The variation of the distances between knot sections has only a minor impact on the distribution of load-carrying capacities.
- **Disturbance of the crack path:** Within knot sections the effective fracture energy is higher compared to clear wood sections due to grain deviations and the reinforcing effect of the knots. A knot factor F_{knot} is introduced to describe the relative increase of fracture energy in the knot section. This factor has a strong impact on the load-carrying capacity. The best fit between the analytical model and test results from literature (Jockwer, 2014) is achieved for $F_{knot,mean} = 2.0$ with $CoV = 40\%$.

The fitted analytical model as illustrated in Fig. 4 gives best agreement with the test results when

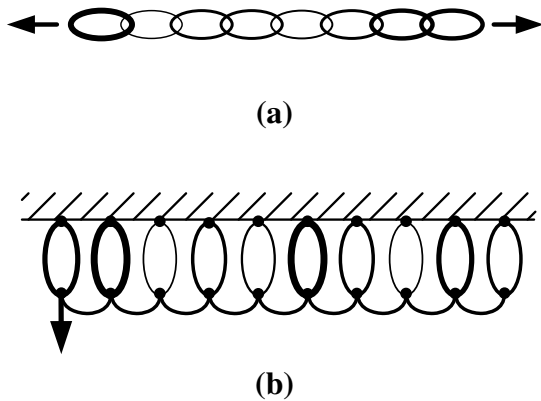


Figure 5: Illustration of the weakest link model (a) and of the strongest link model (b).

reducing the load-carrying capacity to 80% of the reference values. This reduction is in line with the studies by e.g. Franke (2008) and Jockwer (2014). The general trend is, that the presence of knot sections leads to an increase of the load-carrying capacity of notched beams. This effect is in contrast to the current procedures where only the weakening effect of the knot sections on the bending strength is accounted for.

5. STRONGEST LINK MODEL

5.1. Background

As discussed in Section 2 it is difficult to specify grading criteria to guarantee for strength properties other than bending and tension parallel to the grain, like e.g. tensile strength perpendicular to grain and shear strength. For tension perpendicular to grain it is, however, well known that the size of the stressed volume is important and also that failure often is initiated at checks and growth characteristics. The more or less random distribution and the number and size of these weak spots causes the volume effect. The probability of failure in tension perpendicular to grain of wood is often described using the 2-parameter Weibull distribution (Weibull, 1939):

$$p_f(\sigma) = P(R < \sigma) = 1 - e^{-\left(\frac{\sigma}{f_c}\right)^m} \quad (1)$$

where σ is the stress in a unit volume of the material and f_c and m are material parameters which define magnitude and scatter in strength. This distribution together with the Weibull weakest link theory gives

the strength distribution as a serial system of failure events like e.g. a linear chain containing n unit volumes (Fig. 5a) as

$$p_f(\sigma) = 1 - e^{-n\left(\frac{\sigma}{f_c}\right)^m} \quad (2)$$

A very convenient feature of this extreme value distribution is that its *CoV* equals the one of the unit volume strength distribution. A simple generalization of Eq. 2 makes it applicable to arbitrary volumes of material in which the stress may be non-homogenous, but still required to be finite.

The Weibull weakest link theory is, however, not applicable to structural elements with notches, cracks or other shaping that reveals a stress singularity since the theory for such situations in general predicts either zero strength or no crack propagation, no matter the magnitude of load (Gustafsson and Enquist, 1988). For end-notched beams the Weibull weakest link theory is contradicted by test results (Larsen and Riberholt, 1972) as discussed in Section 1. The higher strength observed may instead be described by a strongest link concept.

5.2. Strongest link model

A strongest link model with a sequential system of failure events is proposed in (Gustafsson, 2014) and can be illustrated e.g. by the resistance that a zipper gives towards being opened as illustrated in Fig. 5(b): the zipper link providing the highest resistance is decisive. Such a model can be applied in cases where global failure is governed by crack propagation along a crack path of certain length, and more generally where failure of two or more structural elements, or points, precedes global structural failure. If, e.g., the strength distribution of a single link can be described by Eq. 1, then the strongest link strength distribution of a zipper with n links is

$$p_f(\sigma) = \left(1 - e^{-\left(\frac{\sigma}{f_c}\right)^m}\right)^n \quad (3)$$

The strongest link model results for more links in a higher strength and in a smaller *CoV*. Moreover, for heterogeneous materials with a given mean link or material strength, an increased structural strength is predicted.

