

Optimize Earthwork Hauling Plan with Minimum Cost Flow Network

Duanshun Li (duanshun@ualberta.ca)

Ming Lu (mlu6@ualberta.ca)

Outline

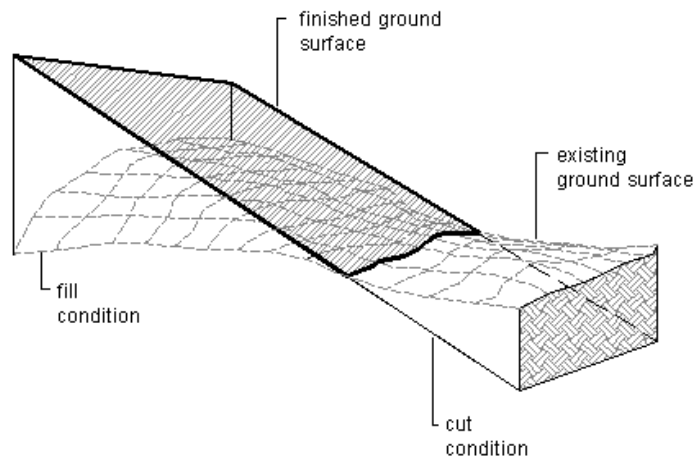
Background

Minimum
Cost Flow
Based
Method

Case Study
&
Validation

Conclusion

Background



Site grading design completed

- **Cut fill balance**
- **Quantity takeoff**

Major tasks in earthwork planning:

- **Material Earthwork Allocation**
- **Temporary haul road design**
- **Equipment Fleet optimization**

Background

Earthwork allocation:

Find the most economic combination of haul jobs to move the material from section to section

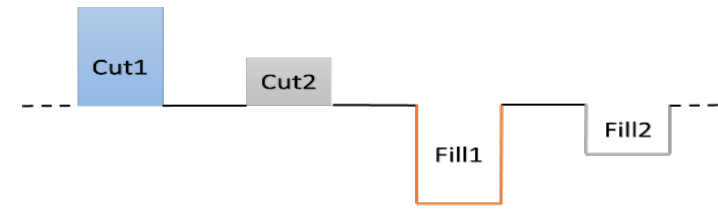
1	4	7	10	13	16	19	22
37133	14846	5013	1065	-7288	-9169	-2661	16089
2	5	8	11	14	17	20	23
24797	4497	-17920	-26853	-27369	-21327	-4500	11153
3	5	9	12	15	18	21	24
21111	3339	-4915	-8243	-8123	-8382	-3025	10732

Job	Cut	Fill	Volume (bcm)	Route
Job-A	20	19	8100	-
Job-B	20	18	16700	[19]
Job-C	21	18	5500	[20, 19,17]
Job-D	21	17	4400	[20, 19, 18]
Job-E	33	17	18600	[21, 20, 19, 18]
Job-F	33	16	36000	[21, 20, 19, 18, 17]
Job-G	33	15	8400	[21, 20, 19, 18, 17, 16]

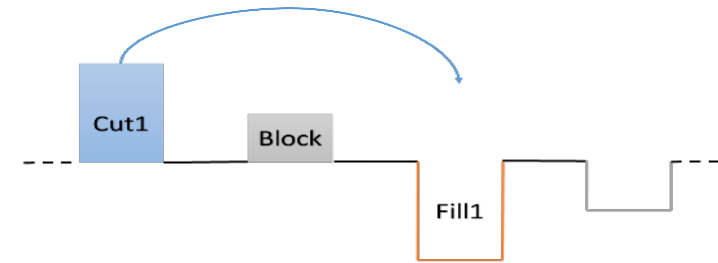
Problem

Limitations of earthwork allocation optimization by linear programming

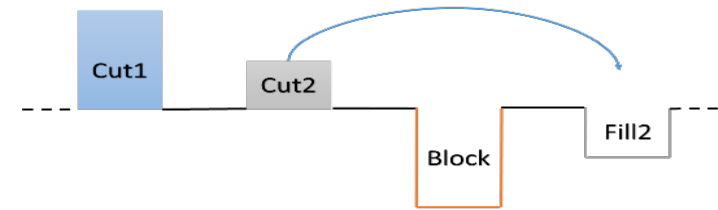
- 1) Time consuming to establish and solve equations
- 2) Generate Haul jobs with conflicts:
Hard blocks: Can be identified before hand, but cannot be eliminated.
Soft blocks: Embedded within haul jobs, can be eliminated.
- 3) Cannot provide job sequence



