

1 Title: A non-invasive, 3D, dynamic MRI method for measuring muscle moment arms in vivo:  
2 demonstration in the human ankle joint and Achilles tendon.

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4 Authors: EC Clarke<sup>1,2</sup>(PhD, BE, BSc), JH Martin<sup>1,2</sup> (MEngRes, BE), AG d'Entremont<sup>3,4</sup> (PhD,  
5 MAsC, BE), MG Pandy<sup>5</sup> (PhD, MEngSc, BE), DR Wilson<sup>4</sup> (DPhil, BEng), RD Herbert<sup>6,7</sup> (PhD,  
6 MAppSc, BAppSc)

7 1. Sydney Medical School, The University of Sydney, Sydney, Australia

8 2. The Kolling Institute of Medical Research, Sydney, Australia

9 3. Mechanical Engineering, University of British Columbia, Vancouver, Canada

10 4. Department of Orthopaedics and Centre for Hip Health and Mobility, University of British  
11 Columbia and Vancouver Coastal Health Research Institute, Vancouver, Canada

12 5. Mechanical Engineering, University of Melbourne, Melbourne, Australia

13 6. Neuroscience Research Australia, Sydney, Australia

14 7. The University of New South Wales, Sydney, Australia

15

16 Correspondence:

17 Dr Elizabeth Clarke

18 Murray Maxwell Biomechanics Lab, Level 10, Kolling Building 6

19 Royal North Shore Hospital, St Leonards, NSW, 2065, AUSTRALIA

20 Ph: +61-2-9926-4821

21 Fax: +61-2-9926-5266

22 Email: [elizabeth.clarke@sydney.edu.au](mailto:elizabeth.clarke@sydney.edu.au)

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25    Abstract

26    Muscle moment arms are used widely in biomechanical analyses. Often they are measured in 2D or  
27    at a series of static joint positions. In the present study we demonstrate a simple MRI method for  
28    measuring muscle moment arms dynamically in 3D from a single range-of-motion cycle. We  
29    demonstrate this method in the Achilles tendon for comparison with other methods, and validate the  
30    method using a custom apparatus. The method involves registration of high-resolution joint  
31    geometry from MRI scans of the stationary joint with low-resolution geometries from ultrafast MRI  
32    scans of the slowly moving joint. Tibio-talar helical axes and 3D Achilles tendon moment arms  
33    were calculated throughout passive rotation for 10 adult subjects, and compared with recently  
34    published data. A simple validation was conducted by comparing MRI measurements with direct  
35    physical measurements made on a phantom. The moment arms measured using our method and  
36    others were similar and there was good agreement between physical measurements (mean 41.0 mm)  
37    and MRI measurements (mean 42.6 mm) made on the phantom. This new method can accurately  
38    measure muscle moment arms from a single range-of-motion cycle without the need to control  
39    rotation rate or gate the scanning. Supplementary data includes custom software to assist  
40    implementation.

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42    Keywords: Biomechanics; muscle; MRI; muscle moment arm; tendon

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## 44 Introduction

45 Muscle moment arms are used widely in biomechanics to relate joint torques and muscle forces,  
46 and to estimate changes in muscle length that accompany changes in joint angle. Some examples  
47 include the use of muscle moment arms to determine changes in the length of muscles of patients  
48 with muscle contractures <sup>1</sup>, assessment of changes in muscle stiffness from joint torque  
49 measurements <sup>2,3</sup>, or development of subject-specific musculoskeletal models <sup>4,5</sup>. These are  
50 applications that often involve dynamic joint motion, so ideally the methods used to measure  
51 muscle moment arms for dynamic applications would be non-invasive, simple, and obtained from a  
52 moving joint. The measurement should be of the true 3D length of the moment arm <sup>6</sup>, not the length  
53 of the moment arm projected onto an anatomical plane, and it should be given as a continuous  
54 function of joint angle, not just at one angle or a small number of discrete joint angles. In some  
55 settings (e.g. clinical) it may be desirable for the method to be quick and involve as little joint  
56 movement as possible.

57 Muscle moment arms can be determined in two ways. The ‘geometric method’ involves measuring  
58 the distance from the joint axis to the muscle-tendon line-of-action whereas the ‘tendon excursion  
59 method’ involves determining the ratio of tendon excursion to joint rotation <sup>7</sup>. A requirement of the  
60 tendon excursion method is that the tendon must not be stretched during the joint rotation. The  
61 tendon strain seen in vivo as the joint rotates can be circumvented by cutting the tendon so that it  
62 can be artificially subjected to constant load during the joint rotation, but it is not possible to cut  
63 tendons of healthy human muscles so this approach is best suited to animal muscles or human  
64 cadavers. The geometric method obviates the need to cut the tendon, so is better suited for in vivo  
65 determination of human muscle moment arms. Imaging technologies can be used to determine the  
66 location of the joint axis and muscle-tendon line-of-action.

67 The simplest methods for geometric measurement of muscle moment arms capture anatomical  
68 images of the joint and muscle-tendon unit in a single plane at a few static joint positions. The  
69 images are used to calculate two-dimensional centres of rotation between consecutive joint

70 positions, and to measure the distance from each centre of rotation to the muscle-tendon line-of-  
71 action in the same plane <sup>8</sup>. A study by Rugg et al demonstrated that Achilles tendon moment arms  
72 were only minimally affected when using a fixed versus moving centre of rotation <sup>9</sup>; however, that  
73 study was performed using two-dimensional MRI scanning of the ankle joint in sequential  
74 stationary postures. Two-dimensional methods may be subject to errors in locating the joint axis  
75 because most joints do not behave as planar mechanisms. More recent studies have used three-  
76 dimensional imaging techniques to determine the 3D distance between the joint axis and the  
77 muscle-tendon line-of-action <sup>6,10-12</sup>, and a recent study by Hashizume et al <sup>6</sup> demonstrated that  
78 measurements from 2D MRI scans significantly overestimate the Achilles tendon moment arm  
79 compared to measurements from 3D MRI scans. While three-dimensional, these methods still  
80 involve static positioning of the joint at a small number of joint angles. The interest is often in the  
81 moment arm under dynamic conditions (e.g. for dynamic musculoskeletal models or joint  
82 dynamometry), and joint axes have been demonstrated to behave differently under static and  
83 dynamic conditions <sup>13</sup>.

84 A major technical advance was the use of cine phase-contrast MRI to obtain non-invasive  
85 geometric measures of joint helical axes and muscle moment arms in three dimensions under  
86 dynamic conditions <sup>14,15</sup>. The technique uses cyclical joint rotation and analysis of velocity encoded  
87 data to define the joint helical axes and calculate muscle moment arms. To our knowledge that is  
88 the only previously published non-invasive geometric technique that has been used to measure  
89 three-dimensional muscle moment arms under dynamic conditions (at the knee and ankle), and  
90 therefore as a near-continuous function of joint angle.

