Influence of turbidity and aeration on the albedo of mountain streams

by

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Abstract

Stream surface albedo plays a key role in the energy balance of rivers and streams that are exposed to direct solar radiation. Most physically based models assume that stream albedo lies between 0.03 and 0.10, based primarily on measurements from low-gradient streams with low suspended sediment concentrations. Albedo should depend upon solar elevation angle, suspended sediment, aeration, and fraction of direct vs diffuse radiation. However, there is no model available for predicting the dependence of albedo on these factors. This study quantified the dependence of albedo of mountain streams on the controlling factors in order to improve the representation of albedo in energy balance studies. Proxy measures for albedo using digital camera imagery were also developed and assessed.

Stream surface albedo was measured at nine sites with a variety of gradients and suspended sediment characteristics in the southern Coast Mountains of British Columbia, Canada. As expected, albedo of low-gradient, non-whitewater (flatwater) streams increased with solar zenith angle, suspended sediment concentration, and proportion of diffuse to direct solar radiation, ranging between 0.025 during cloudy periods in clear water to 0.25 for turbid water at zenith angles of less than 20 degrees. Albedo varied with discharge in steep reaches or at channel steps and cascades where flow was visibly aerated, with a range of 0.09 to 0.33. In clear weather, albedo exhibited notable diurnal variability at flatwater sampling sites. For example, during late summer, surface albedo typically fluctuated between 0.08 and 0.15 on a diurnal basis at a flatwater site on the highly turbid, glacier-fed Lillooet River. Physically based representations of albedo should be incorporated into energy balance models in order to improve predictions of stream temperature, especially for future scenarios.

Preface

This thesis is original work completed by the author. Guidance was given by the supervisory committee: Dan Moore, Brett Eaton, and Ian McKendry. A version of this work has been delivered as a presentation (McMahon, A. & Moore, R.D., Influence of turbidity and aeration on the albedo of mountain streams) on which the author acted as the lead investigator, composing and delivering the presentation at the 2016 Canadian Meteorological and Oceanographic Society (CMOS) / Canadian Geophysical Union (CGU) Joint Assembly on June 2, 2016 in Fredericton, New Brunswick.

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Chapter 1

Introduction

1.1 Motivation for the study

Water temperature governs a range of physical, biological, and chemical processes in streams, and plays a crucial role in the overall health of aquatic ecosystems (Coutant, 1999; Webb et al., 2008; Symonds and Moussalli, 2011). For example, water temperature influences fish mortality (Thomas et al., 1986), distribution (Hughes, 1998), growth and developmental rates (Shelbourn et al., 1973; Elliott and Hurley, 1997), pollutant uptake (Ficke et al., 2007), reproductive fitness (Fenkes et al., 2016), and competitive interactions (Reeves et al., 1987). In addition, dissolved oxygen solubility decreases at higher temperatures, while oxygen requirements for biological processes increase. Dissolved oxygen is a major determinant of aquatic habitat quality during the summer when the oxygen needs of aquatic organisms are highest and availability is at a minimum (Caissie, 2006).

Environmental changes and human activity can modify fluvial thermal regimes (Webb et al., 2008). Forest disturbance associated with wildfire and harvesting in riparian zones increase a stream's exposure to solar radiation, typically resulting in increases in summer water temperature (Moore et al., 2005). Reduction of streamflow associated with flow regulation and withdrawals increases the sensitivity of stream temperature to surface energy inputs by decreasing stream depth (Sinokrot and Gulliver, 2000). Additionally, dam releases may not be the same as downstream river temperature, providing another mechanism for altering water temperature (Olden and Naiman, 2010). Climate change can influence stream temperatures by influencing the timing and magnitude of streamflow as well as the surface energy exchanges (Meisner, 1990; Ficke et al., 2007; Isaak et al., 2010).

Predictive models are often used to assist with designing and evaluating management options to minimize the effects of human activity on stream temperature—for example, for evaluating the sensitivity of stream temperature to flow reductions associated with withdrawals (Dymond, 1984; Bartholow, 1991). The most rigorous approach to modelling stream temperature is through the use of deterministic models that explicitly simulate surface energy exchanges, which include short- and longwave radiation and turbulent exchanges of sensible and latent heat (Sinokrot and Stefan, 1993; Caissie, 2006; Hannah et al., 2008). In streams that are exposed to direct sunlight, solar radiation is typically the dominant component of the energy balance during the summer (Moore et al., 2005).

Stream surface albedo—the fraction of incident solar radiation that is reflected—is typically not measured in stream temperature modelling studies. Some models, like HeatSource (Boyd and Kasper, 2003), compute albedo using a published function of solar incidence angle. Meier et al. (2003) accounted for variability in albedo in terms of solar zenith angle and cloud cover according to relations reported by Anderson (1954). Many modelling studies used an assumed fixed albedo. For example, a fixed value of 0.05 was assumed by Magnusson et al. (2012) in studies on proglacial channels. A lower fixed value of 0.03 was assumed by Caissie et al. (2007) for a pair of low-gradient rivers.

The overall objective of this study is to quantify the dependence of the albedo of mountain streams on the controlling factors to improve the representation of albedo in energy balance models. Progress in the subject will improve energy balance models and ultimately increase confidence in water temperature estimates that drive decision making in riparian and river management. The following section provides a review of the variability of water surface albedo based on both theory and measurements, and the final section summarizes the specific objectives of the study and the structure of the thesis.

1.2 Variability of water surface albedo

The Fresnel equations predict that reflectance of a light beam striking a surface increases at greater incidence angles (between the incident ray and the normal). At high solar altitudes under clear-sky conditions, albedo of the water surface is typically between 0.03 and 0.10 (Oke, 1987). At lower solar altitudes (greater incidence angles), however, values approaching 1.0 have been observed as the sun approaches 0° (Nunez et al., 1972). Clouds and haze greatly enhance scattering of solar radiation, increasing the number of rays travelling at angles other than the solar elevation angle. At low solar elevation angles, this scattering increases the number of rays incident on the water surface at angles greater than the solar elevation angle, decreasing the amount of light reflected by the

surface, consequently decreasing albedo. Conversely, scattered light increases albedo at high solar elevation angles, since a greater number of rays strike the water surface at decreased angles compared to the solar elevation angle (Katsaros et al., 1985).

Increased water surface roughness has a similar effect on reflectance. When the water surface is roughened and solar altitude is high, there is a higher probability that incident beams will be reflected off a sloping rather than horizontal surface, increasing surface albedo. At low solar altitudes, a rough water surface decreases albedo since beams would be more likely to encounter a raised slope rather than glancing off the surface (Oke, 1987).

The relation between albedo, solar elevation angle, and surface roughness has been quantified for lakes and oceans (e.g. Nunez et al., 1972; Payne, 1972; Katsaros et al., 1985; Jin et al., 2004). Payne (1972) measured ocean surface albedo values ranging between 0.03 at high sun angles to 0.45 for solar altitudes below 10°, although with considerable scatter for low sun angles. Using wind speed as a proxy for surface roughness, the effect of roughness was most pronounced at low solar angles. The negative albedosurface roughness relation was most pronounced at solar angles between 17 and 25°, whereas the positive relation at higher solar elevation angles was relatively small in comparison. Nunez et al. (1972) found that increasing wave height had a modest influence on albedo, except for solar altitude angles lower than 15°, when albedo was suppressed with increasing wave heights. Both studies found that the dependency between solar altitude and albedo decreases with increasing cloud cover, becoming undetectable during overcast conditions. Subsequent work has parameterized ocean surface albedo in terms of the driving physical processes with good predictive accuracy. For example, Jin et al. (2004) developed a parameterization of spectral and broadband albedo ocean surface based on solar zenith angle, wind speed, and ocean chlorophyll concentration, accounting for differences between direct and diffuse solar radiation components, achieving a model standard error of 0.014.

The effects of suspended sediment and aeration on albedo have been examined by field and laboratory studies focused on the spectral reflectance of lake and ocean surfaces (e.g. Whitlock et al., 1982; Koepke, 1984). In a laboratory study, Han (1997) found that reflectance increased non-linearly in the visible spectrum as sediment was added, with the dependence of reflectance on SSC decreasing at higher concentrations. At SSC = 500 mg/L, reflectance was highest between 600 and 700 nm, with 23% of natural sunlight being reflected. Whitlock et al. (1982) found in laboratory studies that the reflectance of dense foam with high aeration, consisting of multiple bubble layers, averaged approximately 50% in visible wavelengths. Koepke (1984) measured the albedo of foam

patches on the ocean surface. Fresh foam patches measured 1 s after generation had an average spectral reflectance of 41%, decaying to 16% after 10 s. The average spectral reflectance of all foam patches was 22%.