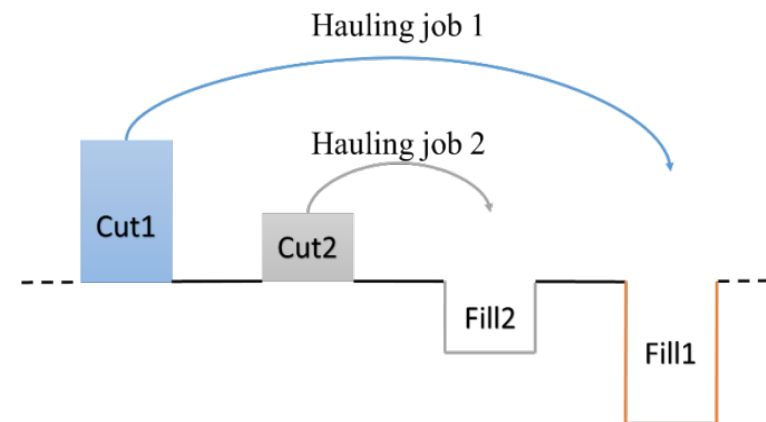
(a) Cut/fill layout



(b) Hauling job 1



(c) Hauling job 2



Simulation Methods

Construction Operations Simulation

Operation oriented: fleet selection

Limitations:

Simulation is separated from earth work allocation

- 1) User specify the route manually
(Hajjar and AbouRizk 1997, Marzouk, and Moselhi 2004)
- 2) Simulate with non-optimal heuristic approach
(Morley, Lu, and AbouRizk 2014)