91 Our objective was to develop and validate a non-invasive method to measure 3D dynamic muscle  
92 moment arms that could be performed using a single joint rotation cycle, has the potential to be  
93 used under either active or passive muscle conditions, and does not require control of joint angular  
94 velocity or MRI gating.

## 95    Materials and Methods

96    *Participants:* Participants were 10 healthy adults (5 men, 5 women) with a mean age of 29 years  
97    (range 22-48 years). Healthy subjects were used for ease of comparison with other published  
98    methods. All subjects gave written informed consent to participate. The methods were approved by  
99    the Human Research Ethics Committee of the University of New South Wales.

100    *MRI scanning:* Participants were positioned prone in a 3T MRI scanner (Phillips Achieva,  
101    Netherlands) with flexible surface coils strapped to the ankle, and with the foot strapped to a custom  
102    jig that allowed an operator to passively rotate the ankle from outside the scanner bore. The thigh  
103    and hips were supported on cushions with the knee flexed between 5 and 10 degrees. The relaxed  
104    ankle was passively rotated by one of the investigators.

105    A method for tracking joint position <sup>16,17</sup> was extended to the calculation of muscle moment arms. A  
106    key feature of the method is optimised registration (co-localisation) of high-resolution static bone  
107    geometries with lower-resolution bone geometries captured using an ultrafast scanning method  
108    while the joint is slowly rotated. The coordinates describing the location of the registered  
109    geometries were used to reconstruct 3D dynamic joint rotation.

110    The scanning protocol included one high-resolution ‘static’ scan of the stationary joint (3D T1-  
111    weighted FSE, 4.7 minutes, flip angle 90°, matrix 320×320, FOV 160×160mm, TR/TE =  
112    355.76/16.68ms, slice thickness 1mm) (Figure 1A) followed by a series of low-resolution  
113    ‘dynamic’ scans obtained while the joint was slowly rotated through its range of motion (ultrafast  
114    (turbo) gradient echo, 104 seconds, 40 dynamics (phases), 8 slices (sagittal), flip angle 10°, matrix  
115    320×320, FOV 320×320mm, TR/TE = 2.731/1.34ms, slice thickness 4mm, slice gap 0.4-3.0mm,  
116    depending on joint size) (Figures 1B-C). The orientation of and gap between the 8 slices across the  
117    joint should be subject- and joint-specific; here the slice orientation was aligned with the plane of  
118    the Achilles tendon from a coronal view, and the slice gap was adjusted to capture 4-5 slices across  
119    the Achilles tendon (see Discussion). The current study used 40 repetitions or time-phases for 1-2

cycles of joint rotation (i.e., 10-20 frames each of joint flexion and extension), which required a total scan time of less than 2 minutes. Dynamic scan data were displayed as 8 ‘movies’ of the rotating joint, one for each of the 8 slices (see supplementary material). The ankle angle for each phase was measured from a single mid-sagittal slice as the angle between the anterior surface of the tibia and the base of the heel on the footplate.

*Segmentation:* A custom Matlab program (see supplementary material) was used to manually segment the tibia, talus and calcaneus on each slice from the single high-resolution static scan. This produced a dense three-dimensional point-cloud representation of the bone surfaces (Figure 2A). The same program was used to segment the tibia, talus, calcaneus and Achilles tendon for each image in each of the 8 slices generated by the dynamic scans. This produced low-density point-cloud geometries of the rotating bones and tendon (Figure 2B-C and supplementary material).

*Registration:* The rigid body motion of each segmented bone was reconstructed by registering the high-resolution bone models from the static scan with the low-resolution models from the dynamic scan using a custom Matlab program (see supplementary material). Registration was performed at each joint position using an Iterative Closest Point (ICP) algorithm<sup>18,19</sup>. The particular implementation of the ICP algorithm is stable against mis-registration that could arise when a portion of either model is missing, or when the points in one model lie beyond the bound covered by the other (e.g. when static and dynamic scans have different fields of view of the joint, such as the tibia model in Figure 2C). Corresponding point pairs were rejected if the location of the points differed by >10mm. A sensitivity analysis determined that varying this threshold from 5-15mm had a negligible impact on the quality of the registration. The registration algorithms returned tibio-talar rotation and translation matrices for each instant in time, which were used in the finite helical axis.

*Finite helical axis calculation:* The tibio-talar joint was used in this study as it is the primary joint responsible for plantarflexion and dorsiflexion of the ankle. Therefore, the helical axis was defined by motion of the talus with respect to the tibia (calculated using a custom Matlab program; see supplementary material). This information can be derived from the standard equation for rigid-body

146 motion, which was used to describe the relative motion of any point on the talus with respect to the  
147 tibial reference frame. The use of rigid-body transformation to calculate the helical axis has been  
148 well described previously<sup>20</sup>.

149 *Muscle moment arm calculation:* For each joint angle, midlines were fit between the anterior and  
150 posterior tendon segmentations for each sagittal slice; together these midlines defined a surface  
151 through the middle of the tendon (Figure 3A-B). The midline of this surface defined the three-  
152 dimensional line-of-action through the tendon for each joint angle (Figure 3B). The lines-of-action  
153 for all joint angles were stacked together and manually trimmed proximally and distally to a 50mm  
154 straight portion, to ensure that the same tendon portions were used for all joint angles (Figure 3C;  
155 also see Discussion). The muscle moment arm for each ankle angle was determined as the length of  
156 the mutual perpendicular between the joint axis and the tendon line-of-action.

157 *Validation:* We developed the custom apparatus shown in Figure 4A-B to validate the MRI method  
158 for measuring muscle moment arms. To mimic the bones in a joint, the apparatus uses a sheep tibia  
159 and femur, which was cleaned of all soft tissues and rigidly fixed to sections of PVC tubes using  
160 perpendicular wooden skewers (Figure 4). To mimic the tendon, a thin latex tube was made and  
161 filled with gelatin then secured to the bone surfaces using cable-ties. One of the PVC tubes  
162 containing the bones was fixed rigidly to a stationary base plate and the other was fixed to a handle  
163 that allowed an operator to rotate the bone about a fixed axis (a PVC tube filled with gelatin). The  
164 tendon surrogate was wrapped over a semi-circular PVC tube so that it could glide over a smooth  
165 surface with a known distance from the rotation axis. The bones and gelatin tubes were visible in  
166 the MRI scans and the tendon path was a known perpendicular distance from the fixed rotation axis  
167 (which was physically measured with Vernier callipers). The MRI scans were performed exactly as  
168 described above for the volunteers, with the operator rotating the handle on the apparatus as they  
169 would for the participants during the dynamic scans. The two sheep bones and the tendon surrogate  
170 were analysed in the same way as they were for the participants for calculation of the moment arm.