1.3 Albedo representation in energy balance studies

Table 1.1 provides a summary of measured stream surface albedo. Leach and Moore (2010) found that mean albedo was 0.05 over pools and glides, and 0.06 over riffles. Evans et al. (1998) reported a mean albedo of 0.07, although there was distinct diurnal variability in albedo attributed to the solar elevation angle. Monthly daily mean albedo values ranged between 0.06 in July and 0.08 in November due to the differences in average solar position between months. Neilson et al. (2009) measured albedo on a low gradient reach of the Virgin River, Utah, USA, for turbidities ranging from 2 to 440 nephelometric turbidity units (NTU). Albedo was less than 0.10 when the river's turbidity was low, but was enhanced by 0.03 to 0.07 at higher levels of turbidity. Working on turbid proglacial streams, Knudson (2012) found that albedo was enhanced by SSC and varied with solar zenith angle. For Lillooet River, albedo ranged from 0.08-0.13, compared to 0.05-0.10 measured on two tributary reaches. Chikita et al. (2010) reported a mean albedo of 0.1 for a proglacial stream with suspended sediment concentrations typically exceeding 200 mg/L, with daily maxima greater than 500 mg/L (Kido et al., 2007).

Table 1.1: Summary of stream surface albedo representations used by previous river energy balance studies. NS indicates values were not specified.

Study	Location	Albedo	Channel Gradient	SSC / NTU
Evans et al. (1998)	Staffordshire, UK	0.05	NS; low gradient	NS; low SSC
Hannah et al (2008)	Aberdeenshire, UK	NS	3-15%	NS
Neilson et al. (2009)	Utah, USA	NS	0.12 - 0.39%	$2\text{-}440\ NTU$
Chikita et al. (2010)	Alaska, USA	0.1	2 30%	>200 mg/L
Leach & Moore (2010)	BC, CA	0.05 - 0.06	2.20%	NS; low SSC
Benyaha et al. (2011)	NB, CA	0.01 - 0.05	NS; low gradient	NS
Richards & Moore (2011)	BC, CA	0.1 - 0.4	26%	60-100 mg/L
Knudson (2012)	BC, CA	0.08 - 0.10	0.60%	34-831 mg/L
Khamis et al. (2015)	Cirque de Gavarnie, France	NS	NS; high gradient	NS

Some work has found that stream surface albedo can be considerably higher than the typical 0.03-0.10 range. Working on a steep proglacial channel, Richards and Moore (2011) found that albedo ranged between 0.10 at low flows up to 0.40 at higher flows as the water surface became increasingly aerated. Albedo varied nonlinearly with discharge

(a proxy for aeration), with an additional term to account for incoming solar radiation, which represents the combined effects of solar elevation angle and the direct fraction of solar radiation. The variable representation of albedo improved the prediction of net radiation at the site: the Nash-Sutcliffe efficiency of the radiation model was 0.81 using the variable albedo compared to 0.75 and 0.78 using fixed albedo values of 0.05 and 0.10.

1.4 Research objectives and thesis structure

The review of the literature in section 1.2 indicates that stream surface albedo can deviate significantly from the typical range of values assumed in many stream temperature modelling studies, especially for turbid and/or aerated conditions. Both theory and observations indicate that albedo should depend on (a) angle of incidence, (b) fractions of direct vs diffuse solar radiation, (c) turbidity and (d) degree of aeration. However, there is currently no quantitative model available for predicting the dependence of stream surface albedo on these factors. The specific research objectives addressed by the thesis are:

- 1. to quantify the dependence of albedo on suspended sediment, solar position, fractions of direct vs diffuse radiation, and aeration for a sample of mountain streams that encompass a range of flow regimes, gradients, and channel morphologies;
- 2. to develop a statistical model to predict albedo that could be easily incorporated into energy balance models; and
- 3. to develop and assess the viability of proxy measures for albedo using digital camera imagery.

The remainder of the thesis is organized as follows. Chapter 2 describes the study area, field methods, and data analysis. Chapter 3 presents the results of the field work and data analysis. Chapter 4 describes how the results of this study address the research questions outlined previously. Chapter 5 summarizes the conclusions of the study and identifies areas where future research is necessary.

Chapter 2

Methods

2.1 Study area and field sites

Research focused on nine streams in the southern Coast Mountains of British Columbia, Canada, which encompassed a range of flow regimes and channel morphologies that are representative of a broad range of conditions that occur in mountain streams (Table 2.1; Figure 2.1; Figure 2.2). The study sites spanned a range of gradients between 0.17% and 9.48%, stream discharges between 1 m³s⁻¹ and 400 m³s⁻¹, and suspended sediment concentrations from 5 mg/L to 700 mg/L.

Sites with minimal topographic and vegetative shading were preferred in order to minimize shadows on the stream surface so that albedo measurements could be taken consistently in direct lighting conditions during clear weather. In order to sample a wide range of sun angles, suspended sediment concentrations and discharges, measurements were typically collected from mid-morning until sunset. Monitoring occurred on 29 days between May and September 2015 with the goal of sampling each site regularly throughout the field season. However, sampling during the field season was interrupted by wildfires in the region; access to upper Lillooet River and North Creek was prohibited during July and August as the result of the Cougar Creek wildfire in the Lillooet Valley. Heavy wildfire smoke throughout the area in early July created air quality concerns, preventing any sampling until smoke had dispersed.



Figure 2.1: Sites used in the study.

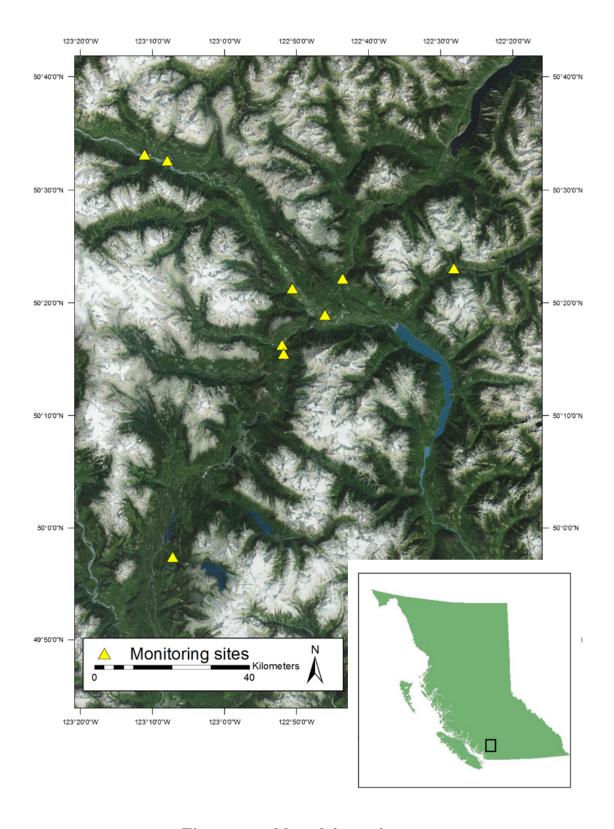


Figure 2.2: Map of the study area.

Table 2.1: Stream reaches used in the study. No. Sites = the number of sites on the reach where measurements were made. VF = sky view factor.

* indicates that channel width was estimated from Google Earth. The lower Lillooet reach is located at the BC-99 road crossing. The upper reach is located at kilometre 15 on the North Lillooet Forest Service road.

Site	Latitude	Longitude	No. Sites	Channel Type	Bankfull	Gradient (%)	\overline{VF}
					Width (m)		
Birkenhead R.	50.370	-122.727	2	riffle-pool	31.3	2.32	0.67
Cayoosh Cr.	50.385	-122.469	2	step-pool	7.6	8.19	0.79
Lillooet R. lower	50.317	-122.768	1	riffle-pool	68.4	0.58	0.76
Lillooet R. upper	50.542	-123.129	1	riffle-pool	155*	0.24	0.63
Miller Cr.	50.356	-122.843	1	riffle-pool	21.9	0.17	0.59
North Cr.	50.558	-123.183	3	cascade-pool	10.5*	2.32	0.68
Rubble Cr.	49.957	-122.120	3	cascade-pool	17.9	9.48	0.61
Rutherford Cr.	50.272	-122.867	3	cascade-pool	37.7	5.81	0.90
Soo R.	50.258	-122.864	1	riffle-pool	64.1	0.22	0.87

2.2 Field methods

Incident and reflected solar radiation, $K\downarrow$ and $K\uparrow$, were measured with a pair of thermopile pyranometers mounted on a 2.5 m long pole suspended manually over the water surface and fixed to a tripod on shore (Figure 2.3). Incident solar radiation was measured with a Kipp & Zonen CM6B pyranometer mounted facing upwards. An integrated level on the CM6B ensured that the pyranometer remained level during measurements. Reflected solar radiation was measured with a Kipp & Zonen CM3 pyranometer pointed downwards and mounted to a gimbal joint to hold it level.

Pyranometers recorded voltage values (mV) that were converted to irradiance (Wm⁻²) using the sensitivity of each device (mV/Wm⁻²). The pyranometers were scanned every 1 s and averaged every 5 s with a Campbell Scientific CR10X data logger. Albedo, α , was calculated as:

$$\alpha = K \uparrow / K \downarrow \tag{2.1}$$



Figure 2.3: Monitoring set-up used to measure albedo and obtain camera imagery mounted at the end of the horizontal support pole.

Pyranometers were typically held at 0.5 m above the water surface during albedo measurements. Adjustments to height and orientation were made to keep shadows or rocks out of the pyranometer's field of view. When sampling at hydraulic jumps, pyranometers were positioned higher to prevent spray from swinging the lower pyranometer and compromising the stability of the measurement.