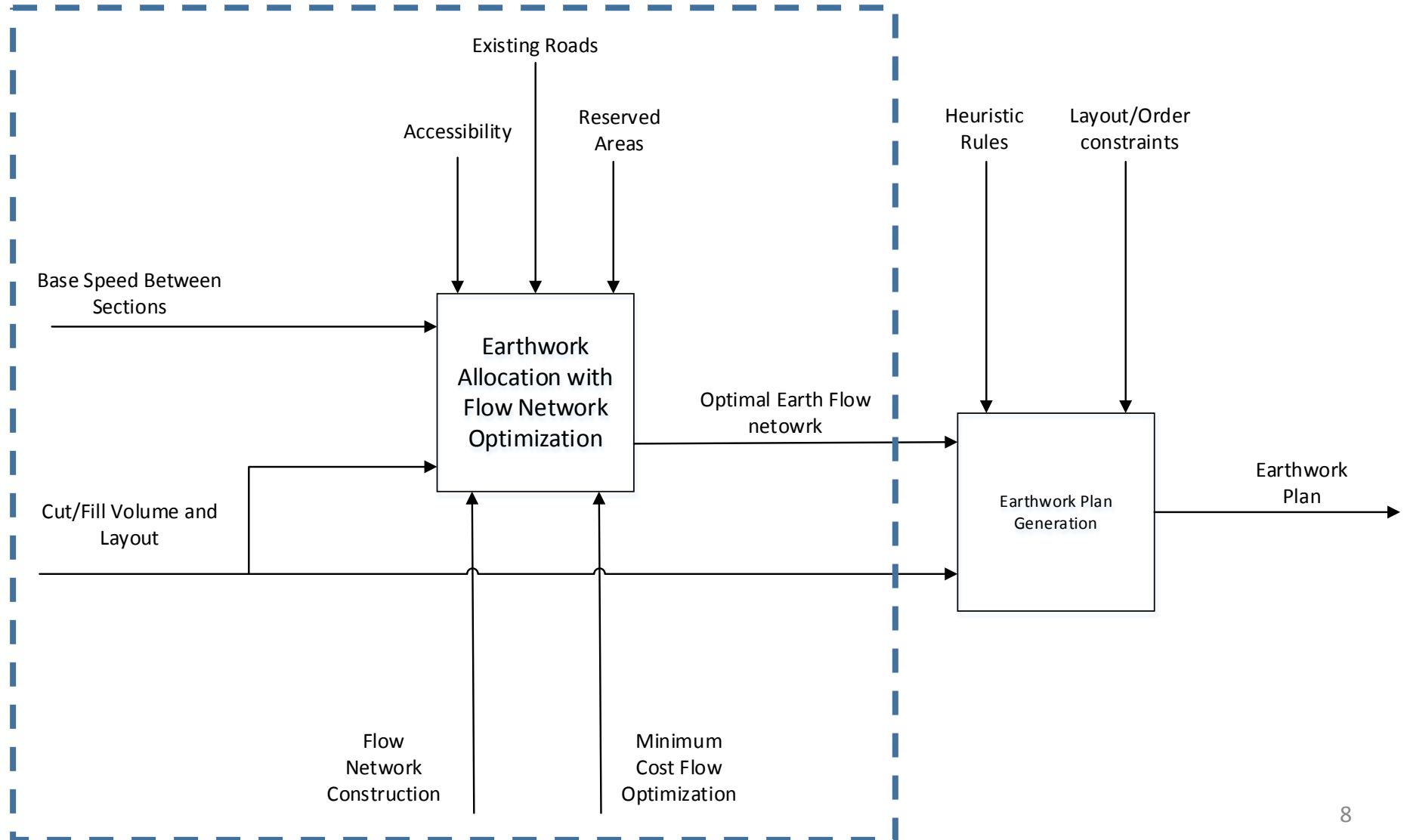
Minimum Cost Flow (MCF) Based Method

Research objective

- 1) Easy to use tool
- 2) Accommodate “hard blocks”
- 3) Avoid “soft blocks”
- 4) Integrate time (job sequence) into earthwork planning