171 The physical distance between the tendon surrogate and the PVC tube axis of rotation was known  
172 and this value was compared with the ‘moment arm’ measured using the MRI method.

## 173 Results

174 The individual muscle moment arm measurements throughout ankle dorsiflexion are shown in  
175 Figure 5. At the level of individual participants, there were considerable differences in the moment  
176 arm-joint angle relationships; that is, the pattern of change in Achilles tendon moment arm with  
177 ankle angle was not consistent across all subjects. The mean moment arm (averaged across all  
178 measured angles for all subjects) was 51.5 mm.

179 The mean Achilles tendon moment arm-joint angle relationships obtained under passive (relaxed)  
180 ankle rotation using the current 3D dynamic MRI method are shown alongside measurements of  
181 Achilles tendon moment arm from other studies<sup>6,9,15,21,22</sup> in Figure 6.

182 Figure 7 compares the ‘moment arms’ measured physically and using the current MRI method from  
183 the tendon surrogate of our validation apparatus, at 14 different joint angles. The mean of 14  
184 measurements of the ‘moment arm’ for the validation apparatus, using the current MRI method and  
185 the same analysis methods as described for the human subjects, was 41.0 mm (SD=1.0 mm). The  
186 mean and maximum absolute differences between the MRI and physical measurements were 1.8  
187 mm and 2.5 mm.

## 188 Discussion

189 The mean Achilles moment arm-joint angle relationships measured with the current MRI method  
190 appear similar to the Achilles moment arm-joint angle relationships reported by others (Figure 6).  
191 (The exception is the moment arms reported by Hashizume et al<sup>9</sup>, which are smaller). This is  
192 despite differences in the scanning methods, subject populations, joint loading (active versus  
193 passive muscle contraction) and definitions of joint centre of rotation, ankle angle and tendon line-



194 of-action. While there is considerable variation at an individual level (Figure 5), the similarities in  
195 population-level data provide evidence of convergent validity.

196 The validation study performed here for 14 different joint angles showed mean and maximum  
197 errors of 1.8 mm and 2.5 mm respectively. The maximum error in the current study was compared  
198 with the mean muscle moment arms for each of the 10 subjects, to gain insight into the likely  
199 proportion of error in using this method to measure Achilles tendon moment arms in various  
200 subjects. The mean Achilles tendon moment arms for individual subjects ranged from 39.6 mm to  
201 64.1 mm, therefore using the maximum error from the validation study (2.5 mm) equates to an error  
202 range of 3.9 % to 6.3 % of the mean Achilles tendon moment arm. The maximum error of 2.5 mm  
203 from this validation study was also less than the mean error reported by Hashizume et al <sup>6</sup> in  
204 performing Achilles tendon moment arm measurements in 2D as compared with 3D, which implies  
205 that the current method is more accurate than 2D measurement of the Achilles tendon moment arm.

206 The MRI method described in this study has some advantages for measurement of muscle moment  
207 arms. First, the current method has the potential to be used with either passive movement or under  
208 active muscle contraction and can be used to measure either 2D or 3D muscle moment arms.

209 Importantly, using the current MRI method, kinematic data can be directly tracked from a single  
210 joint rotation cycle; it does not require repeated cycles of joint rotation like the method based on  
211 cine phase-contrast MRI. Another difference from the cine phase-contrast MRI method is that the  
212 current method does not require control of the joint angular velocity, nor does it require gating to  
213 synchronise the rotation cycle with image capture. For some researchers, this may simplify  
214 implementation. It may also be advantageous when the method is used in clinical populations with  
215 joint pain or limited movement.

216 A technical limitation associated with the geometric method of measuring moment arms (including  
217 the current MRI method) concerns identification of the tendon line-of-action. For example, Sheehan  
218 <sup>15</sup> defined the line-of-action as extending from the soleus myotendinous junction to the insertion of  
219 the Achilles tendon on the calcaneus, and Hashizume et al <sup>6</sup> defined the line-of-action as a straight

220 line passing through the centres of the tendon cross-sections at the proximal insertion site on the  
221 soleus and distal insertion site on the calcaneus. Another approach has been to define the line-of-  
222 action of the tendon as a straight line through a two-dimensional mid-sagittal image of the tendon  
223 <sup>21,23</sup>. It would be possible to employ the same definitions of the Achilles tendon line-of-action with  
224 the current method but the latter definition cannot be applied when the tendon is curved. In the  
225 current study the reason we measured the tendon line-of-action from a 50 mm straight region of the  
226 tendon was because we observed curvature in the distal Achilles tendon of several subjects when  
227 the ankle was in a plantarflexed position. (The ankle was passively rotated in the current study, but  
228 we confirmed that this curvature was also present when the gastrocnemius was actively  
229 contracting.) For tendons whose line-of-action is linear it does not matter which part of the tendon  
230 is chosen to define the line-of-action. However, some tendons have curved lines of action, either  
231 because they pass over underlying structures such as muscles or bones or because they are held  
232 down by a retinaculum. The curved part of the tendon cannot be used to calculate the moment arm  
233 of the muscle.

234 A limitation of the current study is that we did not perform multiple measurements on each subject  
235 so we could not assess the repeatability of the method in estimating Achilles tendon moment arms.  
236 However, the repeatability and accuracy of this MRI scanning has been assessed previously in  
237 studies of patella tracking, which found that variability and registration error were within the range  
238 of accuracy of the procedure <sup>16,17</sup>. Another limitation of the method is the low through-plane  
239 resolution and the limited number of slices containing tendon. The through-plane resolution was  
240 sufficient to define the anterior and posterior surfaces of the tendon (and therefore a midline  
241 surface), but did not allow us to define centroids through re-sliced axial cross sections, which would  
242 have been ideal. It may be possible, with an appropriate scanning field of view, to use ultrafast MRI  
243 scanning to track the three-dimensional locations of the myotendinous junction and calcaneal  
244 insertion.