Albedo was sampled at several points on the stream surface at sites with visible white-water to compare albedo values at points with varying degrees of aeration. During clear weather, each measurement usually lasted 60 to 120 s. Under variable lighting conditions, albedo values were not steady as incoming solar radiation values shifted, so measurements had to be longer to ensure that a steady albedo value had been obtained. Pyranometers were covered between measurements to zero out irradiance values and protect the instrumentation. During clear weather with consistent lighting conditions, albedo measurements were taken every 30 min. Additional measurements were taken during periods of variable cloud cover when atmospheric transmissivity changed frequently. Reflected irradiance was measured during rainy weather early in the study period, but values were small enough that they were difficult to distinguish from noise and resulting albedo values were unreliable. Therefore, sampling was avoided during periods of rain, when incoming solar radiation was minimal.

2.2.1 Suspended sediment

Suspended sediment samples were collected every 2 h using a DH-48 depth-integrated sampler at the location of each albedo measurement. Samples were processed at a laboratory at the UBC Department of Geography. The mass of sediment in each sample was calculated by weighing 47-mm glass microfiber filters, pumping samples through the filters, and then drying and re-weighing each filter. Suspended sediment concentration, SSC (mg/L), was then calculated by dividing the sediment mass by the sample volume.

2.2.2 Streamflow

Discharge was measured at reaches in which albedo measurements were made over aerated portions of streamflow. Channels where streamflow measurements were recorded tended to be narrow, relatively steep, irregular, and boulder filled with cascade-pool or step-pool morphologies, and were appropriate for salt dilution gauging in place of the standard velocity-area method. Dry salt injection was used since flow was adequately turbulent to facilitate rapid solute dissolution and mixing (Hudson and Fraser, 2005; Richardson, 2015). Salt was injected hourly or more frequently if stream discharge changed rapidly. Temperature-corrected electrical conductivity, EC_T , was monitored with a pair of WTW Cond 3310 conductivity meters and WTW Tetracon conductivity probes downstream of the injection point. The meters were staggered by 5 to 10 m in order to verify that complete solute mixing had occurred. Background EC_T (EC_{BG}) was measured prior to injection, and the changes in EC_T were monitored as the injected salt wave moved past the probes until EC_T had returned to the background level. The temperaturecorrected calibration factor CF_T (kg m⁻³/(μ S · cm⁻¹) was calculated at the end of each monitoring day using the procedure described by Richardson (2015), in which a known mass of salt was added to a measured volume of streamwater, and then samples of this solution were added incrementally to another measured volume of streamwater, with EC_T measured after each addition. CF_T was calculated as the slope of the linear regression line between the calculated mass concentration of salt and EC_T . Following calibration, stream discharge, $Q(m^3s^{-1})$, was calculated as:

$$Q = \frac{M}{CF_T \cdot A} \tag{2.2}$$

where M is the mass of the salt injected (kg), and A is the area under the time series of $(EC_T - EC_{BG})$ during the salt wave passage $(\mu S \cdot cm^{-1} \cdot s)$.

2.2.3 Digital camera imagery

Video of the water surface was recorded during each albedo measurement using a water-proof GoPro HDHERO2 digital camera. The camera was mounted facing downwards on the pole mount and was run continuously for the duration of each measurement (Figure 2.3). Video collected was used to provide imagery to refer to while processing and verifying albedo data as well as for the development of a proxy for pyranometer-measured albedo.

2.2.4 Reach characteristics

Surveys were conducted in June and August 2016 to determine the view factor, average bankfull channel width, and channel gradient of each site using a LTI Impulse 200 laser rangefinder and handheld clinometer. Average bankfull width was calculated as the average width of two transects of each stream and was obtained with horizontal rangefinder measurements. Gradient was determined by obtaining horizontal and vertical distance measurements with the rangefinder. The sky view factor (VF) was calculated from zenith angles measured at each site in eight directions (N, NE, E, etc.):

$$VF = \frac{\sum_{i=1}^{8} [1 - (\cos Z)^{2}]}{8}$$
 (2.3)

where Z is the angle between the zenith and the horizon (defined by topography or forest canopy) in each direction, measured with a clinometer.

2.3 Data analysis

2.3.1 Pyranometer calibration

Using the manufacturer's calibration sensitivities for each pyranometer, irradiance values from the CM3 pyranometer were typically 91 to 95% of the values recorded by the CM6B. There was no offset between pyranometers when both were covered and zeroed. This proportional offset was compensated for by calibrating the voltages reported by the CM3 pyranometer with those reported by the CM6B. At the conclusion of each trip to the field, pyranometers were run side by side for several hours. A linear model with no intercept was fitted between the CM3 raw voltage output and the CM6B irradiance. The recorded CM3 voltage was then multiplied by the model's slope to calculate the calibrated CM3 irradiance.

2.3.2 Albedo calculation

Following pyranometer calibration, albedo values were extracted from the pyranometer time series. A five-point moving window, corresponding to 25 seconds of measurement time, was used to calculate smoothed means and standard deviations of $K\downarrow$, time of measurement, and albedo (Figure 2.4). Stable measurements were isolated by removing periods between measurements, unstable measurements, and the leading and trailing edge of each measurement by removing points where $K\downarrow$ within each window exceeded a set standard deviation and slope. Albedo, measurement time, and $K\downarrow$ were calculated as the mean of the values for each measurement period. Further manual processing was performed in order to determine whether measured albedo values were physically reasonable by comparing them to field notes and the digital camera imagery. Unstable albedo measurements that were not removed by the filter were also discarded from the dataset. Lighting conditions and an estimate of the amount of surface aeration for each albedo measurement (i.e. minimal aeration versus highly aerated) were appended to the dataset from field notes.

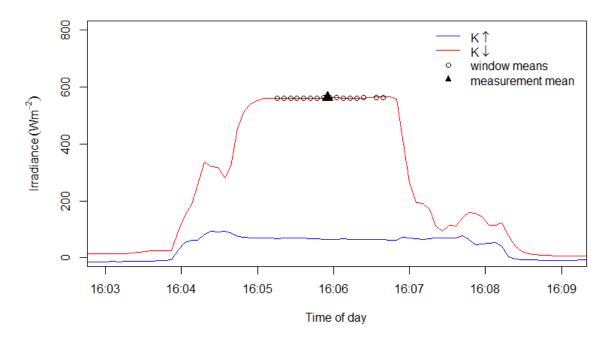


Figure 2.4: Sample albedo time series measurement. Hollow circles are centroids of each 5-point window within the measurement. The black triangle denotes the position of the mean $K \downarrow$ within the measurement.

2.3.3 Solar position

Albedo should vary with solar zenith angle (which, for a horizontal water surface, is also the angle of incidence) and with the fractions of direct and diffuse solar radiation. For simplicity, the atmospheric transmissivity, τ , was used as an index of these fractions (i.e., higher transmissivity indicates a higher fraction of direct radiation). Solar zenith angle, θ , was calculated following Iqbal (1983):

$$\theta = \cos^{-1}[\sin(\delta) \cdot \sin(\phi) + \cos(\delta) \cdot \cos(\omega)] \tag{2.4}$$

where δ is solar declination, ϕ is latitude at the measurement location, and ω is the hour angle. The declination was calculated based on a seven term Fourier expansion:

$$\delta = 0.0069 - 0.3999cos(\gamma) + 0.0703sin(\gamma) - 0.0068cos(2\gamma) + 0.0009sin(2\gamma) - 0.0027cos(3\gamma) + 0.0015sin(3\gamma)$$
 (2.5)

where γ is the day angle, $2\pi(d-1)/365$, where d is the calendar day (d=1 on Jan. 1). Hour angle was calculated as:

$$\omega = 0.2618(L_t - 12) \tag{2.6}$$

where L_t is local area time, calculated as:

$$L_t = T_d - DST + 4(\lambda_{standard} - \lambda)/60 + E_t \tag{2.7}$$

where λ is longitude, T_d is the local clock time, $\lambda_{standard}$ is a standard parallel of longitude (120°W for the region), and E_t is the equation of time, calculated with a five term Fourier expansion:

$$E_t = 229.18[0.000075 + 0.001868cos(\gamma) - 0.032077sin(\gamma) - 0.014615cos(2\gamma) - 0.04089sin(2\gamma)]/60$$
 (2.8)

Transmissivity was calculated as:

$$\tau = K \downarrow / [K_0 cos(i)] \tag{2.9}$$

where K_0 is the solar constant, taken here to be 1367 Wm⁻¹, and i is the solar incidence

angle, approximated here by the solar zenith angle. To simplify interpretation, further analysis was performed using the solar elevation angle, h, which is the complement of solar zenith angle.

2.3.4 Digital camera imagery

Still frames from the digital camera imagery were used to develop a proxy measure for aeration. Still frames were extracted from the digital camera video recorded between June and September at Rutherford Creek. One video frame was extracted per albedo measurement taken at each site. Each frame was converted into a 3-dimensional matrix representing the image's red, green, and blue components, where the number of columns and rows in each matrix channel was equal to the image's height and width in pixels. The coefficient of variation (CV) of the pixels in each colour channel was calculated and averaged between all three colours as a measure of the total variability within the image. Nonlinear regression was used to fit a model relating albedo to CV to assess its value as a proxy.