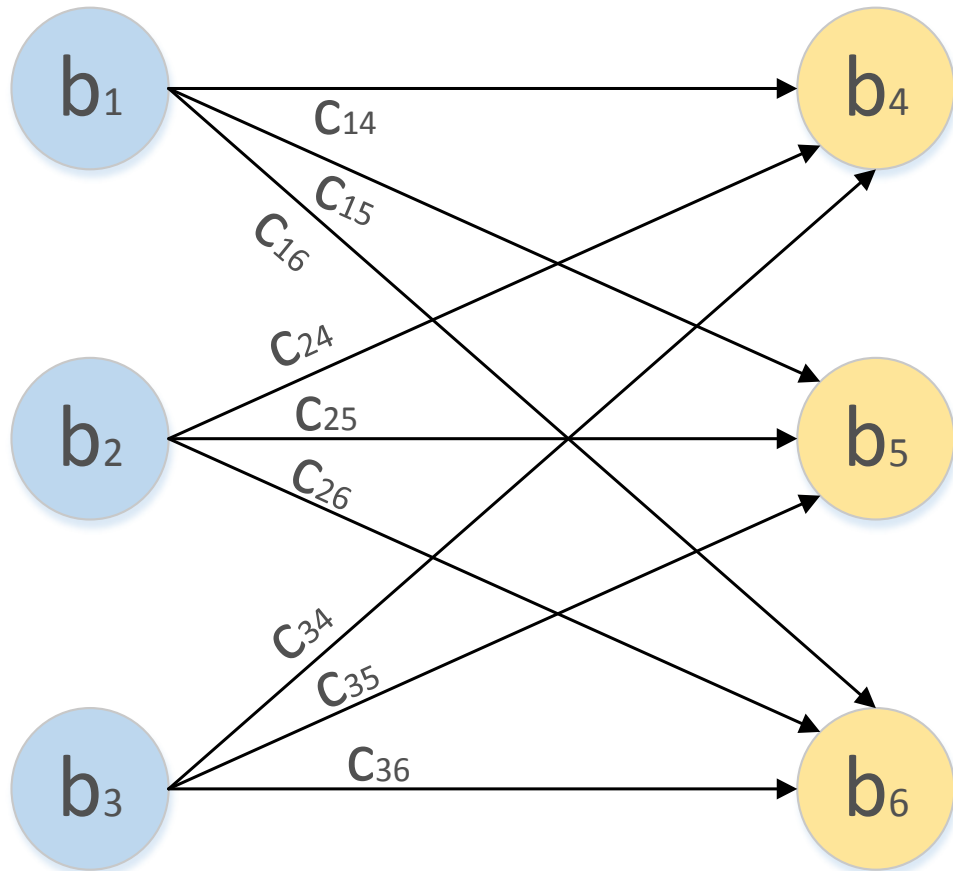
Minimum Cost Flow (MCF) Based Method

Framework



Minimum Cost Flow(MCF) Based Method

Minimum cost flow network



$$\text{minimize } \sum_{(i,j) \in A} c_{ij} x_{ij}$$

$$\sum_{j:(i,j) \in A} x_{ij} - \sum_{j:(j,i) \in A} x_{ji} = b(i) \quad \text{for all } i \in N$$