245 The particular protocol presented here would be particularly useful for measuring moment arms in  
246 adults, and for tendons that are relatively wide with respect to their joint. However with some  
247 protocol modifications the MRI method itself may also be useful for other tendons and in smaller  
248 joints of children. For example, when obtaining measurements from smaller joints and smaller  
249 subjects such as children it would be necessary to reduce the slice gap for the dynamic scanning  
250 protocol so that the slices span the width of the joint. Also, for measuring moment arms in tendons  
251 that are narrow with respect to the joint (e.g. medial or lateral gastrocnemius at the knee) it would  
252 be necessary to increase the number of slices for the dynamic scanning protocol so that there are  
253 several slices through the tendon and so that the slices span the width of the joint. More slices  
254 provide more detailed spatial information for geometry registration, but they do so at the cost of  
255 increasing the scanning time per phase. That may be accommodated by slowing the joint motion to  
256 maintain joint angle resolution and minimise motion artefact. We found that a minimum of 5 slices  
257 was needed to register bone position, but increasing the number of slices beyond 8 produced  
258 blurring on the dynamic scans at the rotation speed we used. Acquisition speed could be improved  
259 by reducing the field of view. It is most important to select a slice gap that provides sufficient detail  
260 of the bones and muscle-tendon units of interest. Another parameter that could be varied is the  
261 number of phases (or repetitions): we used 40 phases which provided 10-20 data points per joint  
262 rotation from plantarflexion to dorsiflexion. The number of phases could be reduced to reduce total  
263 scan time (which might be advantageous if scans were to be obtained from participants while they  
264 performed intense muscle contractions or clinical populations with pain), or increased to capture  
265 replicates for averaging.

266 We have presented an MRI method for measuring 3D muscle moment arms while the joint is  
267 slowly rotating, and we compared measurements made with this method to direct physical  
268 measurements from a surrogate validation apparatus. The method was demonstrated in the human  
269 Achilles tendon under passive muscle conditions, but it also has the potential to be applied to other  
270 muscles and under active muscle conditions. The method is capable of measuring the muscle

271 moment arm from a single cycle of joint rotation, without the need for controlling angular velocity  
272 or (MRI-) gating the rotation cycle. This could make the method particularly suitable for application  
273 to clinical populations.

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344 Figure legends

345

346 Figure 1. Representative static and dynamic images: (A) one mid-sagittal image from the high-  
347 resolution static scan. (B) One mid-sagittal image from the low-resolution dynamic scan during  
348 plantarflexion and (C) dorsiflexion.

349 Figure 2. Registration of high-resolution static geometries with low-resolution dynamic  
350 geometries: (A) three-dimensional point-cloud geometries of the tibia (blue), talus (green) and  
351 calcaneus (red) constructed by segmenting the high-resolution static scan, (B) three-dimensional  
352 point-cloud geometries of the tibia, talus, calcaneus and Achilles tendon constructed by segmenting  
353 the bones and tendon from the 8 slices of the low-resolution dynamic scan stack, and (C)  
354 registration of the three-dimensional bone geometries shown in A (coloured) with the dynamic  
355 slices shown in B (black).

356 Figure 3. Tendon line-of-action: (A) three-dimensional geometries of the tibia, talus, calcaneus  
357 and Achilles tendon at a single joint angle. (B) Schematic of a representative tendon midline surface  
358 (grey grid surface) and the accompanying tendon midline (bold black line), for a single joint angle.  
359 (C) Stacked tendon midlines for all joint angles segmented for a single subject showing  
360 representative proximal and distal trim lines applied to all joint angles.

361 Figure 4. Validation apparatus: the validation apparatus was constructed to mimic the bones and  
362 tendons from a joint but with the ability to physically measure the ‘moment arm’. Gelatin-filled  
363 tubing was used to model the tendon and fixed axis of rotation. Dissected animal bones were used  
364 to mimic the bones in a human joint: one was fixed stationary to the base plate, and the other  
365 rotated about a fixed gelatin-filled PVC tube axis. The tendon surrogate was fastened to the bones  
366 using cable ties and glided over another fixed PVC tube axis of larger diameter. The distance from  
367 the surrogate tendon to the fixed rotation axis was physically measured from the apparatus for  
368 comparison with the MRI method.

369 Figure 5. Achilles tendon moment arms of individual participants: unscaled Achilles tendon  
370 moment arm-joint angle relationships (black symbols) for 10 individual participants. Each  
371 participant's data is shown in a separate panel. The differences in the range of ankle joint angles  
372 between subjects (i.e., differences in the range of the x-axis) are due to differences in ankle  
373 flexibility.

374 Figure 6. Comparison of moment arms estimated using several 3D MRI methods: the  
375 prominent step from low to high moment arm using the current MRI method at an ankle angle of  
376 approximately 65 degrees occurred because subjects were tested over different ranges of motion.  
377 The current MRI method compares well with other measurements in the literature, despite  
378 differences in the methods and subject populations. The data from the current study are mean  
379 moment arms for all 10 subjects, measured in 3D while the ankle is being passively rotated. Data  
380 from Sheehan are unscaled moment arms measured in 3D under active ankle rotation. Data from  
381 Hashizume et al are mean moment arms measured in 3D with the ankle at rest at a range of angles.  
382 Data from Fath et al and Maganaris et al are mean moment arms measured in 2D with the ankle  
383 relaxed at rest for a range of ankle angles, using a moving centre of rotation method. The data from  
384 Rugg et al are mean moment arms measured in 2D with the ankle at rest but under active muscle  
385 contraction, using a centre of rotation method.

386 Figure 7. Measurements from the validation apparatus: the data points are MRI measurements  
387 from a single rotation movement of the surrogate validation apparatus and the solid line is the  
388 physical measurement of the 'moment arm' from the centre of the rotation axis to the tendon  
389 surrogate.

390

391 Supplementary material 1. Video file showing 27 dynamic phases for one mid-sagittal slice  
392 through a representative ankle. The complete dynamic scan set for this study included 8 slices  
393 across the ankle for 40 dynamic phases.

394

395   Supplementary material 2. Video file showing registration of the high-resolution static geometries  
396   with low-resolution dynamic geometries for 27 dynamic phases.

397

398   Supplementary material 3. Link to google code website containing custom Matlab code for  
399   segmentation, registration, helical axis and muscle moment arm calculation

400

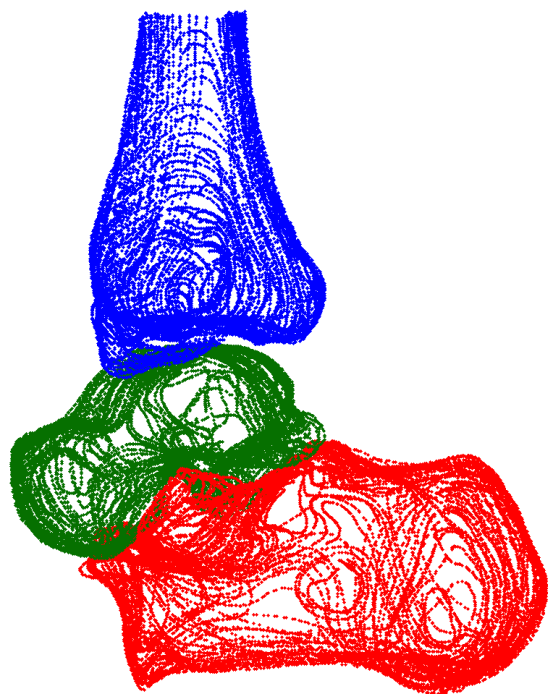
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Figure