2.3.5 Statistical modelling

Albedo measurements were stratified into a "whitewater" set for measurements that took place over visibly aerated flow and a separate "flatwater" subset for the rest. A separate subset was created for measurements taking place at a hydraulic jump on Rutherford Creek to look explicitly into the relation between albedo and discharge. Discharge measurements were also made on Cayoosh Creek and North Creek, but neither stream had an adequate number of discharge measurements associated with albedo at a specific location on the stream to perform a valid statistical analysis. Since albedo measurements were not always taken at the same time as discharge and suspended sediment, Q and SSC values were assigned to each albedo measurement using cubic spline interpolation through the time series of those variables for each day. Splines were generated according to Forsythe et al. (1977); in this approach end conditions were determined by fitting an exact cubic through the four points on each end of the data, thus minimizing the spline energy subject to constraints imposed by the end conditions

Albedo was plotted individually against solar elevation angle, transmissivity, suspended sediment concentration, and discharge to determine the forms of the relation. Predictors were transformed if, during the initial stages of model fitting, it appeared necessary to linearize the relationship and to improve predictive ability. A categorical representation of SSC was used in which low concentrations were assigned a value of 0,

and higher concentrations were assigned a value of 1. The split between low and high concentrations was defined at 30 mg/L for the flatwater subset and at 15 mg/L for the whitewater subset. Additionally, $\sin h$ was used in order to linearize the relationship between solar altitude and albedo. Transformed variables were used to fit models for albedo using multiple regression separately for the flatwater and whitewater subsets. A set of candidate models was constructed for every possible combination of selected variables and their interactions.

Candidate models were initially evaluated on the basis of coefficient values. Models with coefficients that were not physically reasonable were immediately removed from consideration. The predictive ability of remaining models was compared with the Akaike Information Criterion (AIC) for the model fitted to the entire subset. A modified version of the metric, AIC_c , was used, since the number of observations was relatively small compared to the number of predictor variables, and since AIC_c imposes a greater penalty for extra predictors (Symonds and Moussalli, 2011). Candidate models with ΔAIC_c of less than 2 for each subset were evaluated further using leave-one-out cross validation. Models were cross-validated on a stream-by-stream basis to avoid overfitting and to produce a more rigorous test of the model's predictive ability when applied to new sites.

Recursive partitioning was used to categorize variability in the dataset and identify interactions between predictor variables. The resultant regression trees classified subsets of the albedo dataset based on how predictor variables reduced variance in each subset of albedo. Regression trees were pruned using a complexity parameter (c_p) of 0.04. Results of recursive partitioning were used to draw inferences regarding the relative importance of each predictor variable and the structure of the relationship between albedo and predictors.

Chapter 3

Results

3.1 Overview of the study period

Monthly mean air temperatures measured near Pemberton, BC, from 1969-2014 and during 2015 are displayed in Figure 3.1. The majority of the study period was characterized by air temperatures well above monthly averages. The mean monthly air temperature was 3.7 °C above normal during May and June and 2.4 °C above average in July. Temperatures toward the end of the field season were closer to long-term averages. The mean monthly air temperature was 1.0 °C above average in August and 0.4 °C below average in September.

Historical monthly mean total precipitation from 1969-2014 and 2015 monthly total precipitation are displayed in Figure 3.2. Monthly precipitation was below the long term average during much of the spring of 2015 and for the majority of the field season. Less than half of average precipitation fell during April, May, and July 2015. May 2015 was particularly dry; 9.6% of monthly average precipitation occurred. In contrast, August and September 2015 were wet months, receiving 263% and 176% of average total monthly precipitation respectively.

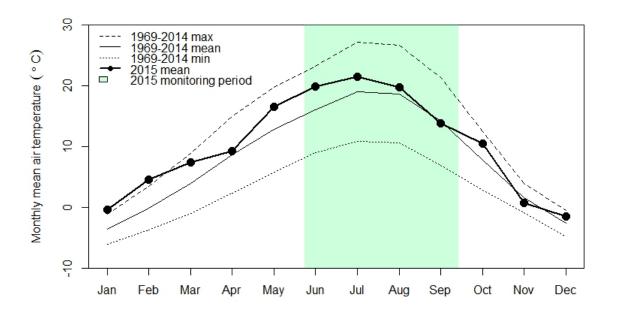


Figure 3.1: Historical maximum, mean, and minimum monthly air temperatures and 2015 monthly mean air temperature measured near Pemberton. The 2015 field season is highlighted in blue. Data from 1969 - 1984 are sourced from Environment Canada station 1086083 (Pemberton BCFS), with years 1984 - 2015 sourced from a nearby station, 1086082 (Pemberton Airport CS).

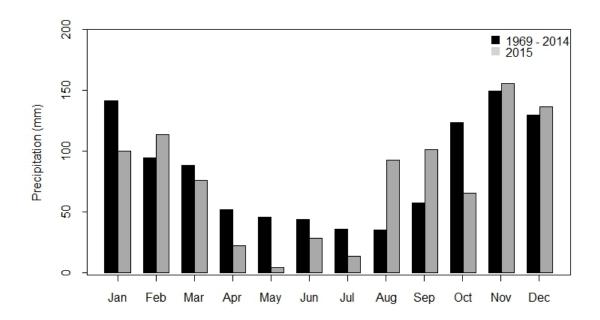


Figure 3.2: Historical mean monthly total precipitation and 2015 monthly total precipitation measured near Pemberton. Data from 1969–1984 are sourced from Environment Canada station 1086083 (Pemberton BCFS), with years 1984 - 2015 sourced from station 1086082 (Pemberton Airport CS).

Peak summer flow on the Lillooet River occurred during the beginning of the 2015 field season (Figure 3.3). Peak summer flows occurred during late May and early June, well before the mid-July average. The early peak is likely attributable to meltwater generation resulting from higher than average air temperatures during the late spring and early summer. Rainfall was below average during the same period, minimizing precipitation contributions to streamflow. Daily mean streamflow was above average for much of July, and returned to near-normal conditions in late July and August as more precipitation fell and temperatures returned to long-term averages.

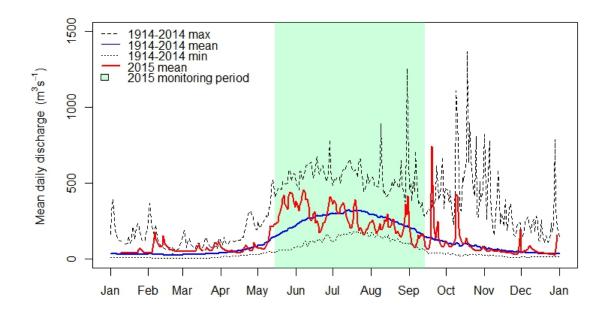


Figure 3.3: Historical maximum, mean, and minimum daily streamflow and 2015 mean flow at the Lillooet River 3 km northwest of the Lower Lillooet reach (Water Survey of Canada station 08MG005 Lillooet River near Pemberton)

3.2 Pyranometer calibration

The relation between CM6B irradiance and CM3 output voltage used to calculate CM3 irradiance is shown in Figure 3.4. Prior to calibration, percent difference between daily CM3 and CM6B irradiance during parallel runs differed from between 4.7% and 18.7%. Following calibration, percent difference between pyranometers was 0.7% to 14.0% (Table 3.4). Standard error of the estimate was between 4.3 and 18.7 Wm⁻². The largest differences in irradiance following calibration occurred on days when shading from clouds

or buildings covered pyranometers during the calibration procedure, creating periods in which one pyranometer would be shaded while the other was exposed to direct solar radiation. On July 21 and August 3, shadows from nearby buildings covered the pyranometers after several hours of recording in direct solar radiation.

Table 3.1: Pyranometer calibration results. Percent differences are between CM3 and CM6B irradiance. $S_e = \text{standard error of the estimate}$.

calibration date	% difference calibrated	slope (Wm^{-2}/mV)	$S_e \text{ (Wm}^{-2})$
31 May	-0.67	55.32	7.2
18 June	-0.94	56.75	4.25
21 July	-4.33	57.2	9.73
3 August	-14.0	56.15	13.91
24 August	-1.09	56.07	12.73
21 September	-5.6	56.48	18.66

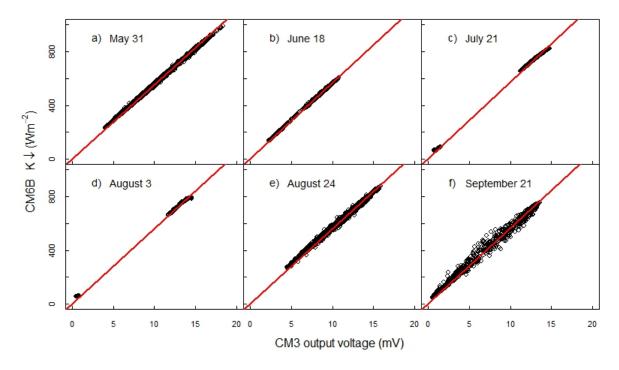


Figure 3.4: Relation between uncalibrated CM3 output voltage and CM6B irradiance during calibration. Red lines are the regression lines for each relation used to convert the CM3 voltage to irradiance

The period of time in which the pyranometers were not exposed to identical light conditions was removed, producing the discontinuities in panels 3.4c and 3.4d (Figure 3.4). Percent difference following calibration was 4.3% on July 21 and 14.0% on August

3. Calibration on September 21 occurred during a period of variable clouds that induced scatter in the relation as shadows moved over the pyranometers, again subjecting them to non-identical irradiances (Figure 3.4f). On days when shading was minimal, calibrated CM3 and CM6B irradiance differed by 1.1% or less.