$$l_{ij} \leq x_{ij} \leq u_{ij} \quad \text{for all } (i,j) \in A$$

N is a set of n nodes

A is a set of m directed arcs

Minimum Cost Flow (MCF) Based Method

Flow network construction

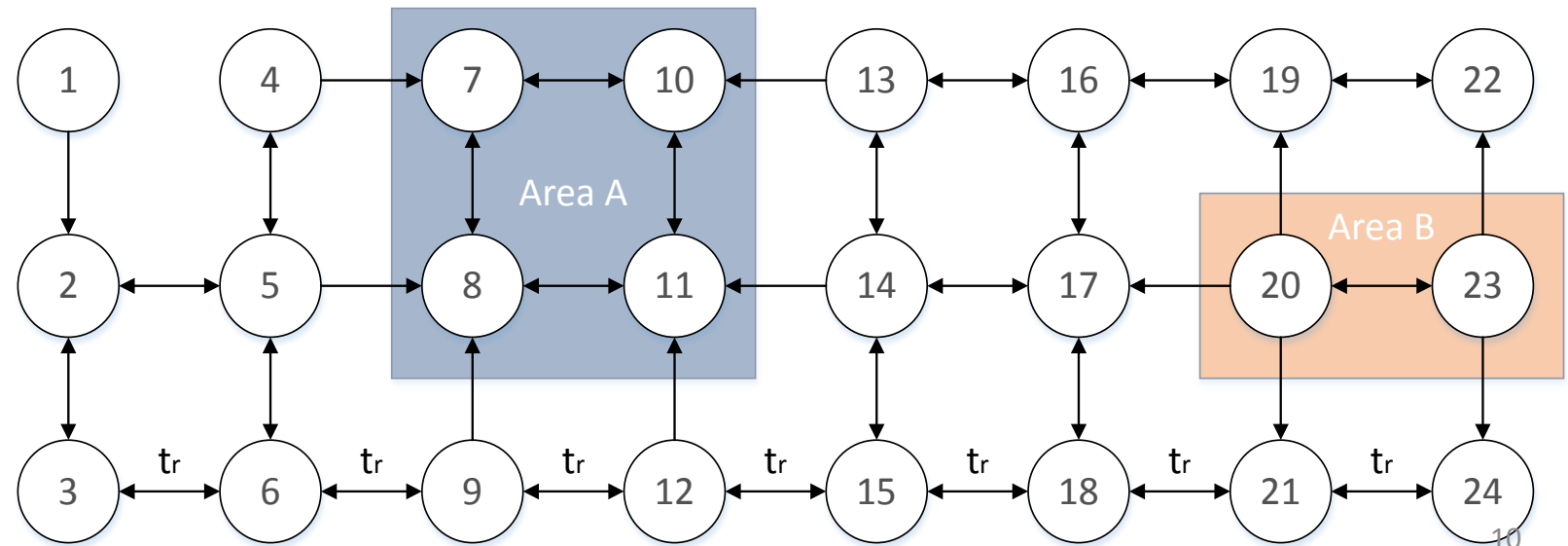
Arcs

Directions

Unit costs

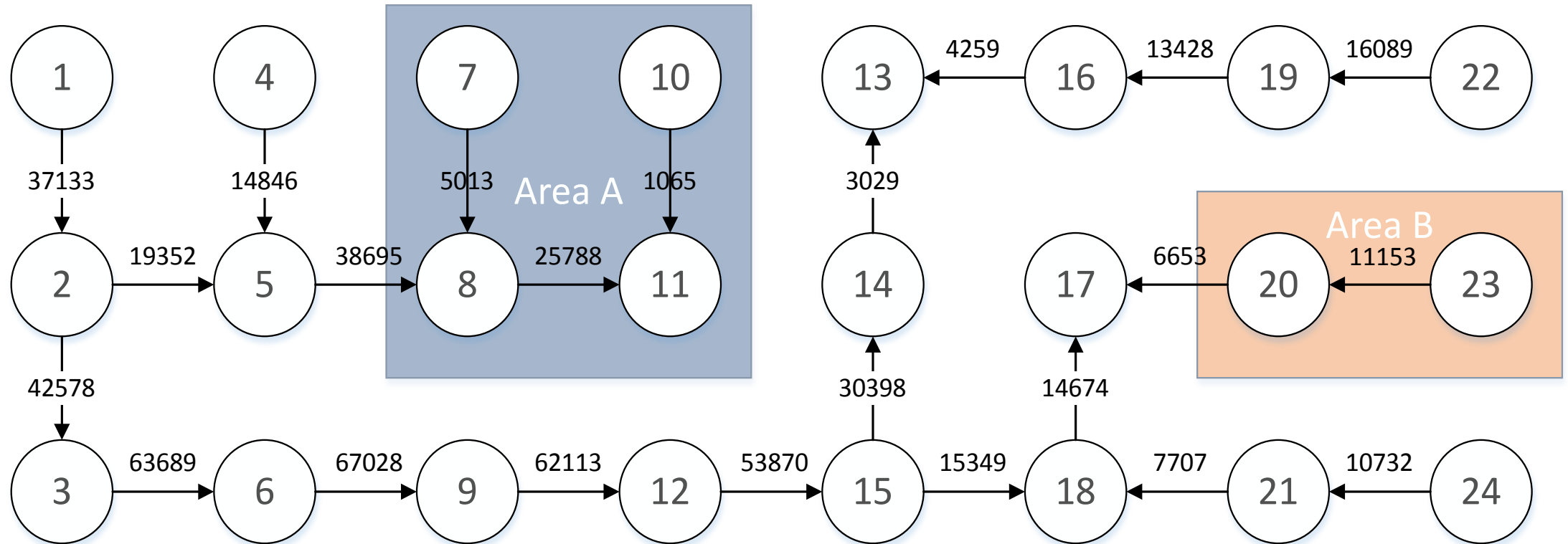
37133	14846	5013	1065	-7288	-9169	-2661	16089
24797	4497	-17920	-26853	-27369	-21327	-4500	11153
21111	3339	-4915	-8243	-8123	-8382	-3025	10732

Area A is a negative net volume area (fill);
Area B is a positive net volume area (cut).