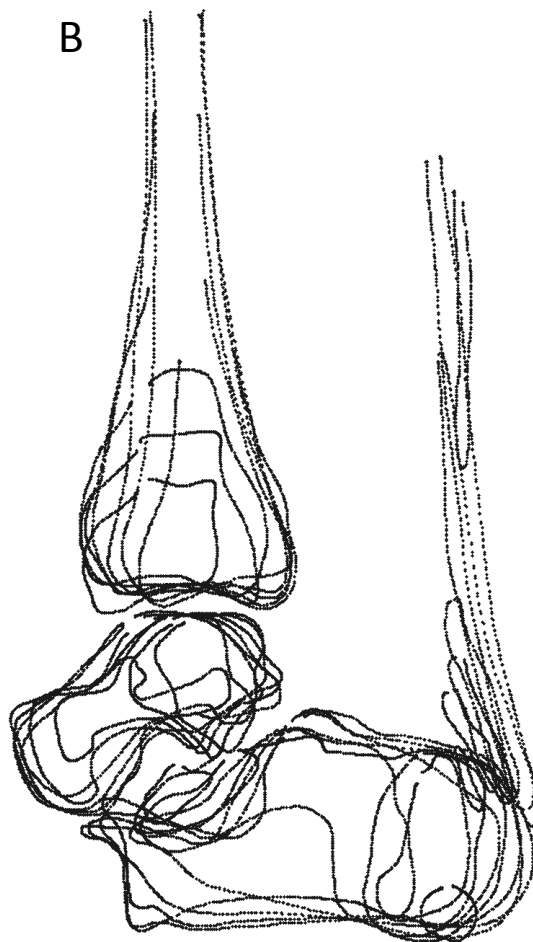


Figure 2

A



B



C

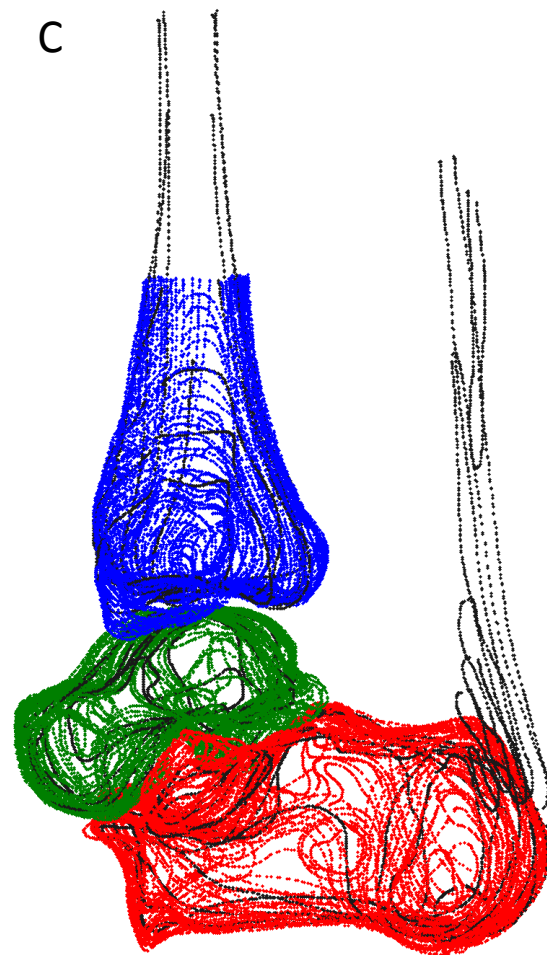