Variability in the slope of the regression line was minimal despite differences in light conditions during calibration and relatively large differences in calibrated values on August 3 and September 21. Regression slopes ranged between 55.3 and 57.2 Wm⁻²/mV. The percent difference between the maximum and minimum vales was 3.3%. Additionally, no trend in the slope of the regression was evident over the course of the monitoring season, indicating that the calibration process produced consistent calibrated irradiance values and that any systematic drift was minimal.

3.3 Analysis of digital camera images

Digital images were captured at Rutherford Creek during trips to the site between June and September at three locations along the stream surface that encompassed a gradient of visible aeration (Figure 3.5, panels a - c). Measurements at location (a) were made over slow moving flow upstream of a rock step. Measurements at (b) and (c) were downstream of the rock step, where (c) was immediately in the lee of the boulder over layers of foam on the water surface, and b) was approximately 2 m downstream.

Linear regressions fitted between albedo and CV for each subset were not significant. Plotted together, the albedo-CV relation appears consistent with a logistic curve, although with considerable scatter. Model residuals had a standard deviation of 0.041 and Nash-Sutcliffe efficiency of 0.28.

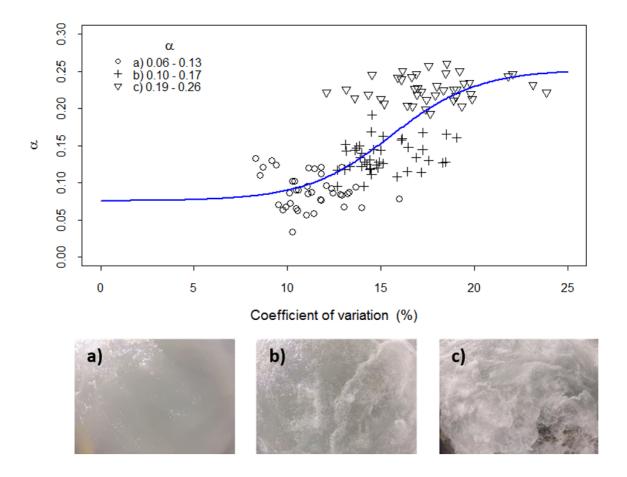


Figure 3.5: Upper panel shows the relation between measured albedo and the coefficient of variation of pixel RGB values at Rutherford Creek based on measurements at three locations denoted a, b and c. The lower panels provide an example image for each site.

3.4 Exploratory analysis of albedo variability

In this section, the relation between albedo and several hypothesized controlling variables (atmospheric emissivity, solar elevation angle, suspended sediment concentration and discharge) are examined. Sections 3.4.1 to 3.4.4, below, present exploratory analyses using bivariate graphs with stratification, and section 3.4.5 examines the potentially interacting effect of all candidate predictor variables using recursive partitioning. The results of these exploratory analyses are then used to define the form of a formal predictive model in section 3.5.

3.4.1 Relation with atmospheric transmissivity

The relation between albedo and atmospheric transmissivity is displayed in Figure 3.6. Albedo exhibited a slight positive correlation with transmissivity for both subsets. A shift in the mean and variance of albedo is apparent at around $\tau=0.6$. Mean albedo was decreased by 0.03 within the flatwater subset and 0.02 within the whitewater subset when $\tau<0.6$. Standard deviation from the mean within each subset decreased 0.006 for flatwater and 0.009 for whitewater over the range of measurements.

Compared to a subjective classification of the dominant insolation condition (direct vs diffuse), defining diffuse as dominant for $\tau < 0.6$ and direct for $\tau \geq 0.6$ matched observed lighting conditions for 97% of albedo measurements. Since sampling typically took place during fair weather, the majority of albedo measurements were taken in direct lighting conditions in both subsets. A total of 66 of 212 flatwater measurements and 17 of 91 whitewater measurements were measured when $\tau > 0.6$.

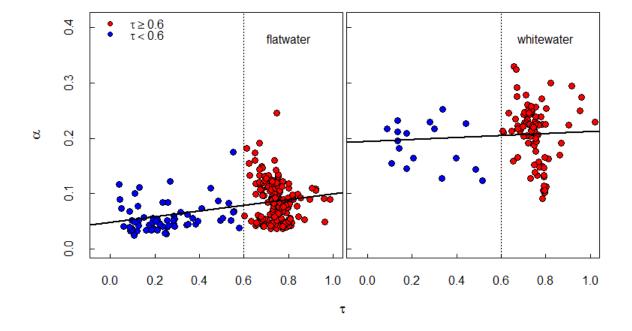


Figure 3.6: Albedo as a function of atmospheric transmissivity for flatwater (left panel) and whitewater (right panel) sites. Solid black lines are regression lines for each subset. Vertical dotted lines at $\tau = 0.6$ indicate an inferred split between light conditions dominated by diffuse ($\tau < 0.6$) and direct insolation ($\tau \geq 0.6$), respectively.

3.4.2 Relation with solar elevation angle

Stream surface albedo exhibited a broad range of variability associated with solar elevation angle (Table 3.2; Figure 3.7). Flatwater measurements ranged from 0.036 to 0.246 in direct light conditions, with a mean of 0.057. Albedo was enhanced by aeration at points on the stream with visible whitewater, and more scatter was present in the relation. Albedo ranged from 0.09 to 0.329 in direct light, with a mean of 0.189. Albedo exhibited a negative response with solar elevation angle in direct light, particularly for elevation angles below 25° during flatwater measurements. Albedo decreased within both subsets during diffuse lighting conditions when the response to solar elevation was suppressed. Differences in albedo during direct and diffuse lighting conditions were most pronounced at low solar elevation angles.

Flatwater albedo in diffuse light ranged from 0.025 to 0.175 in flatwater and from 0.124 to 0.188 in whitewater. The slopes of the relation between albedo and solar elevation were significant for all subsets other than whitewater albedo measurements in diffuse light, which consists of 17 measurements. Measurements over whitewater exhibited more scatter than flatwater measurements. More scatter was inherent in the relation for direct lighting conditions compared to diffuse lighting conditions within both subsets, as evidenced by higher standard deviations.

Table 3.2: Summary of albedo values for flatwater and whitewater subsets and relations with solar elevation angle, stratified by transmissivity. Slope refers to the slope of the relation between albedo and solar elevation angle, n is the number of points in each subset, and p is the significance level for the regression.

	au	Min	Mean	Max	Std. Dev.	Slope	p	n
Flatwater	≥ 0.6	0.036	0.088	0.246	0.033	-0.002	2e-16	212
	< 0.6	0.025	0.057	0.175	0.027	-0.0009	0.0003	66
Whitewater	≥ 0.6	0.091	0.210	0.329	0.049	-0.003	1.07e-9	98
	< 0.6	0.124	0.188	0.253	0.040	-0.0003	0.645	17

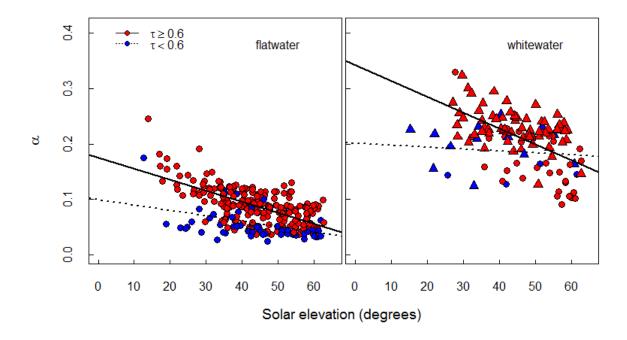


Figure 3.7: Albedo as a function of solar elevation angle. Solid and dashed lines are best-fit regressions for direct- and diffuse-dominated conditions, respectively.

3.4.3 Relation with suspended sediment

Suspended sediment concentrations and associated flatwater albedo and transmissivity values for each reach are listed in Table 3.3. Minimum and maximum concentrations measured during the field season were 0.83 mg/L, measured at Cayoosh Creek, and 746 mg/L, measured on the Lower Lillooet River. The sites had mean albedo values of 0.05 and 0.10 respectively. The albedo-SSC relation is shown on log-axes for the complete flatwater and whitewater subsets in Figure 3.8. The relation is plotted with linear x-axes in Figure 3.9. Albedo had a strong positive relation with SSC at low concentrations that flattened at higher concentrations. Transmissivity had a weak influence on the relation for the flatwater subset. The slope of the relation for flatwater was 0.026 for measurements in direct light, compared to 0.020 for diffuse conditions. The difference was greater for the whitewater measurements. Slopes of the regression were 0.047 and 0.026 for direct and diffuse conditions respectively. However, the slope of the regression was not significant for diffuse measurements in either the flatwater or the whitewater subset.