Minimum Cost Flow (MCF) Based Method

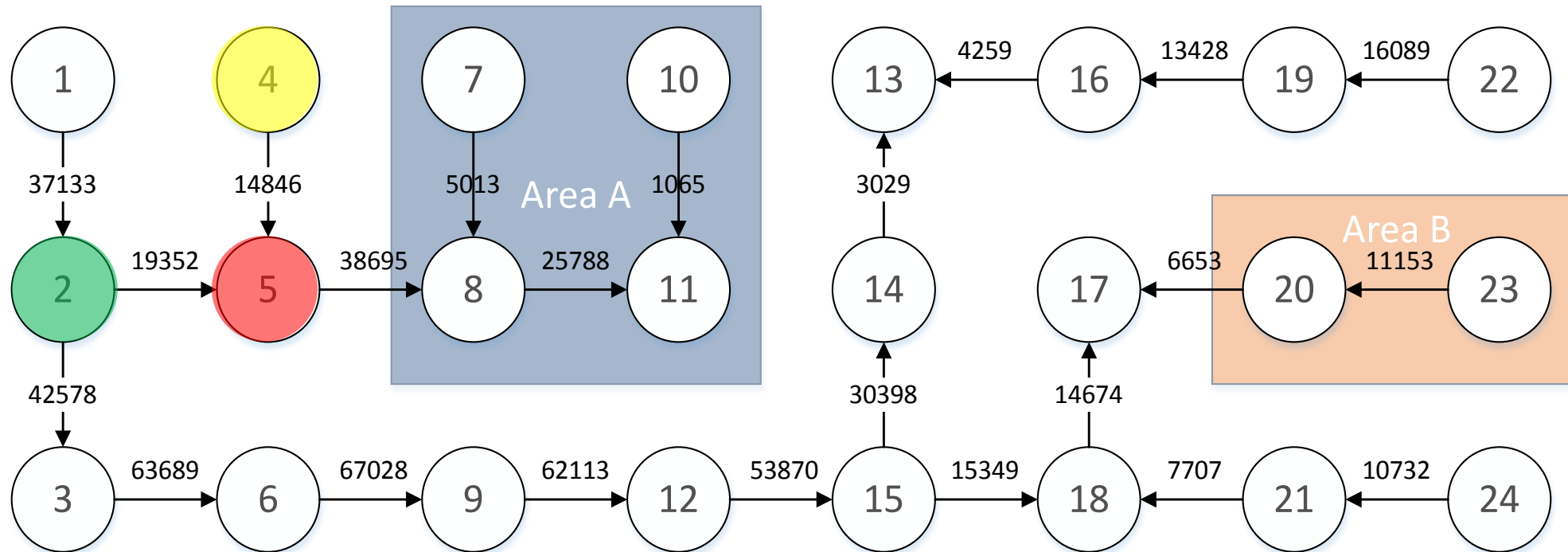
Earth Flow Network



Turning optimum material network flows into ready-to-execute haul jobs

Heuristic rules

- 1) Maximum flow first
- 2) Minimize mobilization of excavators



Haul jobs derived from optimum material flows

Sub Flow	Job	Cut	Fill	Volume	Route (R)	Predecessor
1	1	10	11	1065	-	-
2	2	22	19	2661	-	-
	3	22	16	9169	[19]	2
	4	22	13	4259	[19,16]	3
3	5	23	20	4500	-	-
	6	23	17	6653	[20]	5
4	7	5	8	4497	-	-
	8	2	8	13423	[5]	7
	9	2	11	5929	[5,8]	8

Validation & Evaluation

Optimal validation & evaluation

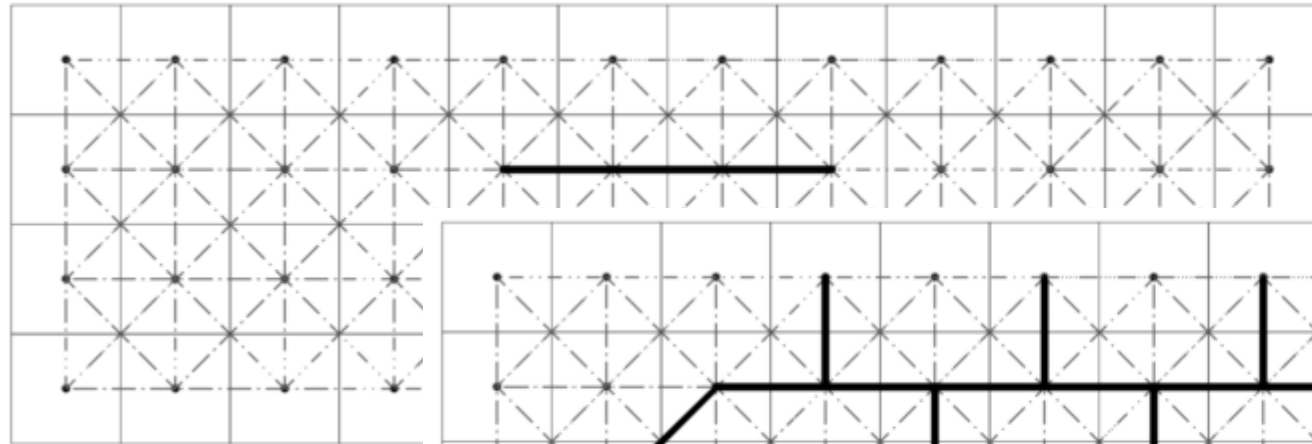
	Average weighted haul distance (m)	Haul effort (bm4)
Morley, Lu, and AbouRizk (2014) Heuristic rules	411	165,805,946
Morley, Lu, and AbouRizk (2014) Random rules	431	173,790,000
Proposed Method	401	161,543,988
Improvement compared to Random Rules	7%	8%
Improvement compared to Heuristic Rules	3%	3%