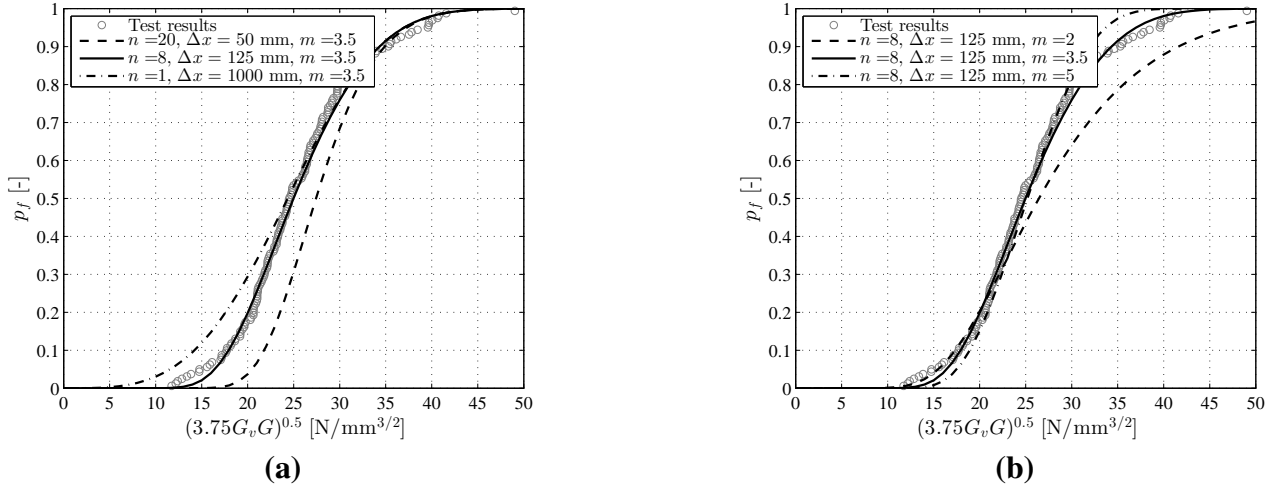


Figure 6: Comparison of test results on notched beams (Jockwer, 2014) and numerical predictions applying the strongest link model in Eq. 5 with (a) variation of n number of links, each link representing the crack propagation length Δx , and with (b) variation of the model parameter m .

In crack propagation analysis the link strength f_c can be interpreted as the fracture toughness K_c of the material determined experimentally for constant stress intensity, K , for a crack propagation of length Δx . The parameter m is then a measure of the scatter in K_c . σ in the ratio σ/f_c represents the stress intensity K . From conventional fracture mechanics analysis the function $K = K(P, x)$ can be determined, P being the external load and x the length of the crack. If K is constant along the crack path then:

$$p_f(P) = \left(1 - e^{-\left(\frac{PK_1}{K_c}\right)^m}\right)^n \quad (4)$$

K_1 represents the value of K when $P = 1$. The application of Eq. 4 to strength analysis of end-notched beams can be done by representing the fracture toughness and the stress intensity in terms of the critical energy release rate G_c and the energy release rate G , respectively, i.e. $K_c = (G_v G_c)^{0.5}$ and $PK_1 = (G_v G)^{0.5}$. If G varies along the crack propagation length L , then

$$p_f(P) = \prod_{i=1}^n \left(1 - e^{-\left(\sqrt{\frac{G(P, x_i)}{G_c}}\right)^m}\right) \quad (5)$$

where $n = L/\Delta x$ and $x_i = (i - 0.5)\Delta x$, with Δx being the reference length for the material parameters G_c and m .

5.3. Discussion

The application of the strongest link model (Eq. 5) and the comparison with test data from literature (Jockwer, 2014) is shown in Fig. 6. The material properties in Tab. 2 were used with $G_c = G_{f,I}$ and a total crack length $L = 1000$ mm. A good fit of the model with the test data is achieved for $m = 3.5$ and $n = 8$ links. This corresponds to a crack propagation length of each link of $\Delta x = 125$ mm. For an increasing number of links n at a constant total crack length L both 5th- and 50th-percentile values increase (Fig. 6 (a)). The 95th-percentile values are affected only marginally by n and Δx . In contrast, the model parameter m has a major impact on the upper tail. With an increase of m the variability of the results and the 95th-percentile values decrease. The validity of Δx as a reference length for other fracture mechanic problems has to be evaluated more extensively.

6. SUMMARY

Growth characteristics have an important impact on the strength and stiffness properties of timber. In this paper their impact on the fracture perpendicular to grain of timber was studied by means of different models. Changes in fracture energy and crack propagation load due to growth characteristics were evaluated by means of numerical models. The results serve as reference for an analytical model in

which the crack path is separated into knot and clear wood sections. In this model the estimated strength of the notched beam increases with increased occurrence of knot sections. This statistical effect is described by a strongest link model representing a parallel system of failure events. The behavior of the strongest link model is discussed in a comparison with test data of notched beams and a good fit is found.

Further applications of the strongest link model to different situations of tension perpendicular to grain or shear fracture seem possible. Such applications could be e.g. the tension perpendicular to grain strength of large curved or tapered glulam beams or the load-carrying capacity of connections loaded perpendicular to grain. In addition the model could help to explain the better fit of a height instead of a volume based size effect model with test data of tensile strength perpendicular to the grain discussed in Mistler (1998). However, for these further applications of the strongest link model additional calibration is necessary.

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