Table 3.3: Minumum, mean, and maximum *SSC* values, mean flatwater albedo, and mean transmissivity observed for each reach. Albedo measurements over aerated flow were excluded from the calculation of mean albedo.

Reach	$\min SSC$	mean SSC	$\max SSC$	mean α	mean τ
	(mg/L)	(mg/L)	(mg/L)		
Birkenhead R.	2.37	15.1	182	0.050	0.491
Cayoosh Cr.	0.83	2.50	7.23	0.054	0.727
Lillooet R. lower	173	405	747	0.099	0.713
Lillooet R upper	208	375	677	0.114	0.710
Miller Cr.	13.1	26.2	41.7	0.047	0.335
North Cr.	24.9	35.4	43.2	0.062	0.611
Rubble Cr.	1.63	117	650	0.087	0.628
Rutherford Cr.	3.25	22.8	40.1	0.088	0.693
Soo R.	15.7	75.5	166	0.105	0.692

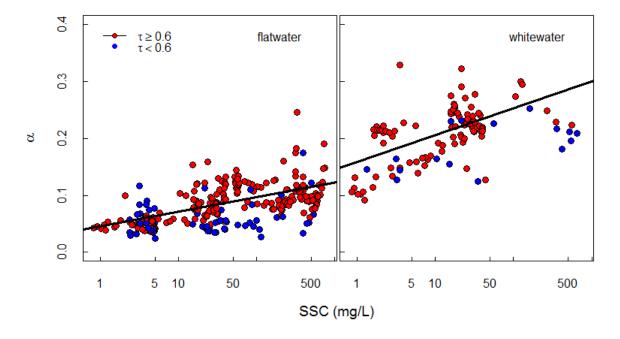


Figure 3.8: The relation between albedo and SSC. Note that the x-axis is plotted on a logarithmic scale. Solid black regression lines are for $\tau \geq 0.6$.

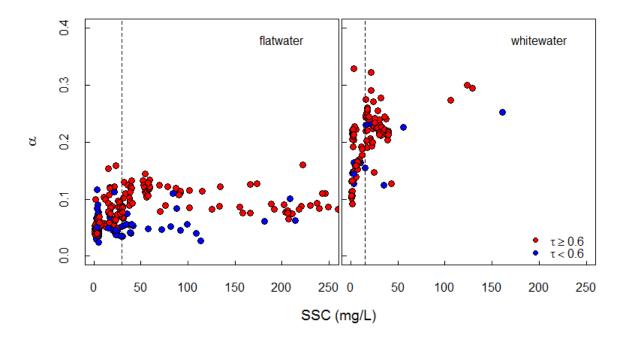


Figure 3.9: The relation between albedo and SSC. Note that the x-axis is on a linear scale and truncated at SSC = 250 mg/L. Vertical lines are positioned at 30 mg/L for the left panel and 15 mg/L on right panel to highlight differences in the form of the relation at low and high SSC.

3.4.4 Relation with discharge and aeration

Albedo exhibited a weak positive relation with discharge at the hydraulic jump on Rutherford Creek (Figure 3.10), although the slope of the regression was not significant (slope = 0.018, p = 0.127). The relation was stratified by solar elevation angle (h) and SSC to assess potential confounding effects. Both high and low SSC measurements were present across the range of measured flows. However, a majority of measurements taken during high flows ($Q > 2.4 \, \mathrm{m}^3 \mathrm{s}^{-1}$) were taken at low solar elevation angles ($h < 40^\circ$). The influence of atmospheric transmissivity was minimal, since only 2 of the 54 albedo measurements at the hydraulic jump were measured during diffuse lighting conditions.

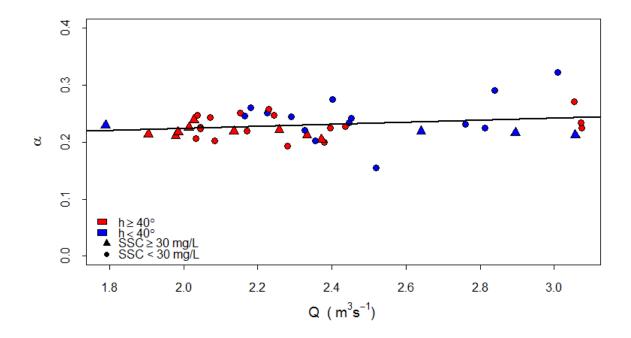


Figure 3.10: Albedo as a function of discharge at Rutherford Creek, stratified by transmissivity and suspended sediment concentration.

3.4.5 Recursive partitioning

Regression tree fits to the flatwater and whitewater albedo subsets are displayed in Figures 3.11 and 3.12. For both subsets, SSC was the strongest predictor of albedo. Initial splits occurred at SSC = 30.9 mg/L for flatwater measurements and at SSC = 15.4 mg/L for whitewater measurements. For flatwater, subsequent splits were made at $h = 37.52^{\circ}$ and $\tau = 0.52$. For whitewater, the subsequent split occurred at SSC = 1.61 mg/L. No additional splits occurred for whitewater measurements with values of SSC greater than 15.44 mg/L using $c_p = 0.4$.

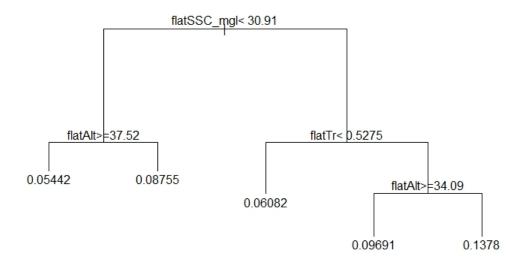


Figure 3.11: Regression tree fit to the flatwater subset. Mean albedo values for the final classes are indicated on the end of each leaf. Variable names in the figure correspond to predictor variables as follows: flatSSC_ mgl = SSC (mg/L), flatAlt = h (degrees), flatTr = τ .

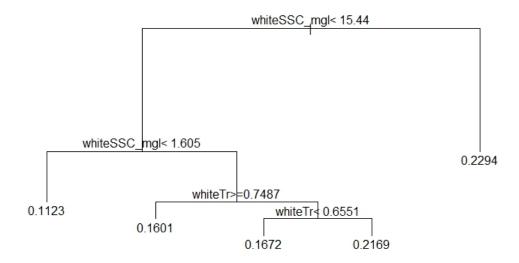


Figure 3.12: Regression tree fit to the whitewater albedo subset. Variable names in the figure correspond to predictor variables as follows: whiteSSC₋ mgl = SSC (mg/L), whiteAlt = h (degrees), whiteTr = τ .

3.5 Statistical modelling

3.5.1 Model fitting and cross validation

Tables 3.4 and 3.5 summarize results of the model fitting using the categorical SSC representation. For both flatwater and whitewater subsets, many models, including those with the lowest ΔAIC_c values, did not have physically reasonable coefficients. Within the flatwater subset, the two models with the highest predictive ability had SSC terms with a negative coefficient for both models, which is not physically realistic. Of the flatwater models with physically reasonable coefficients, models 3 and 4 had the greatest predictive ability. Both explained 60% of the variance prior to cross-validation. Models 5 and 6 were the only candidate models within the whitewater subset that had physically reasonable coefficients. Model 6 had the highest predictive ability, accounting for 43% of the variance in albedo.

The model fitting process was repeated using $\ln SSC$ (Table 3.6; Table 3.7). Model 11 has the lowest AIC_c value of all models within the flatwater subset, and accounts for 62% of variance in albedo. Additionally, all coefficients are physically reasonable for the model. There was also support for model 10, as evidenced by ΔAIC_c of 1.875 and plausible coefficients. Within the whitewater subset, only models 12 and 13 had reasonable coefficients.

Model R^2 and RMSE following the cross-validation process are displayed in Table 3.8. Within the flatwater subset, models using $\ln SSC$ had higher predictive ability than models that included categorical SSC. However, differences in predictive ability in the flatwater candidate models using the same SSC representation were small. Cross validated R^2 and RMSE each differ by less than 0.001 between the two flatwater categorical SSC models. The difference was slightly larger for the flatwater $\ln SSC$ models; R^2 differed by 0.005. Whitewater models had higher predictive ability using categorical SSC than with $\ln SSC$. Residual distributions varied little between models built for the same subset of albedo and using the same SSC representation, so models were selected on the basis of predictive ability. Since models 3 and 4 were nearly identical in their predictive ability, model 3 was selected for its simplicity. Observed versus predicted values of albedo using the selected models are displayed in Figure 3.13.

Table 3.4: Summary of model fitting for the flatwater subset. SSC is represented categorically with a threshold at SSC = 30 mg/L. Bold values indicate models where $\Delta AIC_c < 2$ compared to the strongest model with physically reasonable coefficients. $S_e = \text{standard error of the estimate}$. Only models with physically reasonable coefficients are displayed in this table and in Tables 3.5-3.7.

	$\Delta { m AIC}_c$	$Adj. R^2$	S_e	b_0	$\sin h$	SSC	au	$\sin h \cdot SSC$	$\sin h \cdot \tau$	$SSC \cdot \tau$
1	16.724	0.574	0.022	0.121	-0.119	0.026	0.043			
2	18.716	0.572	0.022	0.119	-0.115	0.030	0.043	-0.006		
3	0.000	0.600	0.021	0.043	-0.009	0.026	0.173		-0.182	
4	1.915	0.599	0.021	0.045	-0.012	0.020	0.174	0.008	-0.185	

Table 3.5: Summary of model fitting for the whitewater subset using the categorical representation of SSC with a threshold of SSC = 15 mg/L.