Figure 3

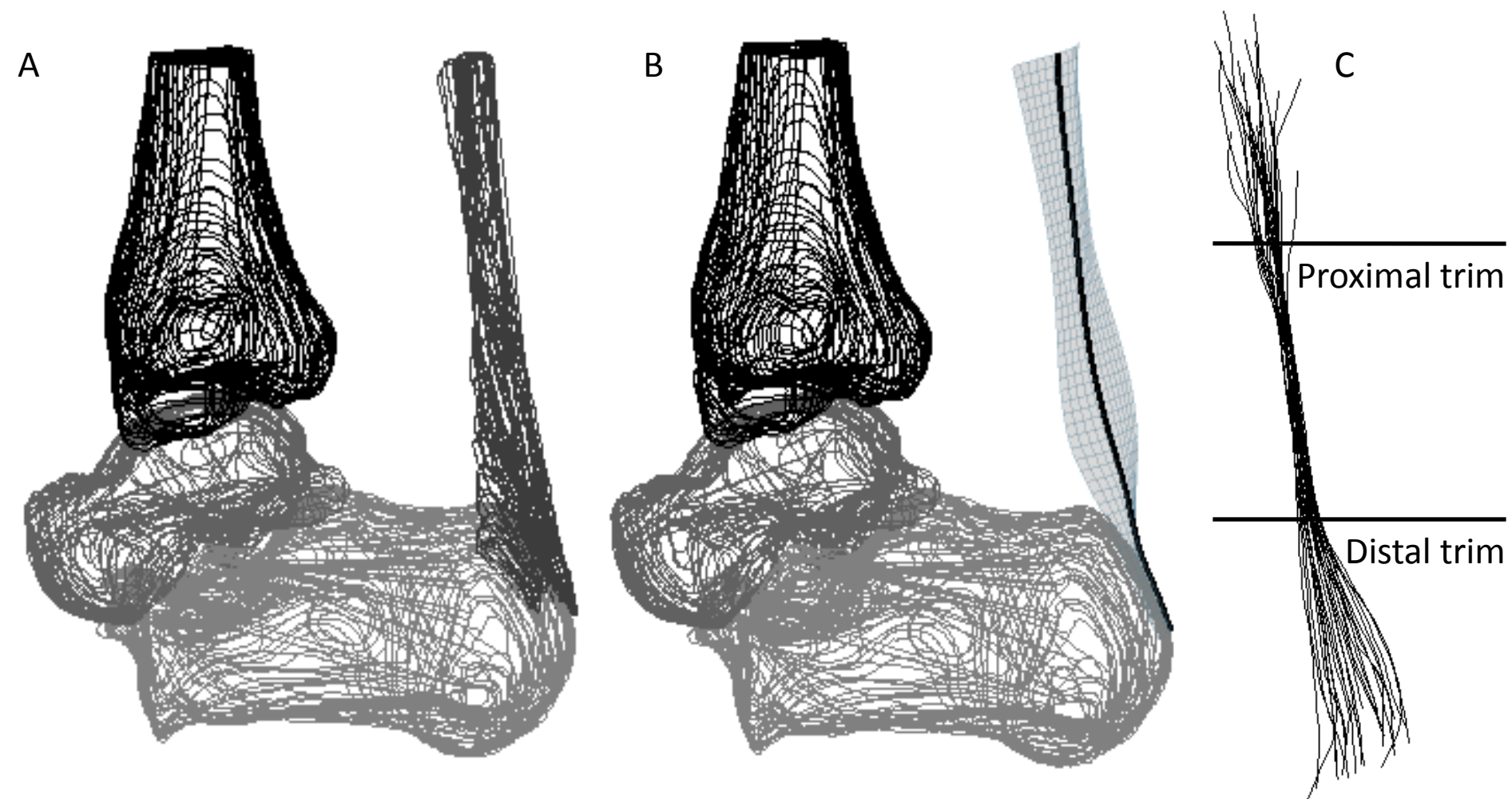
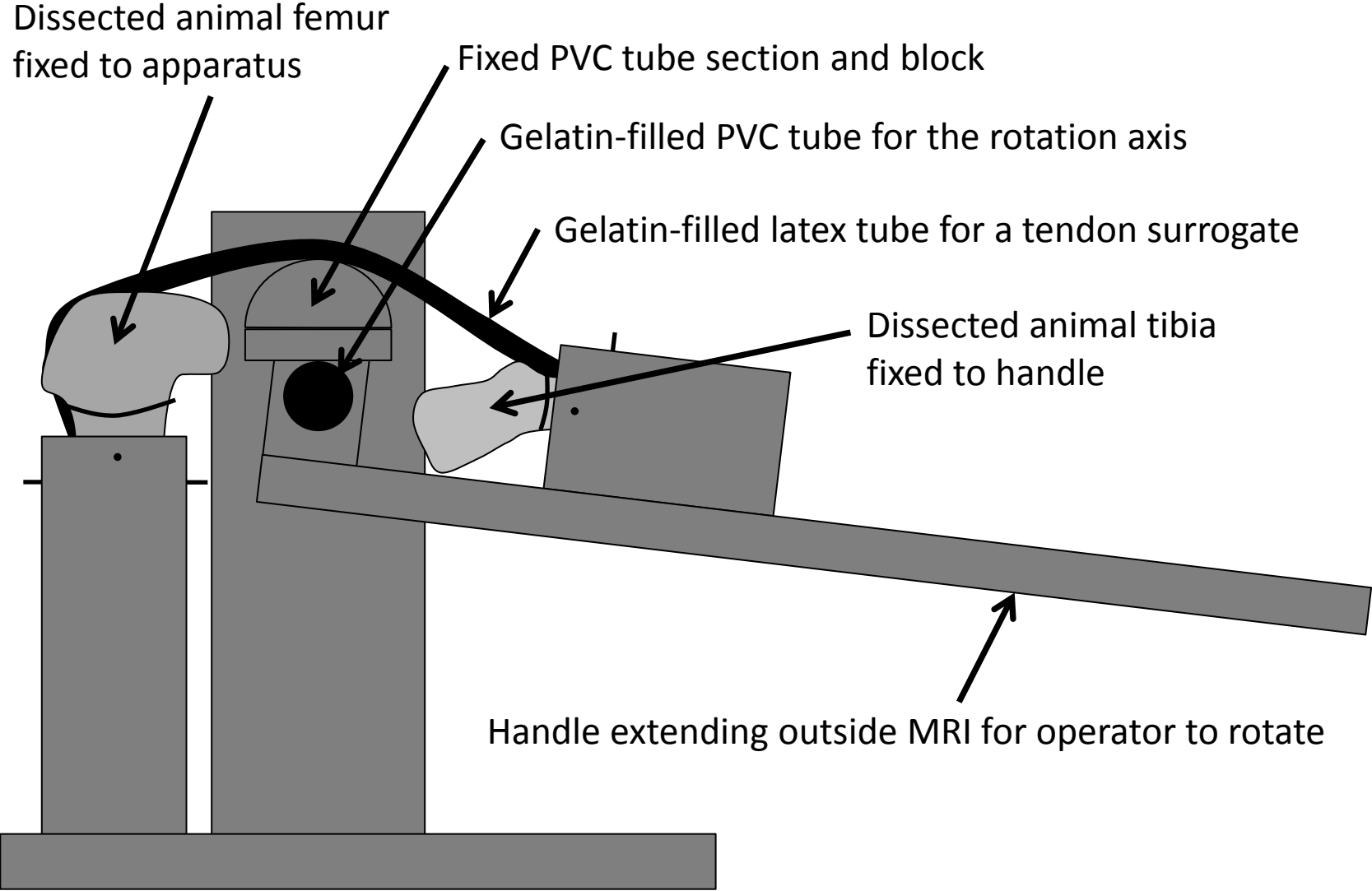