Validation & Evaluation

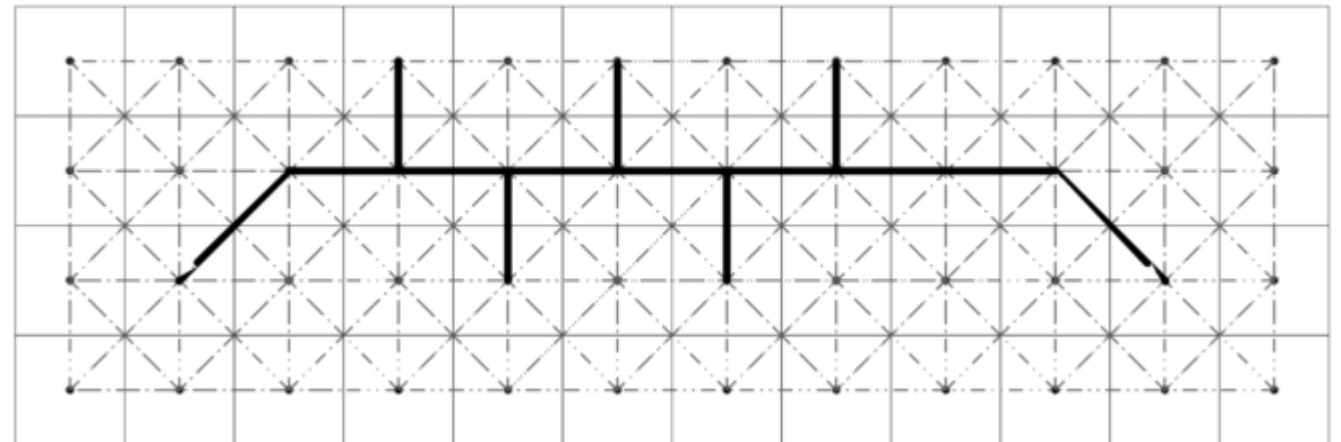
Block removal validation & evaluation

Cell 1 -15000	Cell 2 -3700	Cell 3 +3700	Cell 4 +9000	Cell 5 +9000	Cell 6 +8000	Cell 7 -1000	Cell 8 -11200	Cell 9 -2300	Cell 10 -22000	Cell 11 -6900	Cell 12 +11200
Cell 13 -62600	Cell 14 +22500	Cell 15 +33800	Cell 16 +36000	Cell 17 +23000	Cell 18 +22200	Cell 19 +8100	Cell 20 -24800	Cell 21 -9900	Cell 22 -2200	Cell 23 +14300	Cell 24 +7900
Cell 25 -3700	Cell 26 +22500	Cell 27 +28100	Cell 28 +2300								
Cell 37 0	Cell 38 -1400	Cell 39 +2300	Cell 40 +1200								

Layout 1



Layout 3



Validation & Evaluation

Block removal validation & evaluation

Mutual reliance of shortest path based method reaches up to 60%.

Mutual reliance is eliminated in proposed research.

Layout	Percentage of Jobs with Mutual Reliance	
	Liu and Lu (2014) (Original) with Floyd's Algorithm	Proposed Method
Layout1	34/57 = 60%	0%
Layout3	30/56 = 54%	0%

Conclusion

The paper proposed an approach which:

- 1) Provides an intuitive graph based interface.
- 2) takes job sequence and constructability into consideration.
- 3) Is able to generate multiple optimal solutions –practically feasible.
- 4) Eliminates “soft blocks”

Questions ?