	$\Delta \mathrm{AIC}_c$	$Adj. R^2$	S_e	b_0	$\sin h$	SSC	au	$\sin h \cdot SSC$	$\sin h \cdot \tau$	$SSC \cdot \tau$
5	0.663	0.419	0.036	0.218	-0.117	0.049	0.058			
6	0.000	0.428	0.036	0.256	-0.119	0.001	0.006			0.069

Table 3.6: Summary of model fitting for the flatwater subset using ln *SSC* as a predictor variable.

	$\Delta { m AIC}_c$	Adj. R ²	S_e	b_0	$\sin h$	$\ln SSC$	au	$\sin h \cdot \ln SSC$	$\sin h \cdot \tau$	$\ln \mathit{SSC} \cdot \tau$
7	23.545	0.581	0.022	0.156	-0.114	0.007	0.042			
8	16.647	0.592	0.022	0.187	-0.158	0.018	0.041	-0.015		
9	13.227	0.597	0.022	0.092	-0.025	0.007	0.148		-0.148	
10	1.875	0.615	0.021	0.154	-0.165	0.010	0.096	-0.017		0.014
11	0.000	0.619	0.021	0.117	-0.106	0.009	0.150	-0.014	-0.086	0.012

Table 3.7: Summary of model fitting for the whitewater subset using $\ln SSC$ as a predictor variable.

	$\Delta \mathrm{AIC}_c$	Adj. \mathbb{R}^2	S_e	b_0	$\sin h$	$\ln SSC$	au	$\sin h \cdot \ln SSC \sin h \cdot \tau \ln SSC \cdot \tau$
12	1.686	0.352	0.038	0.299	-0.121	0.013	0.073	
13	0.000	0.368	0.038	0.264	-0.115	0.002	0.125	0.017

Table 3.8: Cross-validated R² and RMSE for models selected during the initial stages of model fitting. FW and WW indicate whether the model is for flatwater or whitewater conditions. Bold indicates final selected models.

		Model	\mathbb{R}^2	RMSE
3	\mathbf{FW}	$\sin + SSC + \tau + (\sin h \cdot \tau)$	0.597	0.023
4	FW	$\sin h + SSC + \tau + (\sin h \cdot SSC) + (\sin h \cdot \tau)$	0.597	0.024
5	WW	$\sin h + SSC + \tau$	0.413	0.061
6	$\mathbf{W}\mathbf{W}$	$\sin h + SSC + \tau + (SSC \cdot \tau)$	0.422	0.061
10	FW	$\sin h + \ln SSC + \tau + (\sin h \cdot \ln SSC) + (\ln SSC \cdot \tau)$	0.615	0.023
11	\mathbf{FW}	$\sin h + \ln SSC + \tau + (\sin h \cdot \ln SSC) + (\sin h \cdot \tau) + (\ln SSC \cdot \tau)$	0.620	0.023
12	WW	$\sin h + \ln SSC + \tau$	0.360	0.064
13	$\mathbf{W}\mathbf{W}$	$\sin h + \ln SSC + \tau + (\ln SSC \cdot \tau)$	0.373	0.065

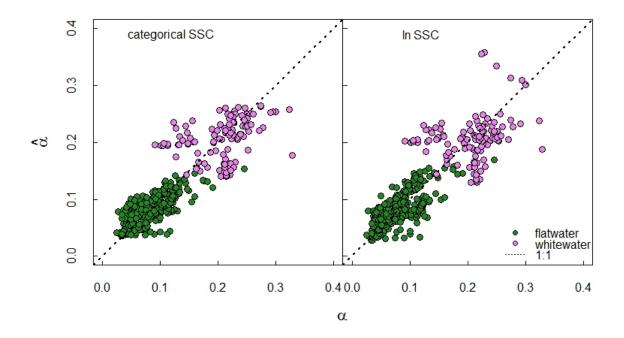


Figure 3.13: Cross-validated predicted albedo values versus observed albedo for the flatwater and whitewater subsets. The left-hand panel shows results with *SSC* represented as a binary variable (low/high) and the right-hand panel shows results with ln *SSC* as a predictor variable

Chapter 4

Discussion

4.1 Analysis of albedo variability

4.1.1 Solar angle and transmissivity

Albedo exhibited large diurnal swings in magnitude during clear sky conditions. Differences between maximum and minimum albedo values observed in direct lighting conditions averaged by reach were 0.12 for both flatwater and whitewater locations. The maximum flatwater albedo value measured on the lower Lillooet reach was 0.25, measured at a solar elevation angle of 13.9°. Measured values of albedo at given solar elevation angles were similar to those reported in ocean and lake surface. For example, Payne (1972) reported a diurnal pattern in albedo that was similar in magnitude to those in this study, including comparable values at low solar elevation angles.

The latitude and high relief of the study area restricted the range of angles that direct solar radiation could be measured from. Horizon angles throughout the study area averaged 25° in the west and southwest directions, and were consistently above 10°, imposing a lower limit on the range of elevation angles. The highest elevation angle possible for the sites (at solar noon on the summer solstice) is 63.1°, and the highest elevation angle during an albedo measurement was 62.8°. As a result of these limits, some patterns of variability were not observed that may affect streams at lower latitudes or in lowland regions. For example, albedo values approaching unity have been observed on calm surfaces as the sun approaches 0° at sunrise or sunset

The interaction between transmissivity and solar elevation angle matched the expected pattern of variability described by Katsaros et al. (1985) and Oke (1987) for flatwater conditions. Diffuse lighting conditions (low transmissivity) were associated with

reduced surface albedo across the range of calculated solar elevation angles. The largest reduction of albedo during diffuse light conditions occurred at low elevation angles when the sun was near the horizon. However, diffuse lighting conditions appeared to have minimal influence on whitewater albedo at high elevation angles. The apparent lack of response may reflect the fact that aeration would create a broad range of incidence angles, even for direct solar radiation, in contrast to flatwater. However, the apparent lack of response could also result from suspended sediment bias. SSC measurements corresponding to whitewater albedo measurements taken at solar elevations greater than 45° in direct light conditions averaged 22 mg/L, whereas average SSC for whitewater albedo in the same conditions was 81 mg/L. The suppressed response of albedo to solar altitude under diffuse lighting conditions also explains the reduction in variance in albedo, since values are reduced the most at low solar elevation angles. Diffuse lighting conditions should create the greatest reduction in albedo at low solar elevation angles when albedo values are highest during clear-sky conditions, which would reduce the amount of variance in the relation between albedo and elevation angle.

4.1.2 Discharge and aeration

A primary objective of this study was to quantify the influence of aeration on stream surface albedo. At Rutherford Creek, albedo measurements were taken at three locations that encompassed a range of visible levels of aeration. Average albedo values at the three sites were 0.09, 0.13, and 0.22, respectively. Subsequent albedo measurements taken at calm and aerated portions of the stream surface several metres apart from each other on Rutherford Creek and Rubble Creek differed by 0.14, on average. These findings indicate that, controlling for the effects of solar elevation angle and transmissivity, aeration significantly enhances albedo.

The relation between albedo and discharge was weak. The weak response of stream surface albedo to aeration with increasing flow can likely be attributed in part to the height of the pyranometers above the stream surface during measurements as well as the range of flow conditions experienced at Rutherford Creek during the field season. Measured flows during sampling campaigns on Rutherford Creek only ranged between 1.8 and 3.1 m³s⁻¹, reflecting the diversion of flow around the sampling reach for a run-of-river hydroelectric facility. Albedo measurements at the hydraulic jump were taken at a height of approximately 0.5 m in order to minimize the pyranometer's view of boulders and to consistently view aerated portions of the surface, as opposed to viewing a combination of visibly aerated and calm portions of the water surface that would vary with discharge. In contrast, Richards and Moore (2011) measured albedo over

a broader range of flows, ranging from approximately 0.5 to 7.0 m³s⁻¹. Furthermore, their downward-facing pyranometer was at a greater height above the surface than in the current study (1 m at low flow), so it sampled a larger area with varying degrees of aeration, which in turn varied with discharge, contributing to a stronger relation between albedo and discharge.

Reflectance increases in visible wavelengths as the thickness of foam increases (Whitlock et al., 1982), suggesting that increasingly thick layers of foam should increase albedo after the entirety of the pyranometer's field of view is covered by whitewater. Despite whitewater covering almost all of the pyranometer's field of view during whitewater measurements at Rutherford Creek, the highest albedo value measured was 0.32, which is below the maximum value of 0.4 measured by Richards and Moore (2011), and 0.5 measured by Whitlock et al. (1982), suggesting that albedo could continue to increase with aeration at higher discharges at the hydraulic jump. Highly aerated flow over cascades, where albedo values were likely to be higher than 0.32, were present at Rubble Creek; however, the most vigorously aerated portions of flow were inaccessible and thus were not sampled.