Figure 4A



SIDE VIEW

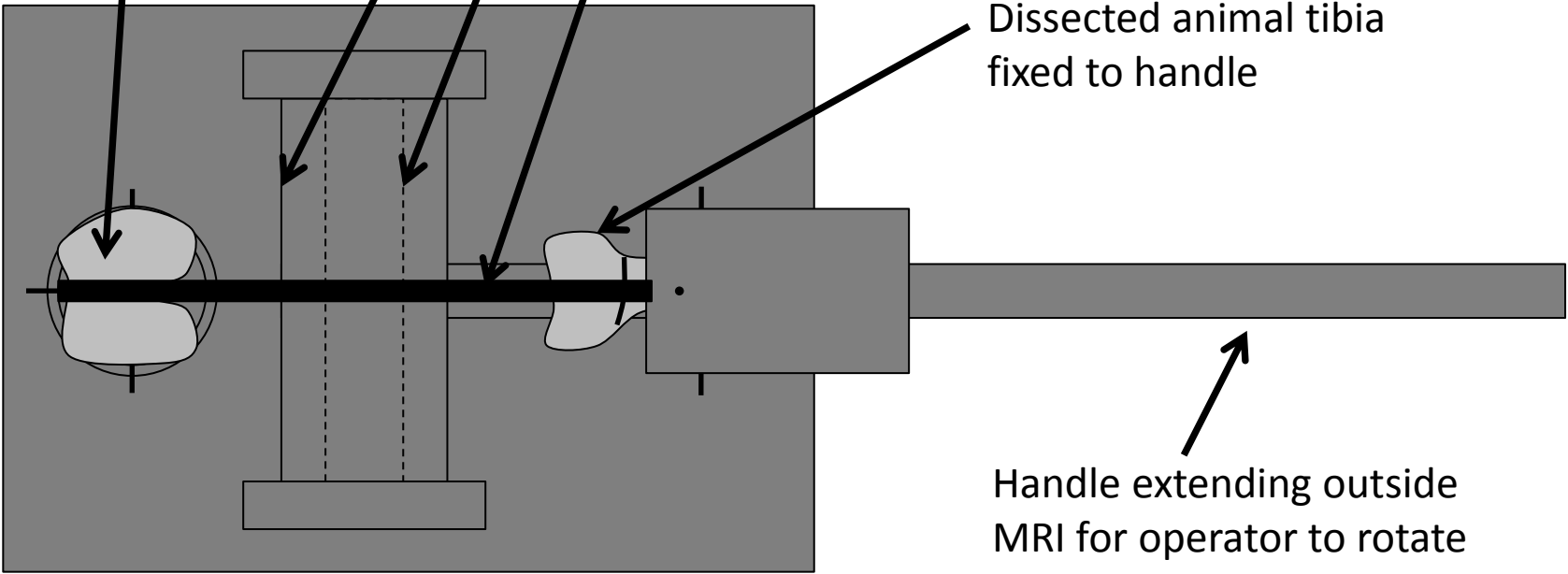
Figure 4B

Dissected animal femur  
fixed to apparatus

Fixed PVC tube section and block

Gelatin-filled PVC tube for the rotation axis

Gelatin-filled latex tube for a tendon surrogate



Dissected animal tibia  
fixed to handle

Handle extending outside  
MRI for operator to rotate

TOP VIEW



Figure 5

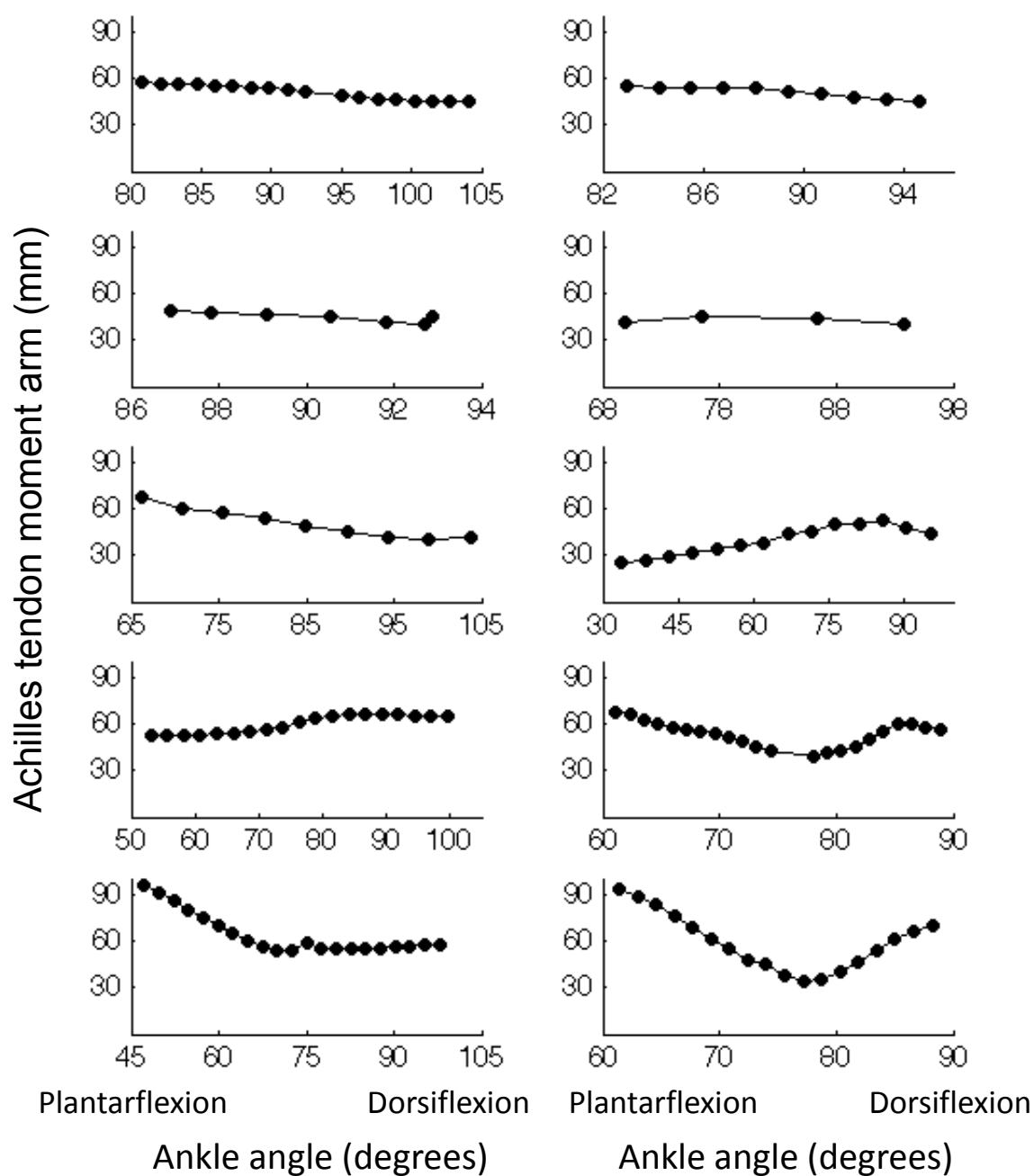


Figure 6

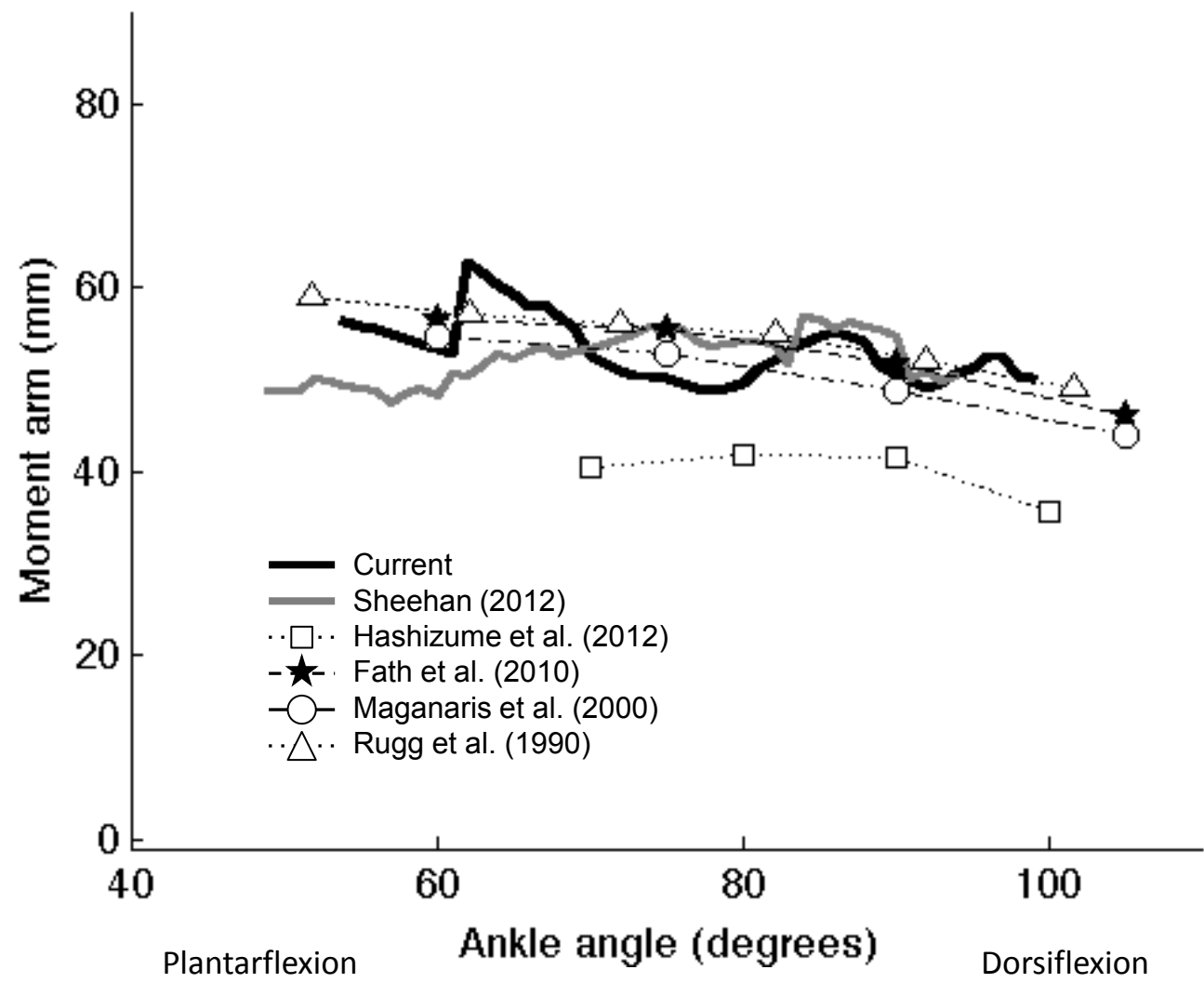
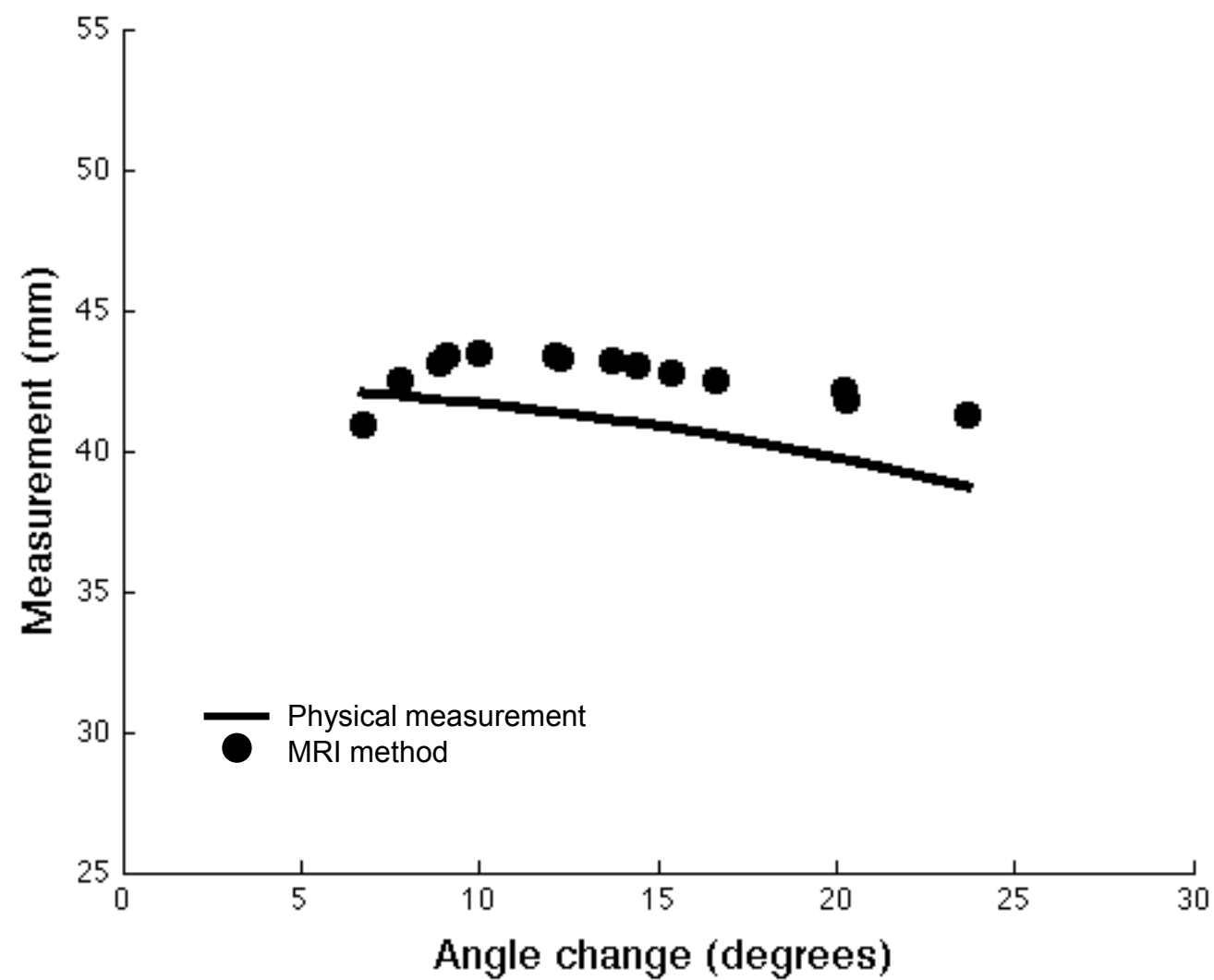


Figure 7



# Supplementary data 1

[Click here to download Supplementary data: SupMaterial\\_Movie\\_Figure1.avi](#)

**Supplementary data 2**

[Click here to download Supplementary data: SupMaterial\\_Movie\\_Figure2.avi](#)

**Supplementary data 3**  
[Click here to download Supplementary data: SupMaterial\\_3.docx](#)