One issue that is difficult to address is the location-specific relation between aeration and discharge. For instance, the rate at which flow becomes visibly aerated with increasing discharge may differ between riffles and hydraulic jumps downstream of rock steps. Additionally, stream surface albedo varies widely on a fine spatial scale in channels with complex morphologies. Therefore, it may be most effective to determine the relationship between albedo and aeration in terms of areal increases to visible whitewater at higher flows to account for aeration effects.

4.1.3 Suspended sediment

Stream surface albedo varied with suspended sediment concentration (Table 3.3). Albedo in streams with low suspended sediment concentrations (SSC < 50 mg/L) averaged 0.06, which is comparable with the values found in studies on low-gradient streams with low SSC (e.g Evans et al., 1998; Leach and Moore, 2010). Other studies have reported average daily albedo values as low as 0.03 (Caissie et al., 2007; Benyahya et al., 2012), which were lower than almost all clear-sky albedo values measured in this study. Only three measured albedo values in this study were less than 0.03; all three were measured under overcast conditions.

Measured albedo values for streams with higher suspended sediment concentration were similar to values found in past work from high-turbidity settings. Mean albedo values for streams with SSC greater than 50 mg/L averaged 0.10, which is consistent

with the values reported by Chikita et al. (2010) on a highly turbid proglacial river where SSC typically exceeded 200 mg/L. Measurements from Lillooet River were nearly identical to those found in previous work by Knudson (2012) on the same river. Nielson et al. (2009) also reported an increase of 0.03 to 0.07 in albedo with turbidity. Average flatwater albedo measured in this study with corresponding SSC > 50 mg/L was 0.04 higher than measurements with SSC < 50 mg/L.

Albedo increased sharply with SSC at low concentrations and flattened at high concentrations for both flatwater and whitewater conditions. This nonlinear dependence of albedo on SSC is not surprising; a similar relation was observed by Han (1997) within visible wavelengths in a laboratory setting. The strong positive relation between albedo and SSC visibly began to flatten as sediment concentrations approached 30 mg/L in flatwater and 15 mg/L in whitewater. Consistent with these visual observations, primary splits in the recursive partitioning analysis were at 30.91 mg/L for flatwater and 15.44 mg/L for whitewater.

The saturation effect in the relation may be explained by enhancement of albedo by backscatter that would decrease at higher concentrations of suspended sediment (Nunez et al., 1972; Katsaros et al., 1985), since backscatter has been reported to be higher in clear water than highly turbid water (Jerlov, 1968).

4.2 Model performance

4.2.1 Model selection and testing

Models fit for flatwater albedo had greater predictive ability than those for whitewater conditions. The weaker predictive ability of the whitewater models reflects the increased scatter in the relation brought on by aeration that was not accounted for by any terms in the model. Surface roughness at low solar elevation angles at aerated locations may have also contributed to scatter (Oke, 1987), particularly at hydraulic jumps where albedo tended to be largest in magnitude.

The majority of the models considered during the initial stages of model fitting did not have reasonable coefficients and were thus rejected. Considering the cross-validation performance and the physical reasonableness of the model coefficients, three models are recommended. Two flatwater models, models 3 and 11, were selected, using each representation of SSC (categorical and continuous), as well as one whitewater model (model 6) using the categorical SSC representation. For flatwater, model 3 (continuous SSC) slightly outperformed model 11 (categorical SSC). However, the categorical representa-

tion is useful because the model can be used even in the absence of suspended sediment data for streams that can visibly be classed as turbid. Model 6 had greater predictive ability using a categorical SSC term than model 13, which used continuous SSC as a predictor. Moreover, model 6 requires less input data.

4.2.2 Model scaling

The models developed here address variability in albedo with respect to the governing physical processes, but are based on measurements from isolated points on the water surface. As demonstrated at Rubble Creek, Cayoosh Creek, and Rutherford Creek, the value of albedo can vary widely on a scale of metres. Measurements from a single point or several points on the stream surface do not necessarily represent the entire stream surface, since variability in albedo is continuous both temporally and spatially across the stream surface.

Spatial variability could be addressed to some extent by sampling albedo at a greater number of points along the stream surface and calculating an average value for the reach in question. Temporal variability due to solar elevation angle is already accounted for by the model. However, stream surface shading derived from vegetation, topography, streambanks, and cloud cover varies both spatially and temporally, influencing the fractions of direct and diffuse solar radiation (and thus the albedo). Future work should explore methods of upscaling albedo measurements to represent the full stream surface and investigate the effectiveness of point measures compared to a more complete whole-surface representation of albedo.

4.3 Analysis of digital camera images

The magnitude of scatter in the relation between albedo and the coefficient of variation within the photographs was comparable in proportion to the measured albedo values, limiting the utility of the relation as a predictor of albedo. However, the form of the relation between albedo and CV is reasonable. The fit of the observations to a logistic function supports the assertion that albedo increases with CV as the surface becomes more visibly aerated, and that the relation should flatten at high amounts of aeration as images become increasingly white as they are saturated with light-coloured pixels.

Much of the noise in the relation may be inherent to the changing appearance of the water surface from moment to moment. Flow crossing beneath the camera may not have the same appearance and CV from second to second, particularly over rock- or log-steps or cascades where localized water velocity is high. Further, solar elevation angle, atmospheric transmissivity, and SSC influence albedo independently from aeration, thus representing additional confounding influences and sources of scatter.

Chapter 5

Conclusion

5.1 Key findings

Due to its dependence on the incidence angle for direct solar radiation, albedo exhibited a strong diurnal cycle in clear weather conditions that is consistent with patterns of variability reported in ocean and lake studies (Nunez et al., 1972; Payne, 1972; Oke, 1987). Albedo values measured in conditions dominated by direct radiation ranged from 0.04 to 0.25 in flatwater and 0.09 to 0.33 in whitewater, so characterizing stream albedo using individual albedo measurements may not be appropriate, especially in streams that are exposed to direct solar radiation at a range of solar elevation angles. Albedo tended to decrease with increasing diffuse radiation, especially at low solar angles, consistent with optical theory (Katsaros et al., 1985; Oke, 1987).

Albedo was enhanced at sites with visible whitewater: at Rutherford Creek, albedo averaged 0.09 over calm surfaces and 0.22 over aerated surfaces. The observed weak response of albedo to increasing discharge and aeration was potentially limited by the narrow range of flows that were sampled during the field season. Also, it is likely that albedo exhibits a stronger response to discharge when averaged over larger areas of the stream surface, as found by Richards and Moore (2011).

Albedo increased sharply with SSC at low concentrations and then levelled out at higher concentrations. Recursive partitioning analysis of the albedo-SSC relation suggested thresholds of 30 mg/L in flatwater and 15 mg/L over flatwater. Compared to low SSC conditions, average values of albedo were enhanced by 0.04 for $SSC \geq 30$ mg/L over flatwater, and by 0.06 for $SSC \geq 15$ mg/L over whitewater.

Predictive models were fit separately for flatwater and whitewater using regression analysis, with candidate predictors including the sine of the solar elevation angle, transmissivity and suspended sediment concentration, and their interactions. Candidate models were tested through cross-validation between study reaches, and models with physically unrealistic coefficients were rejected. For flatwater, use of $\ln SSC$ as a predictor yielded the highest predictive capability; predictive ability decreased slightly using a categorical representation of SSC. However, the model incorporating SSC as a categorical variable (low/high) offers the advantage of allowing the user to make predictions in the absence of suspended sediment data. For whitewater, the categorical SSC representation yielded superior predictive ability compared to the inclusion of $\ln SSC$ into the model.

The coefficient of variation of digital camera images was tested as a proxy for albedo in relation to aeration. The albedo-CV relation approximated a logistic curve, suggesting that the positive relation between albedo and CV flattens as images become more visibly white as light-coloured pixels saturate the image at high flows. Unfortunately, the magnitude of scatter in the relation is comparable to the range of measured albedo values, limiting the utility of the relation as a predictor.

5.2 Recommendations for future research

This study has quantified the dependence of albedo on the controlling physical processes for mountain streams encompassing a broad range of conditions and developed statistical models to predict stream surface albedo. The statistical models were tested through cross validation, but should be evaluated over a broader range of conditions. In particular, the range of solar elevation angles sampled was limited by the high relief of the study sites and by the latitude and dates of sampling. Therefore, the predictive models should be further tested at sites that experience both lower and higher solar elevation angles than sampled here. In this study, only suspended sediment concentration was considered, whereas the effect of suspended sediment on albedo could also be influenced by mineralogy or particle size distribution.

Stream surface albedo varies both spatially and temporally across the stream surface. Measurements of albedo, including those in this study, have been measured at isolated points over the stream surface that may not be representative of the overall albedo of the stream surface. Future work should consider methods for upscaling these existing point models or developing alternative models that account for whole-surface albedo.

The relation between albedo and discharge found in this study was weak and thus not incorporated into the whitewater albedo models. Further, the relation between albedo and discharge is location-specific and may vary on a fine spatial scale. In order to address spatial complexities in the discharge-aeration relation and to increase the predictive

ability of the whitewater albedo models, future work should continue to investigate the relationship between albedo and aeration as a function of streamflow and channel morphology (e.g., slope, bed roughness, hydraulic geometry).

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